

Precision Measurement of Electroproduction of π^0 Near Threshold

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and

Hall A collaboration

Background

Because the coupling between quarks in QCD increases at low energies, normal perturbation theory does not work at low energy.

There is a effective theory known as chiral perturbation theory(ChPT) that is expected to work well at low Q^2 , low energy and momentum

ChPT

Start with a Lagrangian embodying the underlying symmetries of QCD expressed in terms of the relevant degrees of freedom: the pion and nucleon.

Scattering or production processes can be described in terms of small quantities Q/M , and m_π/M .

The detail of interaction are absorbed into parameters called Low Energy Constants(LEC's), which obtained by measurement. Once LEC's are determined, one can predict the evolution of cross section with Q^2 and W (center of mass energy of the π -N system).

Differential cross section

The differential cross section for pion electro-production using an unpolarized electron beam can be written as

$$\frac{d\sigma}{d\Omega_e d\Omega_\pi^{cm} dE'} = \Gamma \left\{ \frac{d\sigma_T}{d\Omega_\pi^{cm}} + \epsilon_L \frac{d\sigma_L}{d\Omega_\pi^{cm}} + [2\epsilon_L(1+\epsilon)]^{1/2} \frac{d\sigma_{LT}}{d\Omega_\pi^{cm}} \cos \phi + \epsilon \frac{d\sigma_{TT}}{d\Omega_\pi^{cm}} \cos 2\phi \right\}$$

The transverse and longitudinal photon polarization parameters, ϵ and ϵ_L , and the virtual flux factor, Γ are defined as,

$$\epsilon = \frac{1}{1 + 2\vec{q}^2/Q^2 \tan^2 \frac{\theta_e}{2}},$$

$$\epsilon_L = \frac{Q^2}{\nu_{cm}^2} \epsilon,$$

$$\Gamma = \frac{\alpha E' k_\gamma}{2\pi^2 E Q^2 (1 - \epsilon)},$$

$$k_\gamma = \frac{W^2 - m^2}{2m},$$

$$\nu_{cm} = \frac{W^2 - m^2 - Q^2}{2W}.$$

S and P Waves Give 7 Pion Multipoles

$$\bullet \frac{d\sigma_T}{d\Omega_{\pi}^{\text{cm}}} = |E_{0+}|^2 + \frac{1}{2} (|P_2|^2 + |P_3|^2) + 2 \operatorname{Re}(E_{0+} P_1^*) \cos \theta_{\pi}^* + (|P_1|^2 - \frac{1}{2} (|P_2|^2 + |P_3|^2)) \cos^2 \theta_{\pi}^*$$

$$\bullet \frac{d\sigma_L}{d\Omega_{\pi}^{\text{cm}}} = (|L_{0+}|^2 + |P_5|^2) + 2 \operatorname{Re}(L_{0+} P_4^*) \cos \theta_{\pi}^* + (|P_4|^2 - |P_5|^2) \cos^2 \theta_{\pi}^*$$

$$\bullet \frac{d\sigma_{TT}}{d\Omega_{\pi}^{\text{cm}}} = \frac{1}{2} (|P_2|^2 - |P_3|^2) \sin^2 \theta_{\pi}^*$$

$$\bullet \frac{d\sigma_{LT}}{d\Omega_{\pi}^{\text{cm}}} = -\operatorname{Re}(L_{0+} P_2^* + E_{0+} P_5^*) \sin \theta_{\pi}^* - \operatorname{Re}(P_1 P_5^* + P_4 P_2^*) \sin \theta_{\pi}^* \cos \theta_{\pi}^*$$

S Waves

E_{0+} and L_{0+}

P waves

P_1, P_2, P_3, P_4 , and P_5

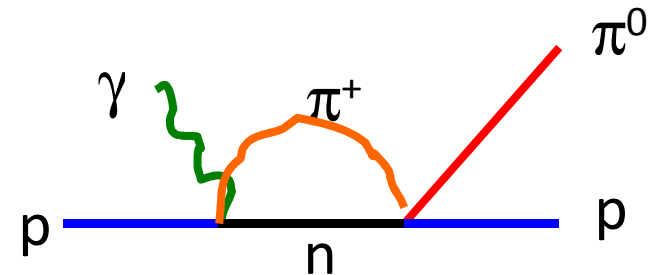
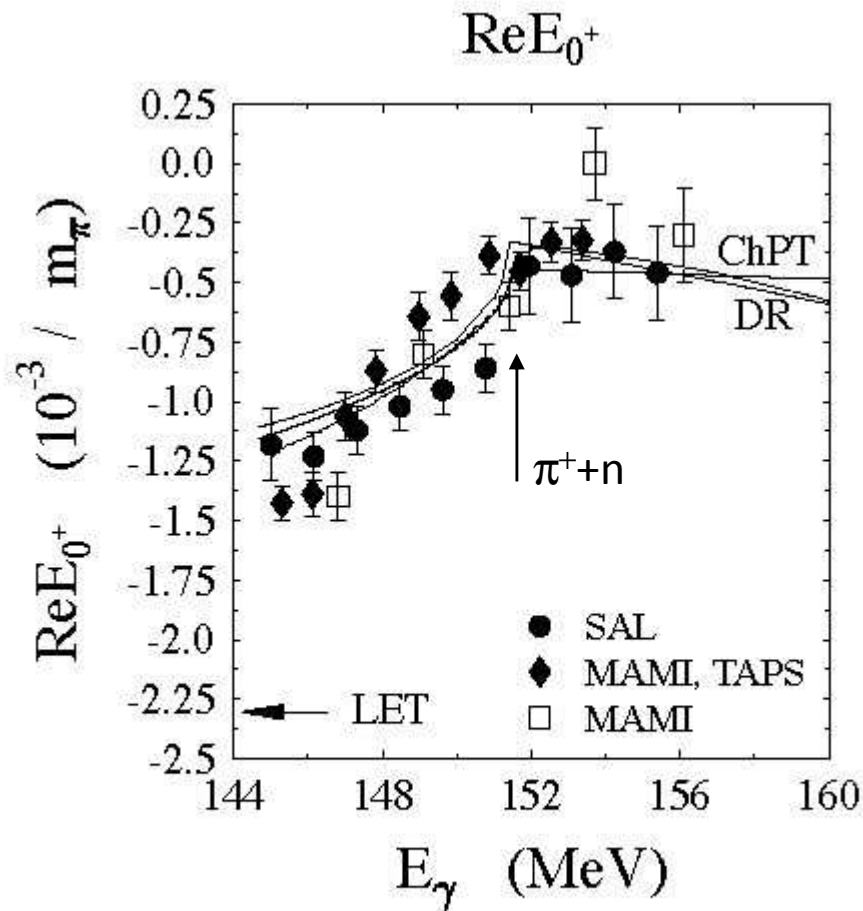
Previous experiments

π^0 -photo production on the proton $Q^2=0$

(Unitary Cusp)

$$\gamma + p \rightarrow \pi^0 + p$$

$$\gamma + p \rightarrow \pi^+ + n \rightarrow \pi^0 + p$$



Explained by one loop corrections.
Was a real triumph of ChPT.
LEC = 14.84 MeV⁻³ [O (p)³],

Classic LET result is $-2.3 \times 10^{-3}/m_\pi$. (Born terms)

Measured value is $-1.3 \times 10^{-3}/m_\pi$

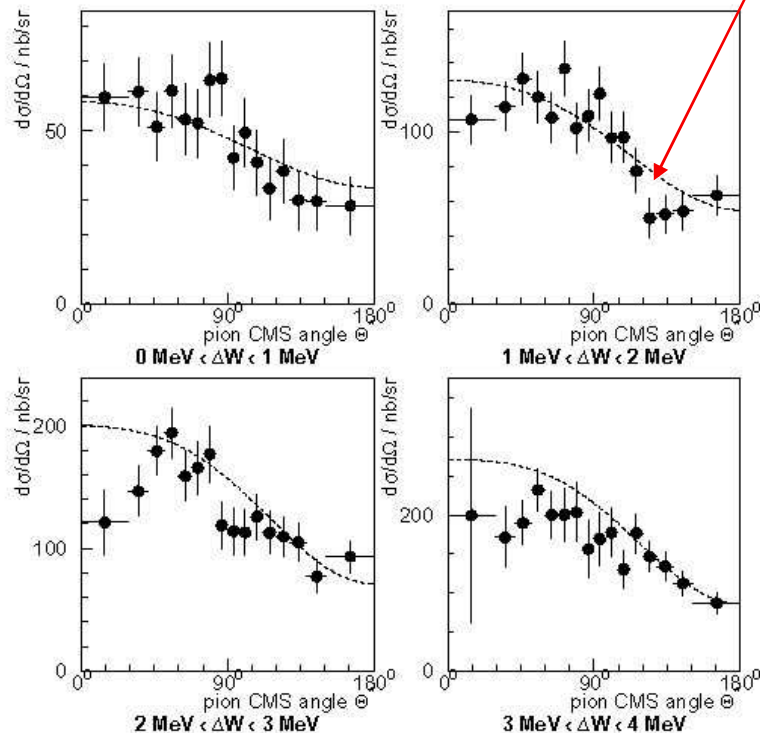
π^0 -electro production on the proton

$$\sigma_T(\theta_\pi^*) + \varepsilon_L \sigma_L(\theta_\pi^*)$$

ChPT

ChPT -----
MAID -----
Fit s+p -----

$Q^2 = 0.10 \text{ (GeV/c)}^2$

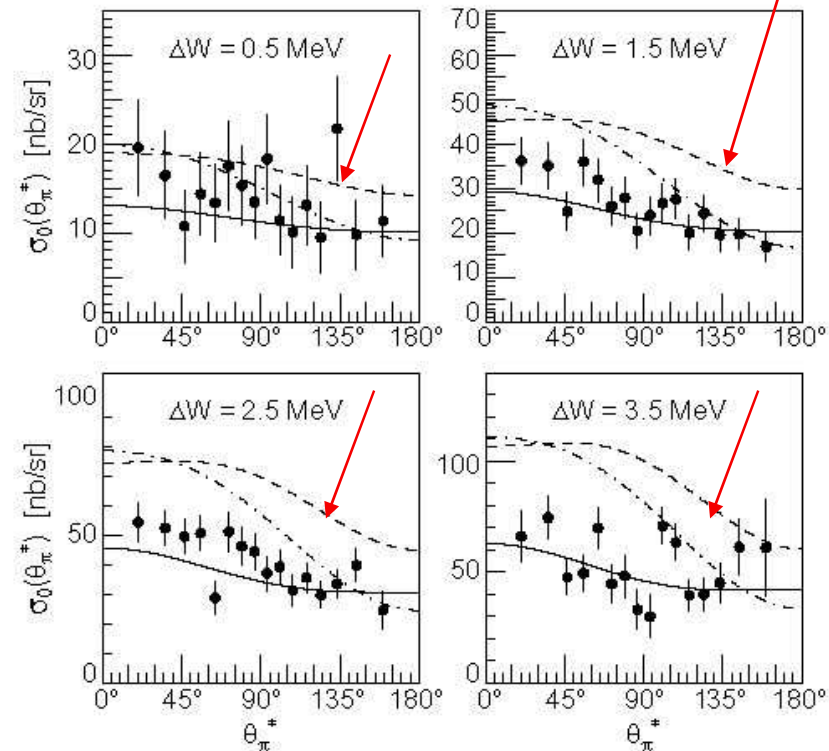


Distler et al. PRL 80, 2294 (1998)

Fixes LEC's

$a_3 = -0.92$ and $a_4 = -0.99$

$Q^2 = 0.05 \text{ (GeV/c)}^2$

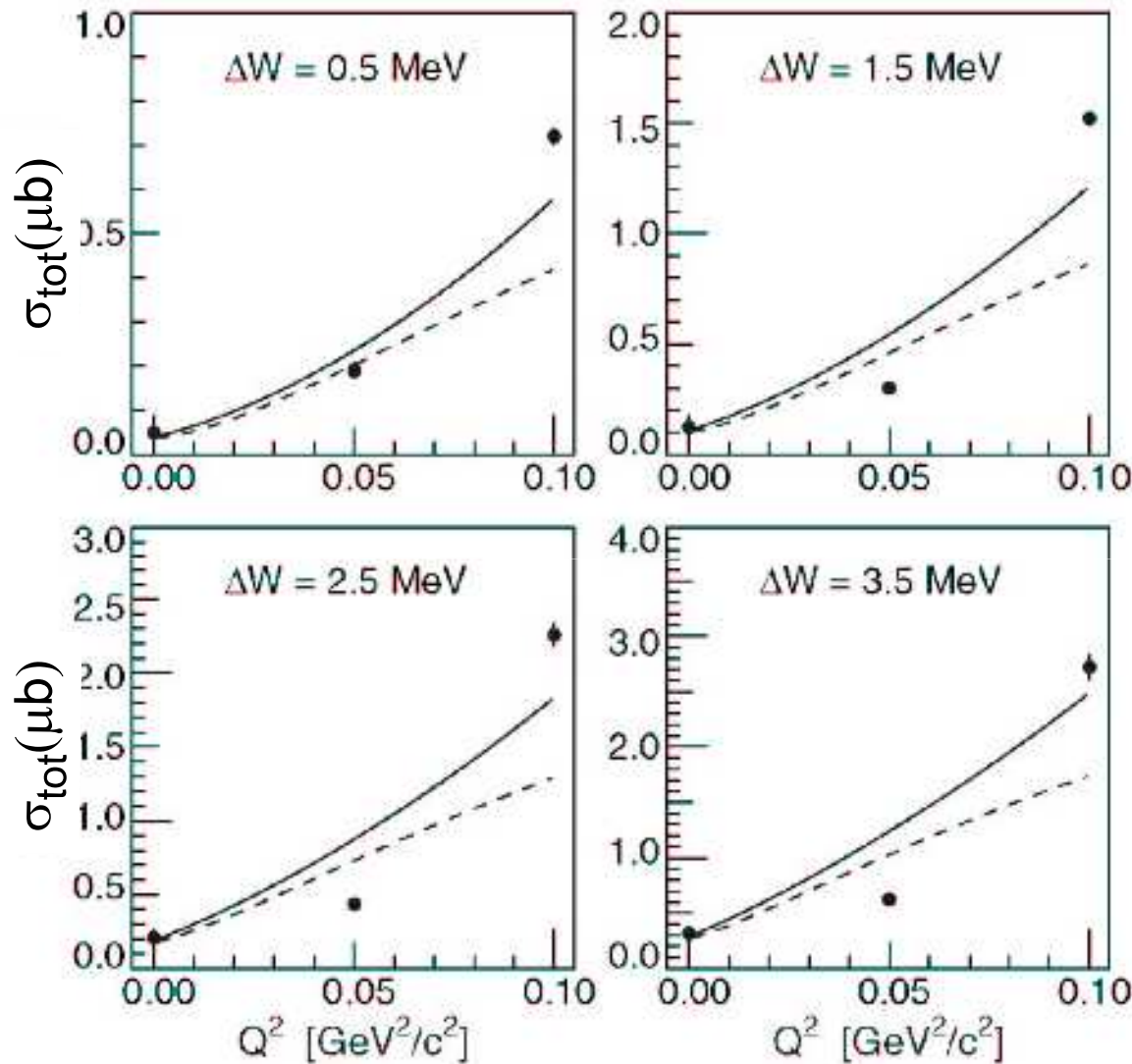


Merkel et al. PRL 88, 12301 (2002)

Shows the quality of the fit to the data that determines LECs. ChPT prediction gets progressively worse away from threshold.

ChPT Bernard et al.
NP A607, 379(1996)

π^0 -electro production on the proton



$Q^2=0.10 \text{ (GeV/c)}^2$
Distler PRL 80, 2294 (1998)

LEC's
 $a_3 = -0.92$ and $a_4 = -0.99$

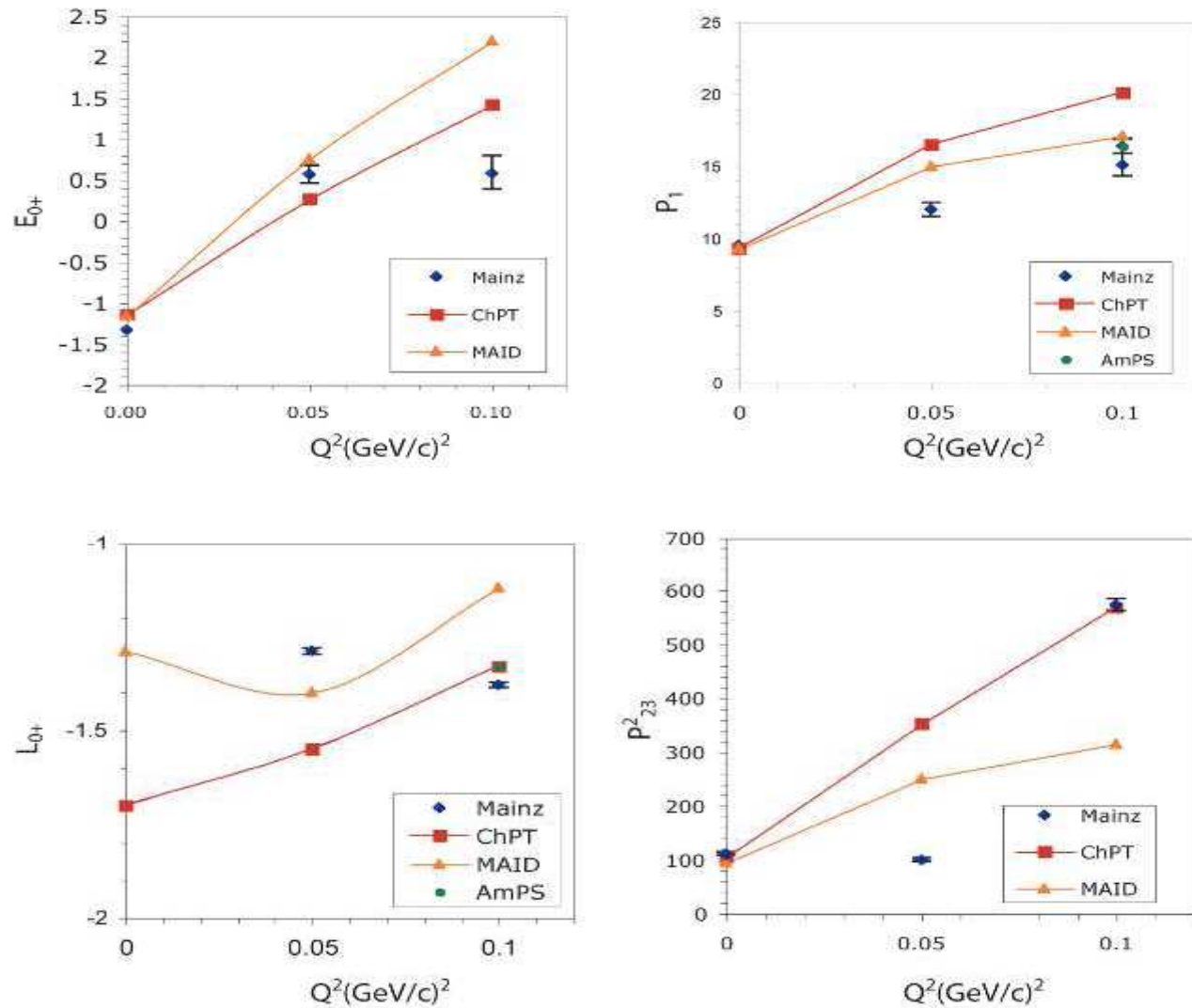
$Q^2=0.05 \text{ (GeV/c)}^2$
Merkel et al. PRL 88, 1230 (2002)

ChPT ———
Bernard, et al. NP A607, 379(1996)

MAID -----

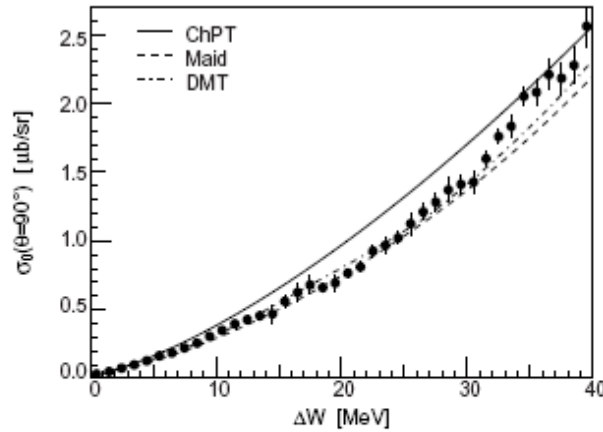
- Large deviations between ChPT and data
- Need data in a finer grid in Q^2

π^0 -electro production on the proton

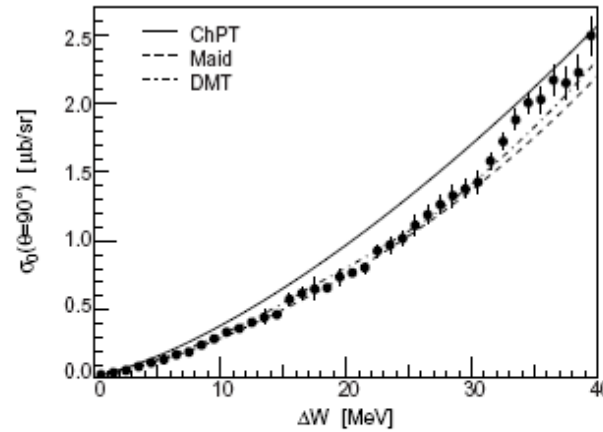


Mainz data are from Distler PRL80 (1998) 2294 and Merkel PRL. 88 (2002)12301
 AmPS NIKHEF data are from Welch PRL 69 (1992) 2761

(a) Model dependent



(b) Model independent



π^0 -electro production on the proton $Q^2=0.05$

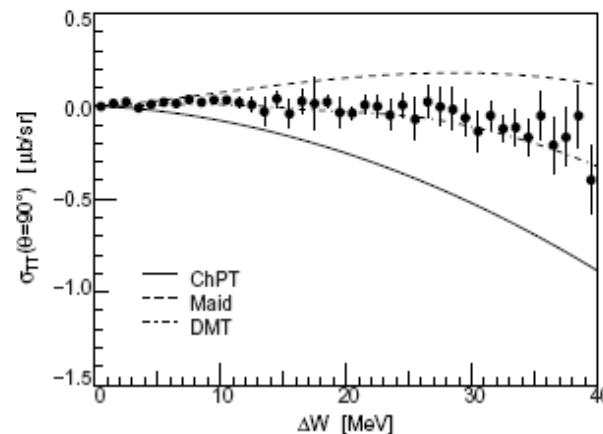
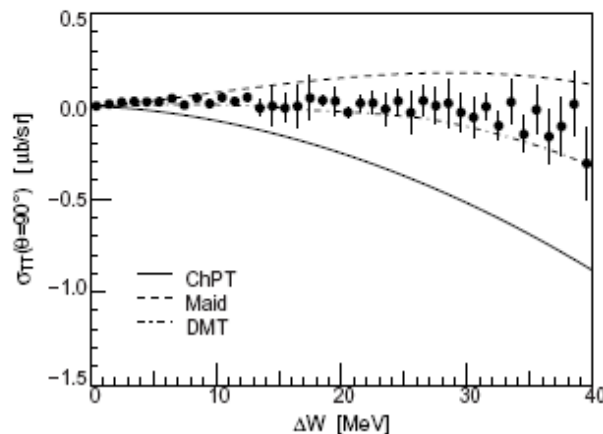
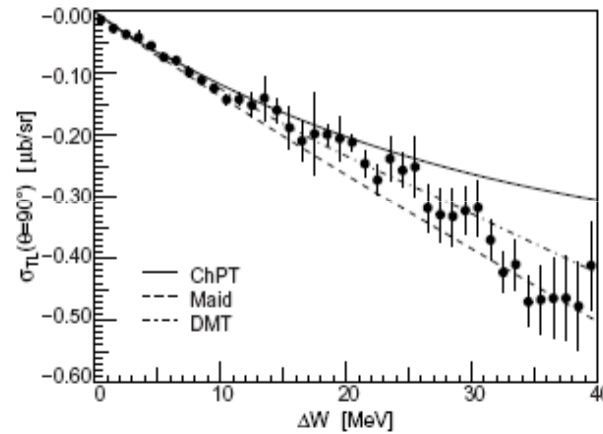
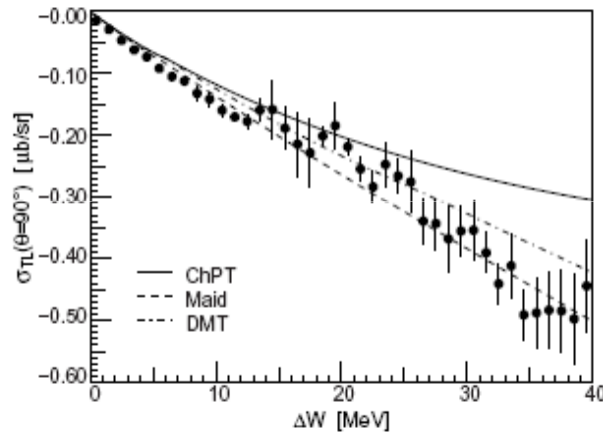
From MAMI recent experiment

Weis, Eur. Phys. J. A 38,
27-33(2008)

By the cut in θ a large fraction of events was lost. In addition, the acceptance in θ was different for each kinematical setting. To overcome these two problems, a second, model-dependent method was used to separate the cross-sections. In this method, the phenomenological model MAID was used as parameterization of the cross-section. For each event, the differential cross-section was projected to the nominal kinematics at $\theta = 90^\circ$ by

$$\sigma(90^\circ, \phi) = \sigma(\theta, \phi) \frac{\text{MAID}(90^\circ, \phi)}{\text{MAID}(\theta, \phi)}.$$

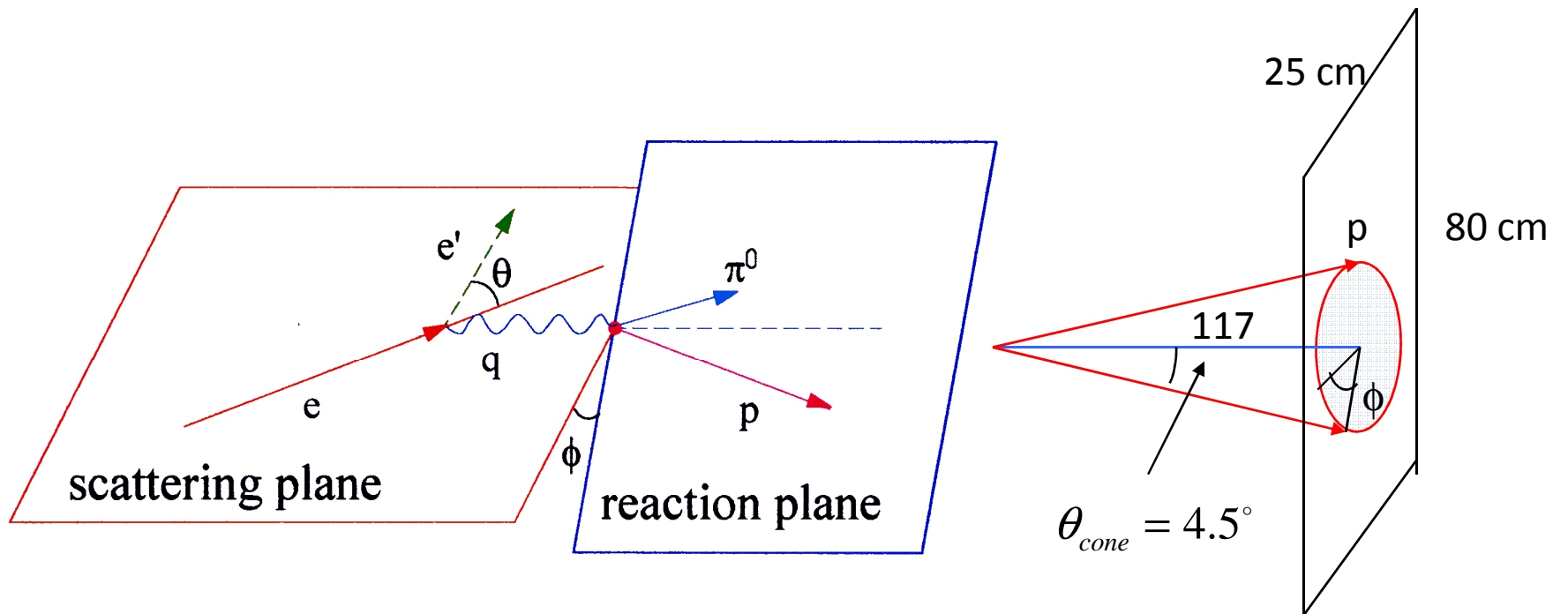
By this method, the statistical error could be reduced for the price of an additional model error.



The experiment

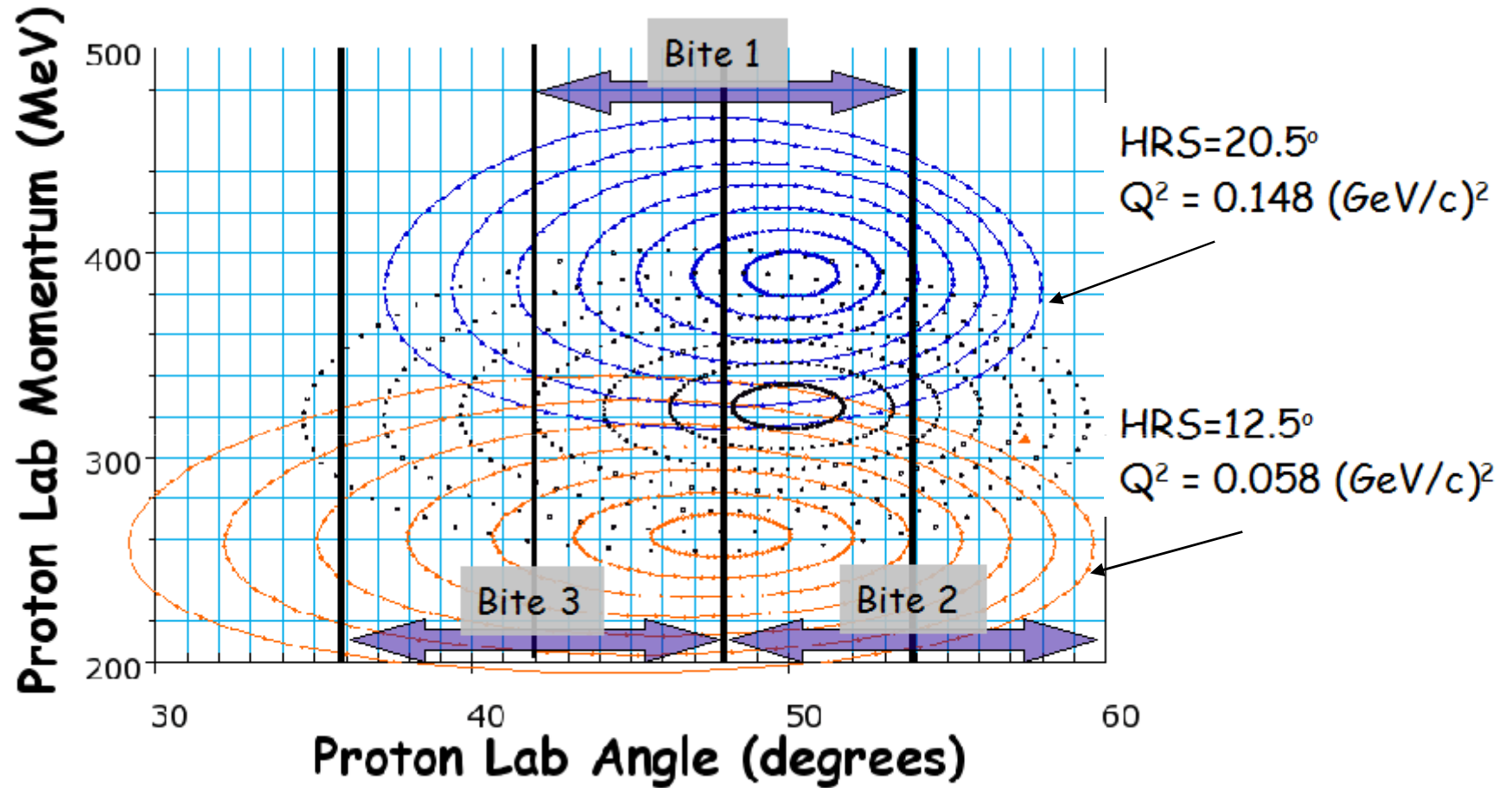
Extract structure functions $\sigma_T + \epsilon_L \sigma_L$, σ_{TL} and σ_{TT} and the asymmetry A_{TL} from $p(e, e'p)\pi^0$ in a fine grid of Q^2 and W from $Q^2 = 0.05 - 0.15$ in steps of 0.01 $(\text{GeV}/c)^2$ and from above threshold $(M + m_\pi)$ $\Delta W = 0 - 20$ MeV in steps of $1 - 2$ MeV.
This results will provide a test of chiral dynamics.

W (MeV)	Above Threshold	Q ² (GeV/c)	θ_{cone} (Deg.)
1075	1.7	- 0.05	4.5
1076	2.7	- 0.10	4.5
1095	22	- 0.10	9



BigBite Solid Angle Vertical $\pm 18^\circ$
 $\sim 100 \text{ msr}$ Horizontal $\pm 5^\circ$

Coverage of bigbite at 1.2 GeV



Ellipses of constant ΔW (W relative to π threshold)

E04-007: Threshold $H(e,e'p)\pi^0$ Layout

Target

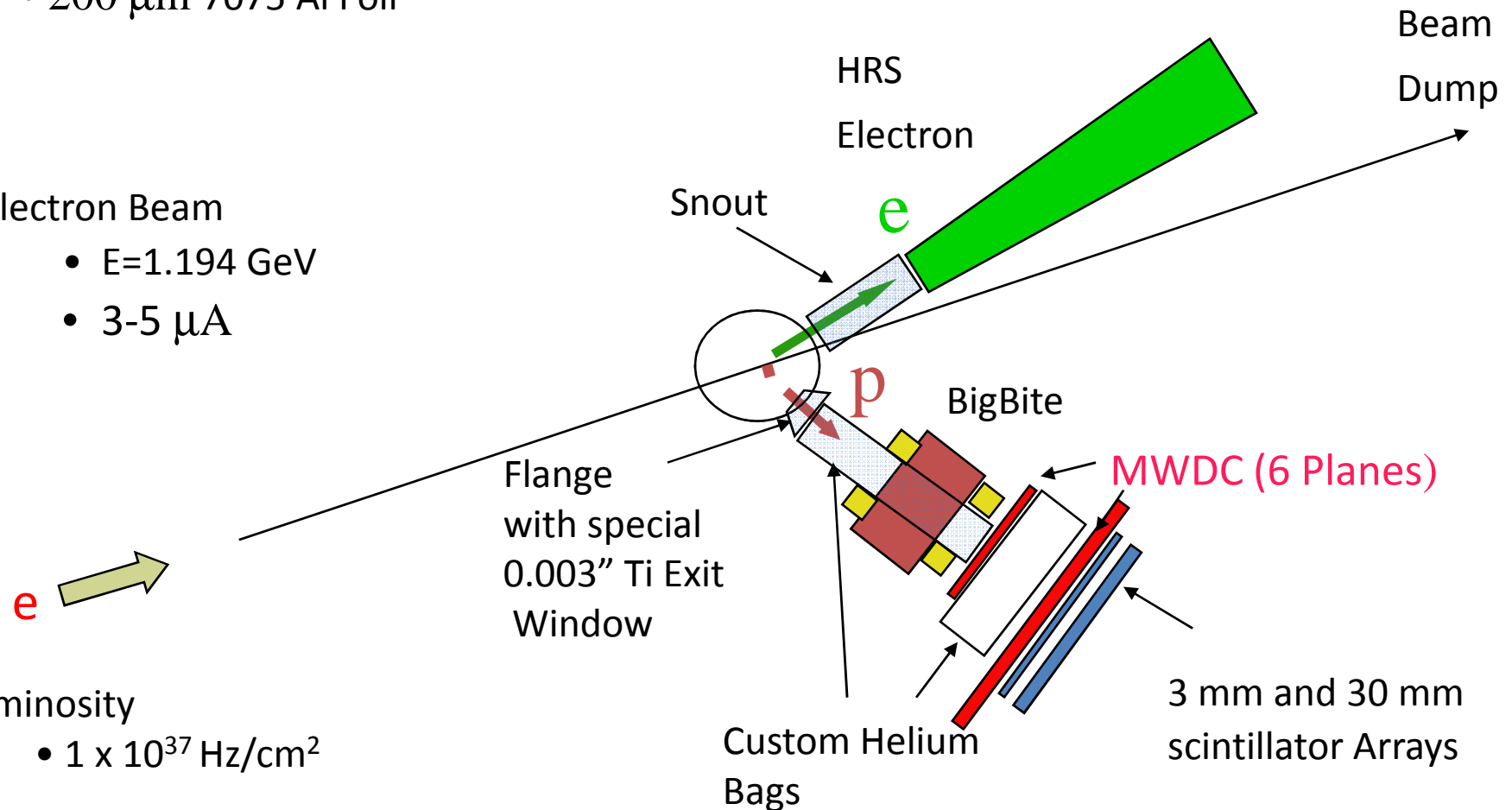
- New 6 cm long, 1" diameter LH2 cell
- 200 μm 7075 Al Foil

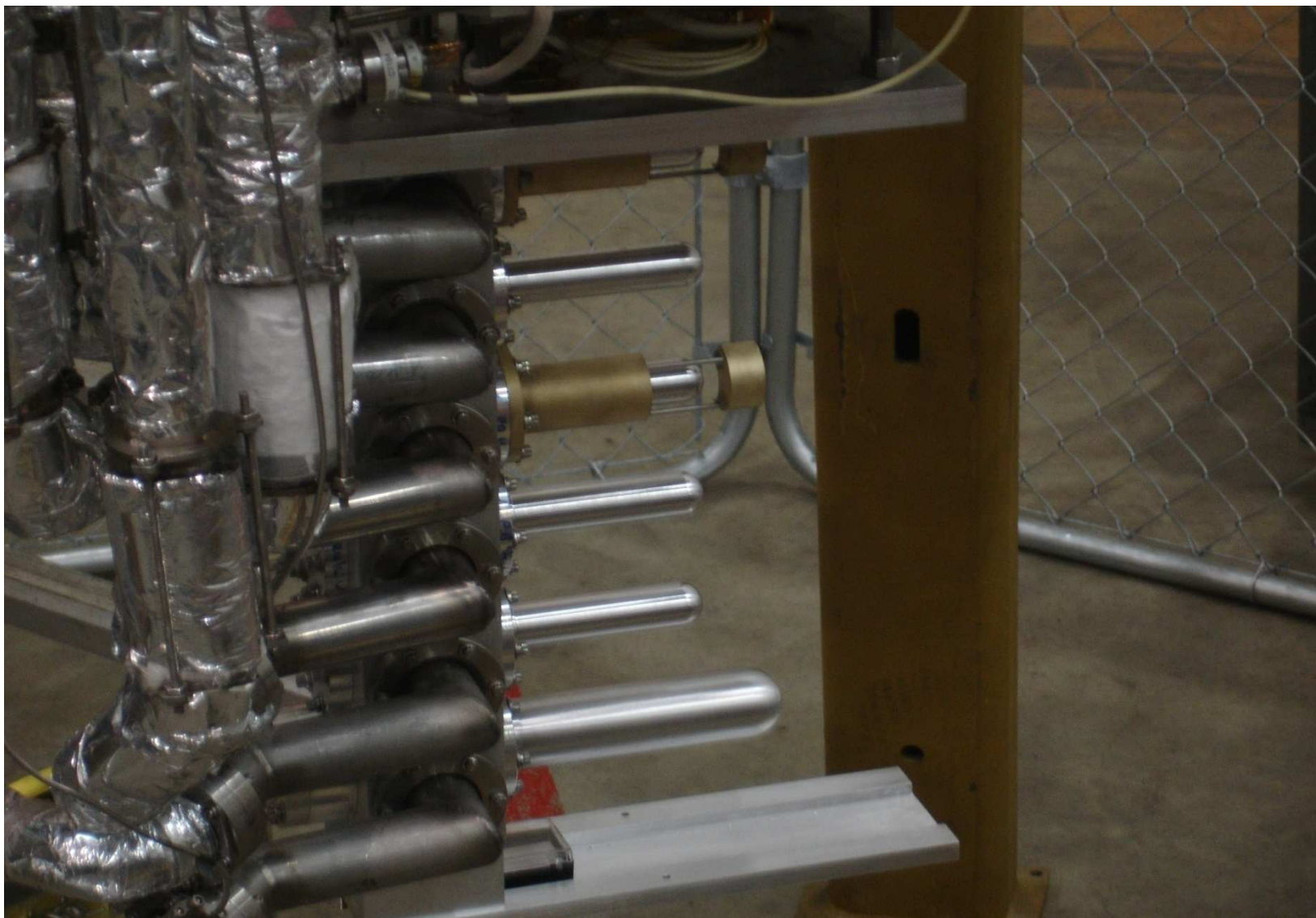
Electron Beam

- $E=1.194$ GeV
- 3-5 μA

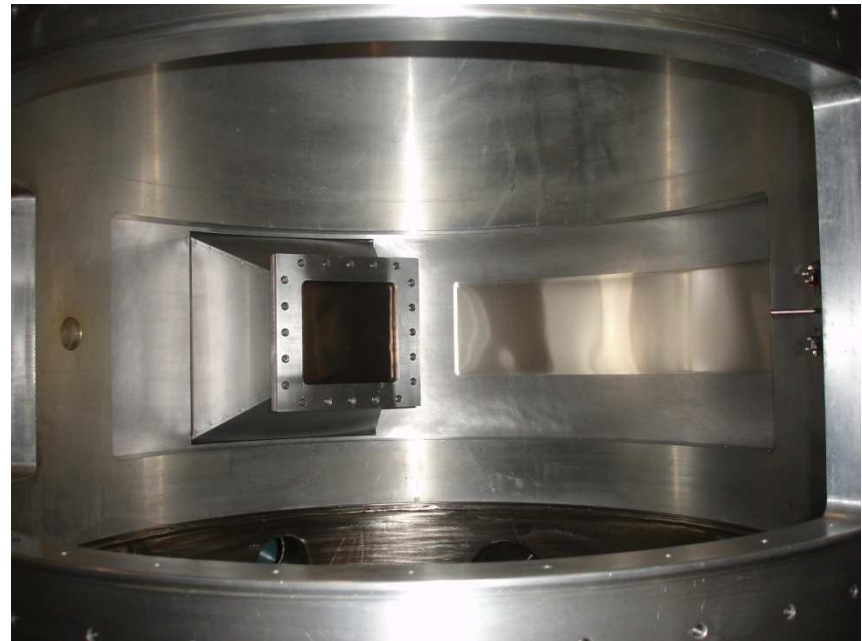
Luminosity

- 1×10^{37} Hz/cm²





Special Flange with 0.003" Ti Window



E04-007: Custom 0.0035" thick polyurethane helium filled balloon

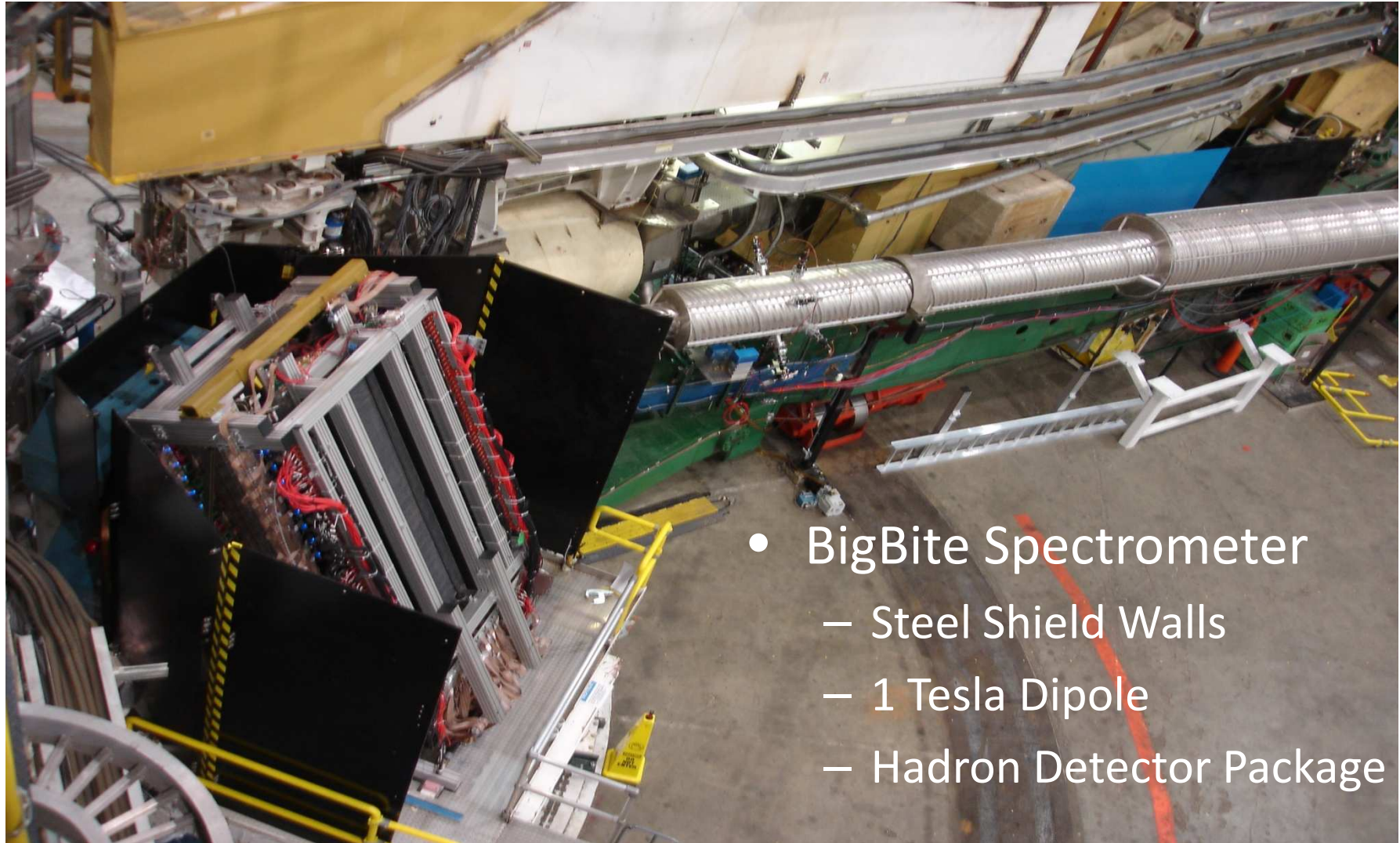


BigBite Arm

- BigBite Dipole Magnet
- Front and back MWDC chambers
- BigBite acceptance matches HRS
Resolution $\Delta p/p = 1\%$
- Two large arrays of Scintillators. One 3 mm thick and the other 30 mm thick as trigger planes form coincident with LHRS and for PID.
- helium bag in magnet gap and between MWDC chambers



E04-007: Installed In Hall A



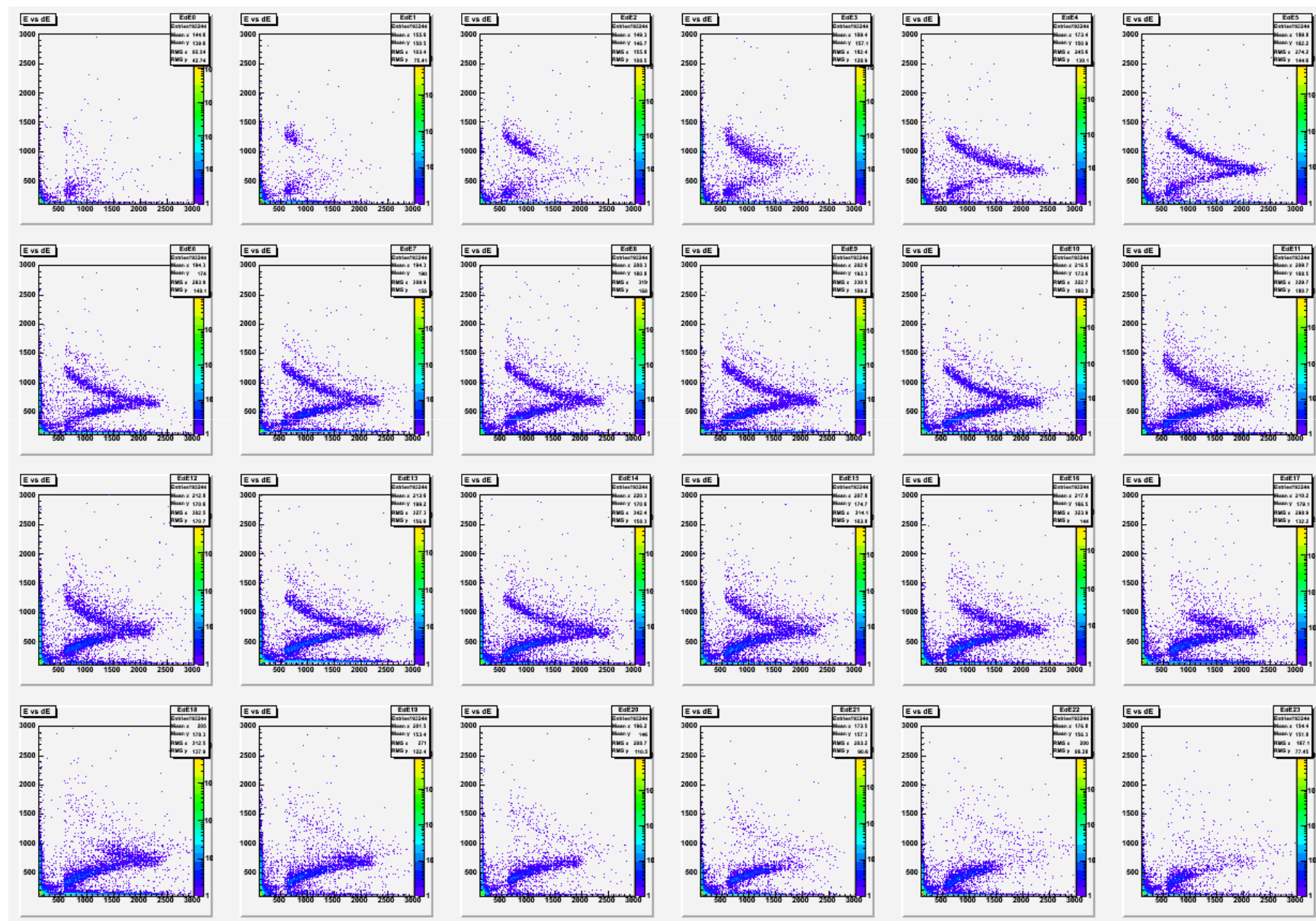
- BigBite Spectrometer
 - Steel Shield Walls
 - 1 Tesla Dipole
 - Hadron Detector Package

E04-007: Calibration Data

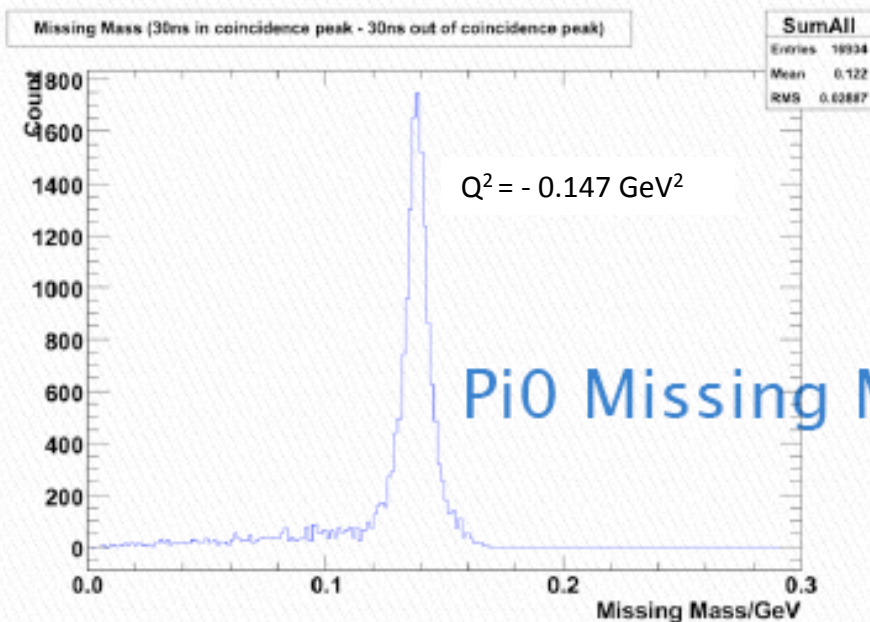
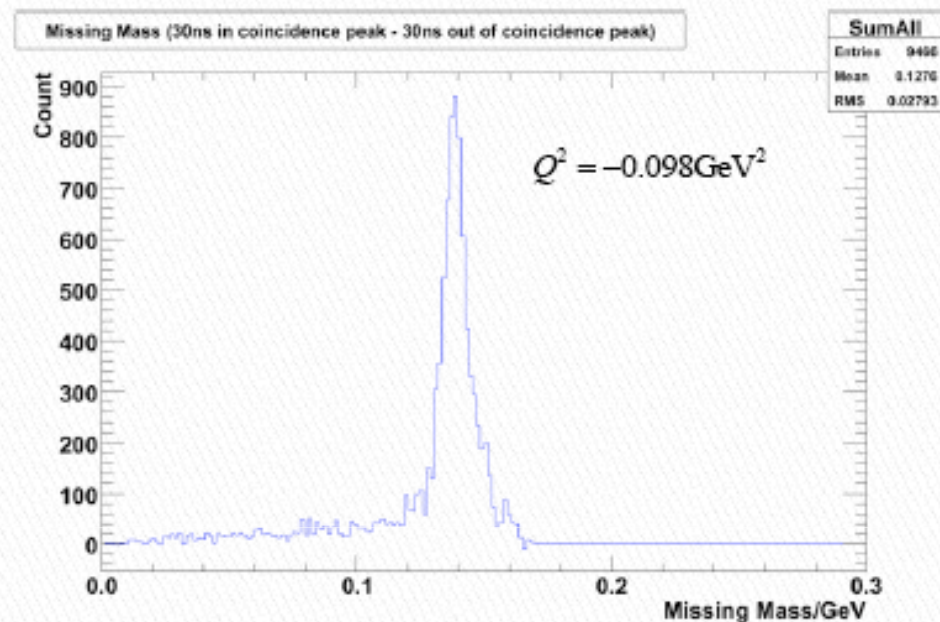
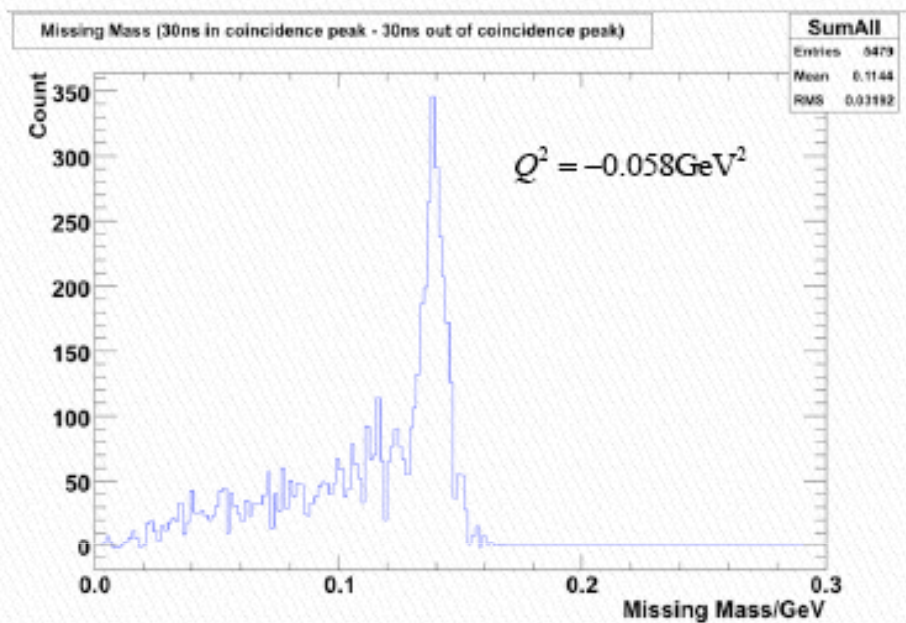
For each production kinematics we took:

- Tantalum elastic - absolute beam energy- electron in HRS
- Proton elastic - electron in HRS, check cross section, proton in BigBite optics
- Carbon elastic and inelastic - check beam energy and cross section
- HRS Sieve slit data with hydrogen elastic
- BigBite Sieve Slit data with Quasi elastic from deuterium for optics
- Hydrogen data with collimated target cell
- Elastic recoil proton data with different currents in BigBite
- Production data with different beam currents (1- 6 ua)
- Data with different wire chamber high voltage and threshold. First time used for protons.
- Electronic 1 KHz pulser in data stream to measure computer dead time correction
- Production data with widely varied prescale factors.

E04-007: E- ΔE from 30 mm and 3 mm paddles



E04-007: BigBite "Online" Optics Jin Huang

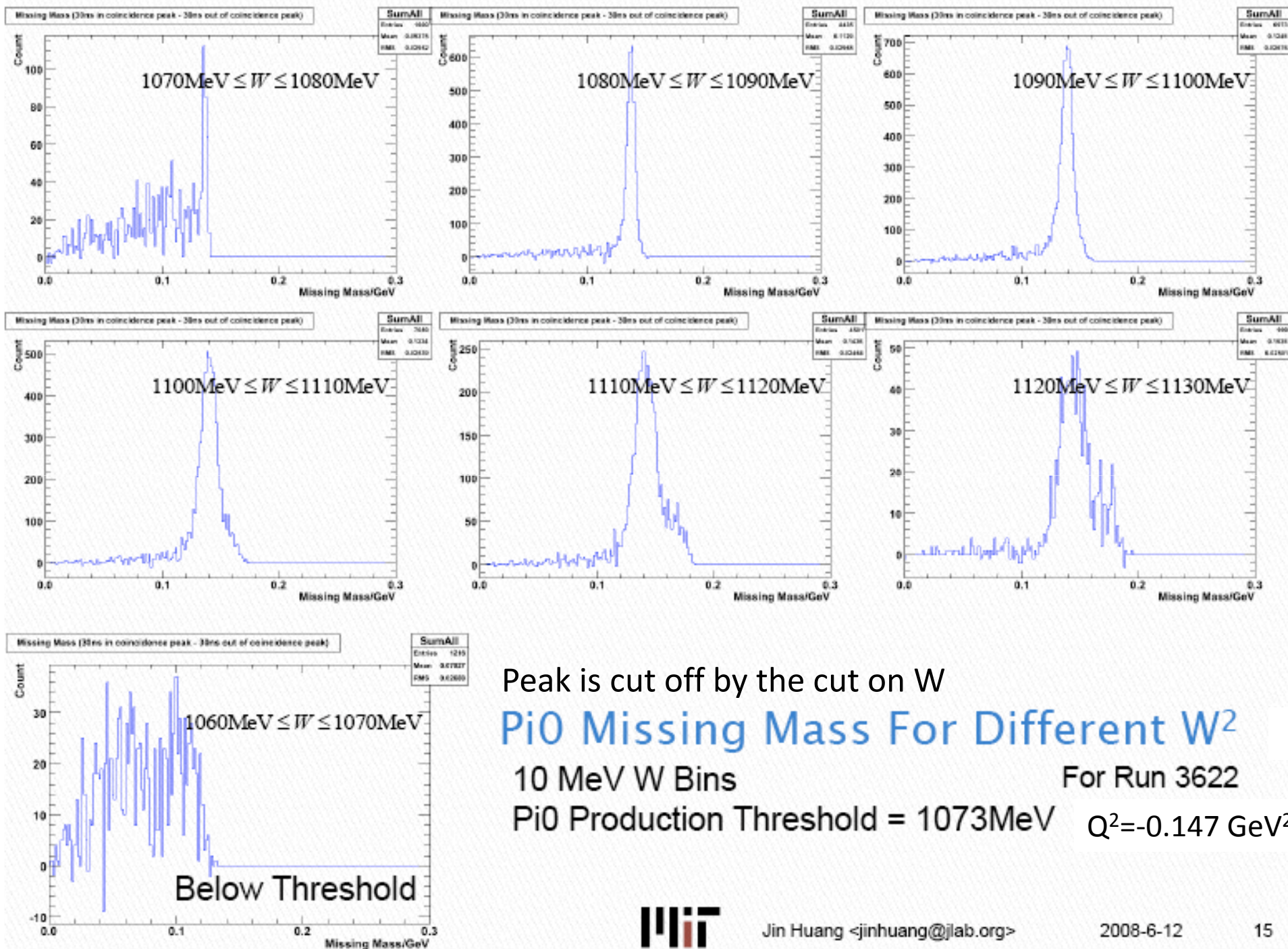


E plane scintillator Trigger

Cut on 30 ns peak - 30 ns background

Cut on W above Threshold

Pi0 Missing Mass For Different Q^2 Run



Peak is cut off by the cut on W

Pi0 Missing Mass For Different W^2

10 MeV W Bins

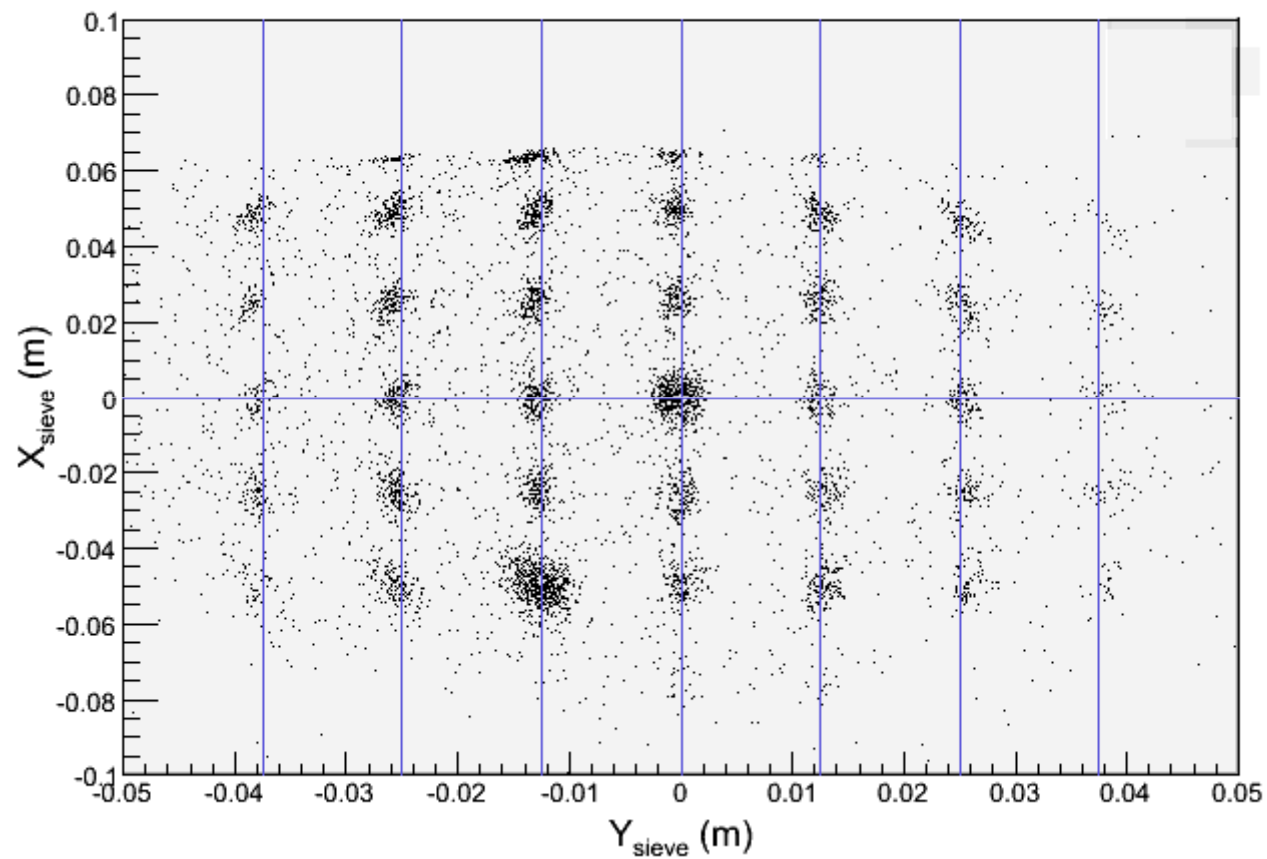
For Run 3622

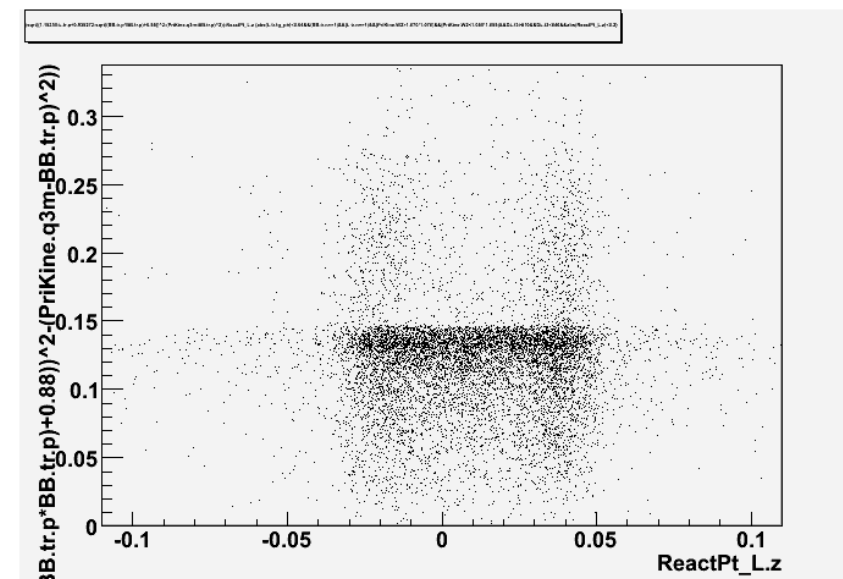
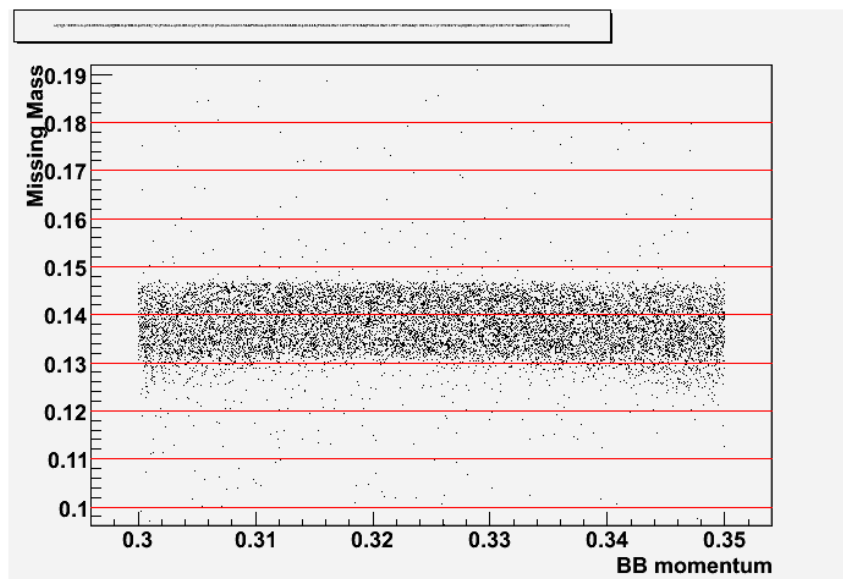
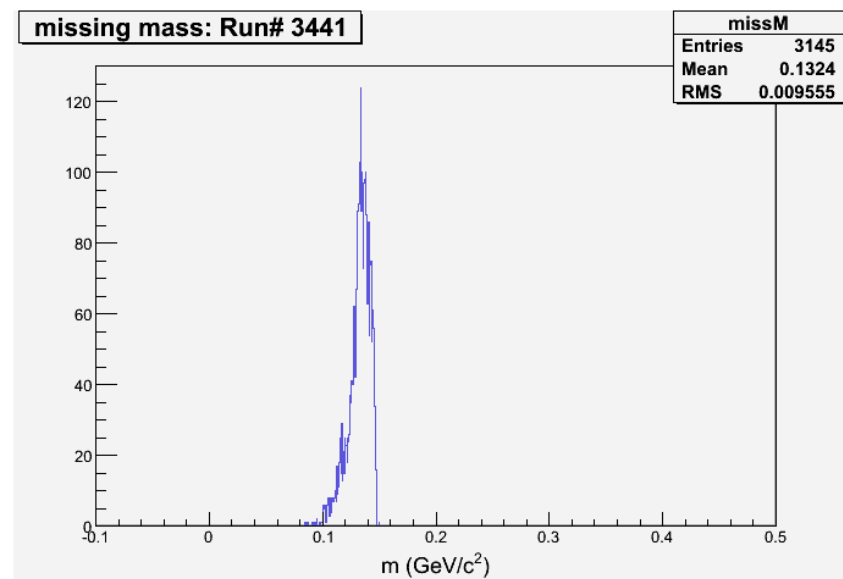
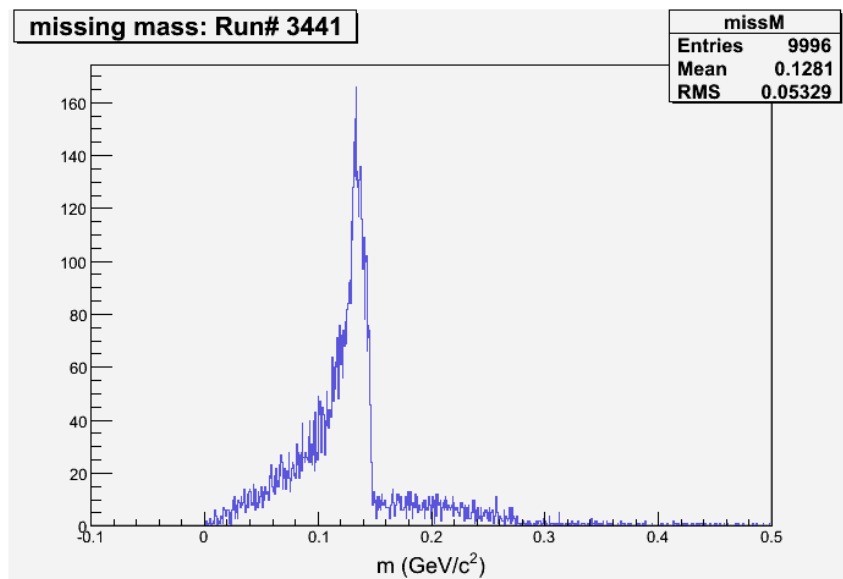
Pi0 Production Threshold = 1073MeV $Q^2 = -0.147 \text{ GeV}^2$



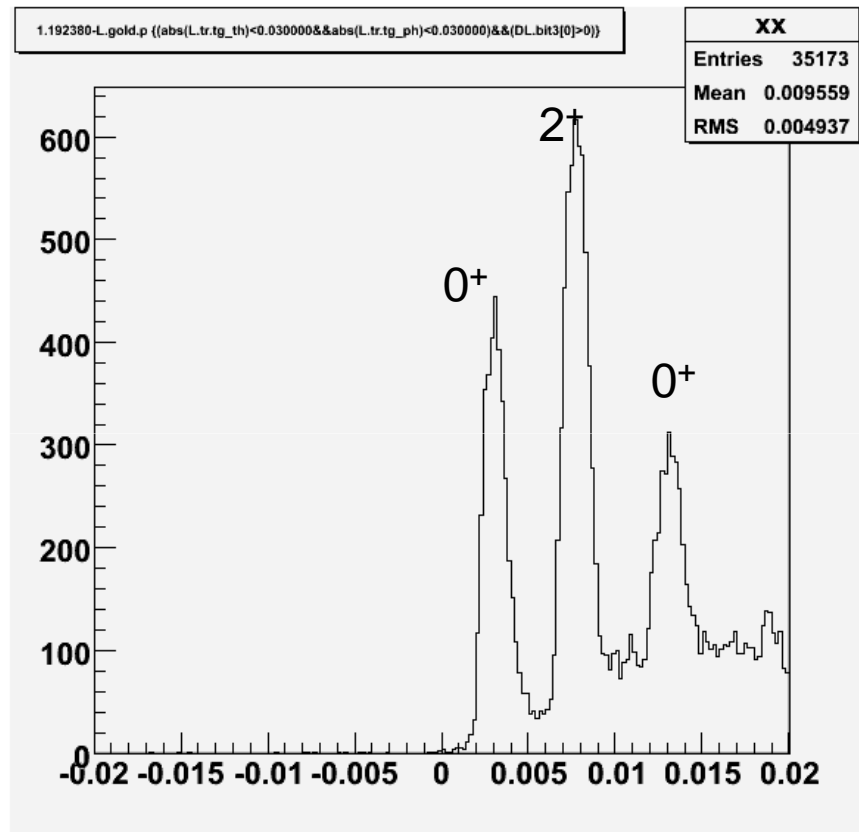
HRS Optics

Sieve: Run 4640 (New Database)

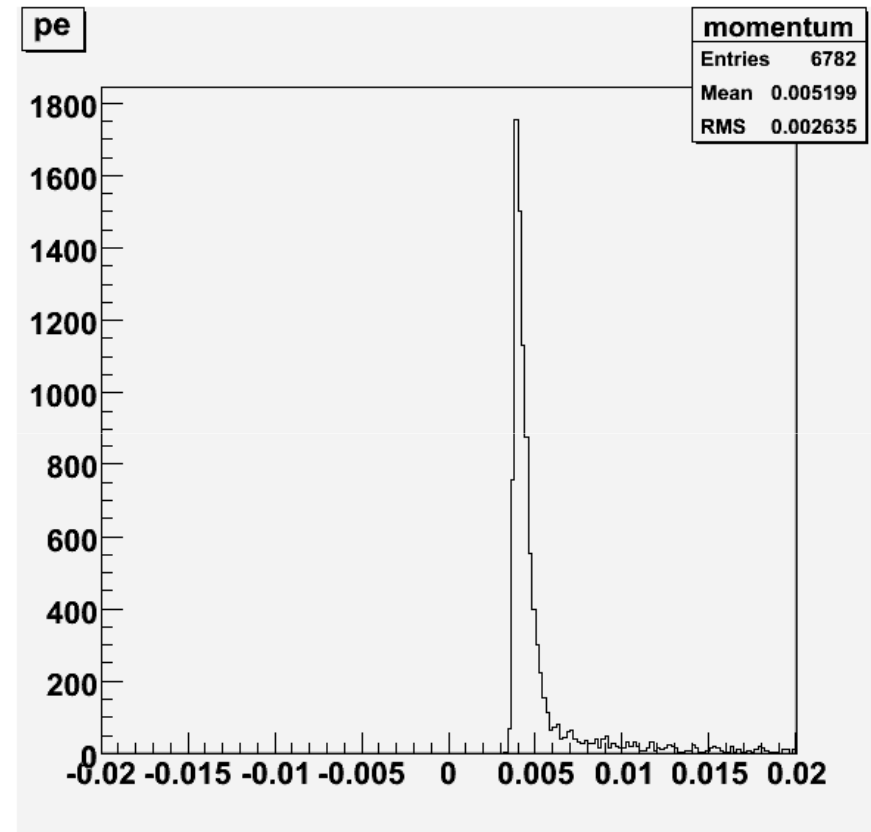




C12 data

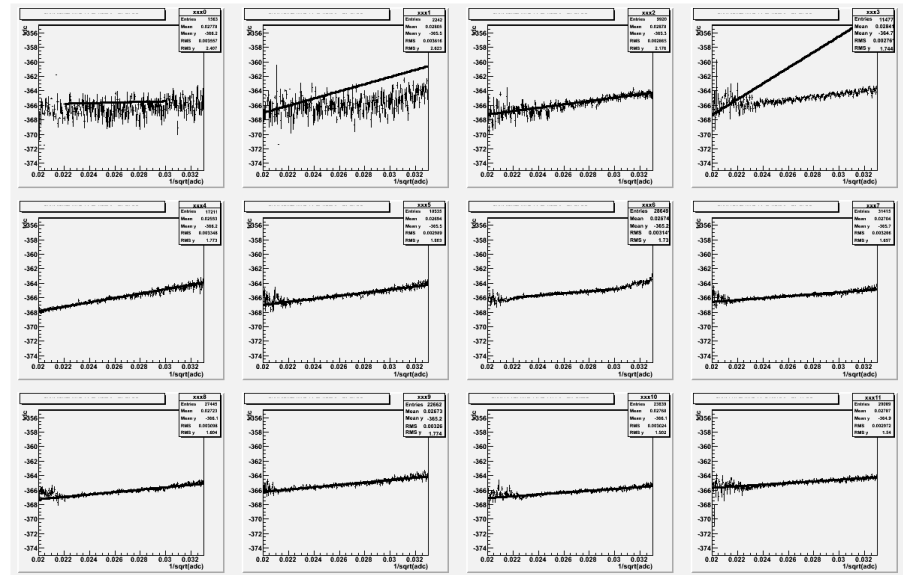
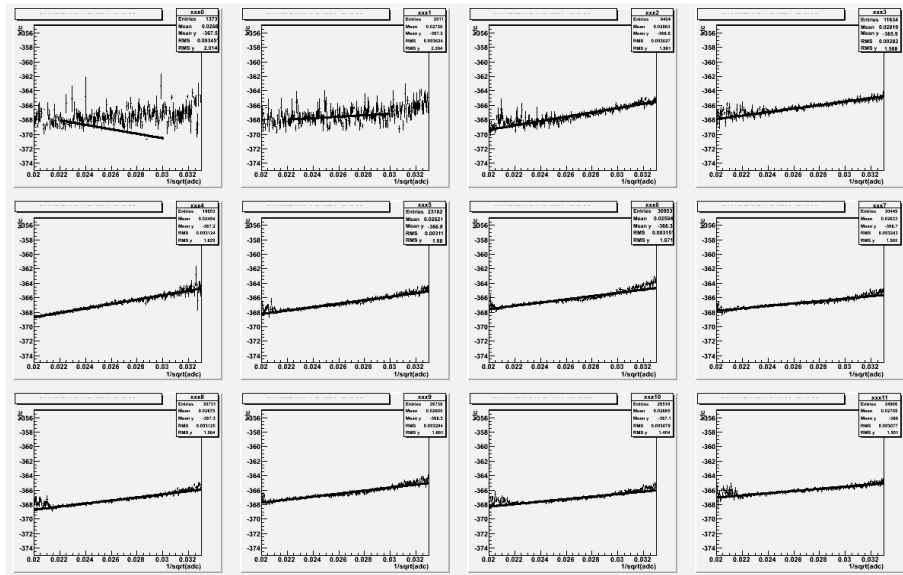
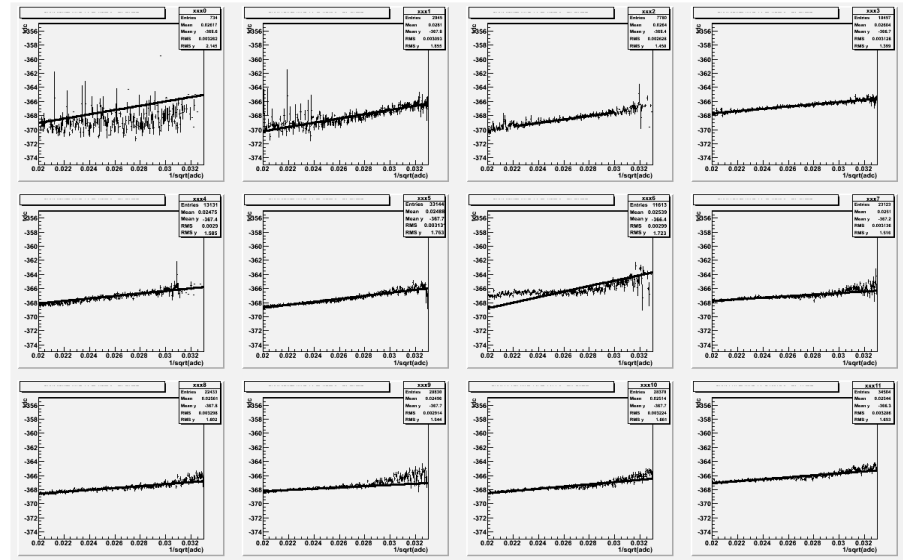
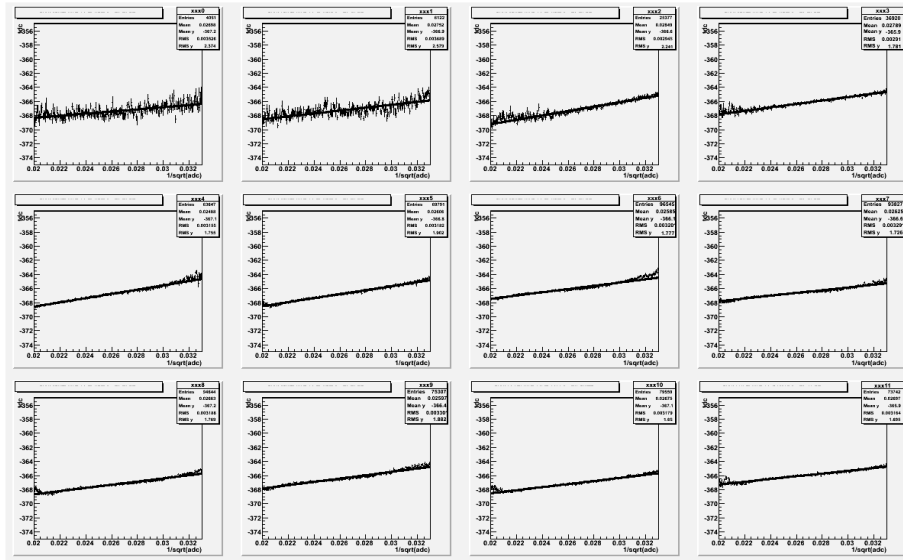


C12 elastic simulation
(from mceep)

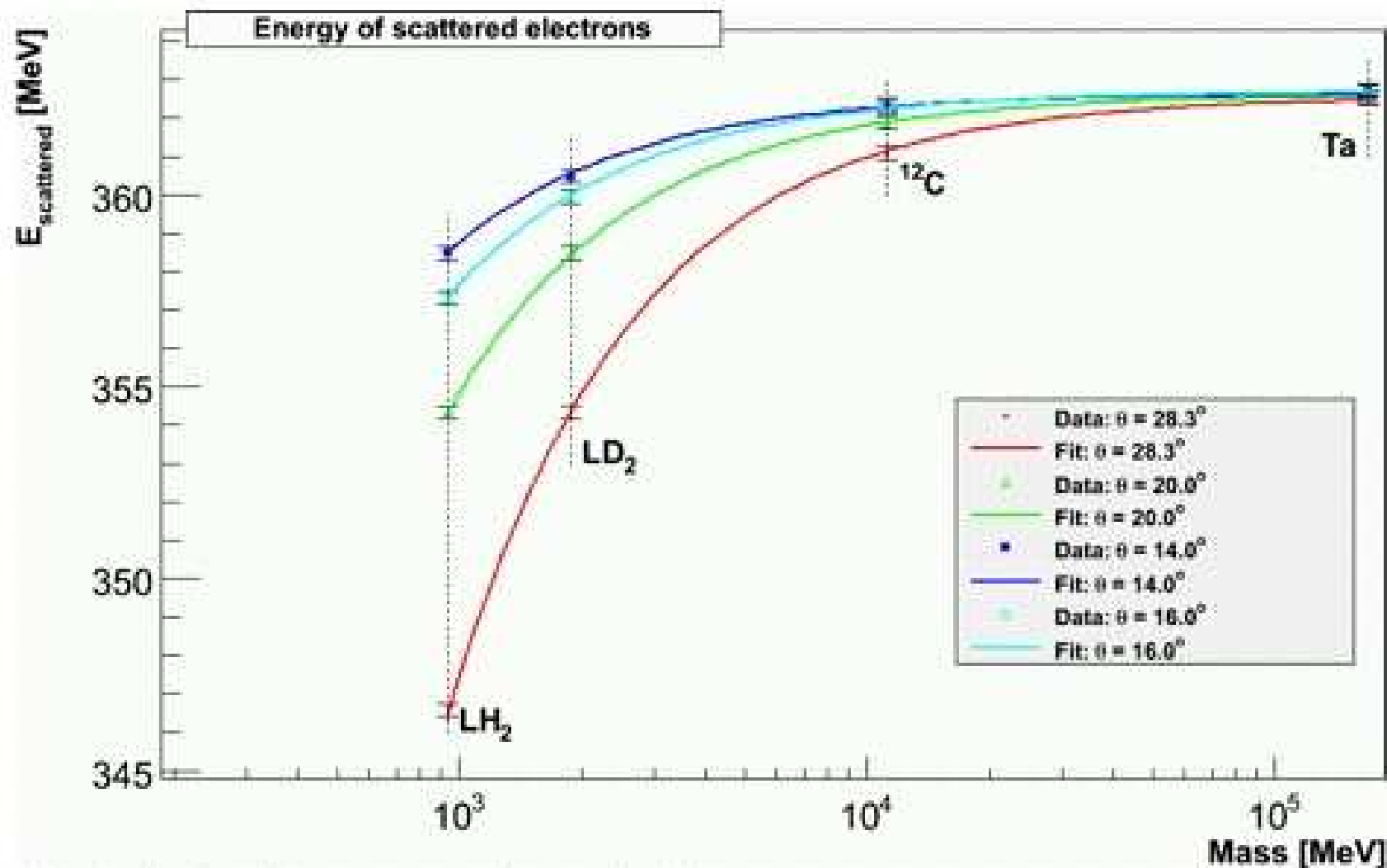


Run 4390

Time walk correction(1/sqrt(adc) vs tdc)



Beam energy determination



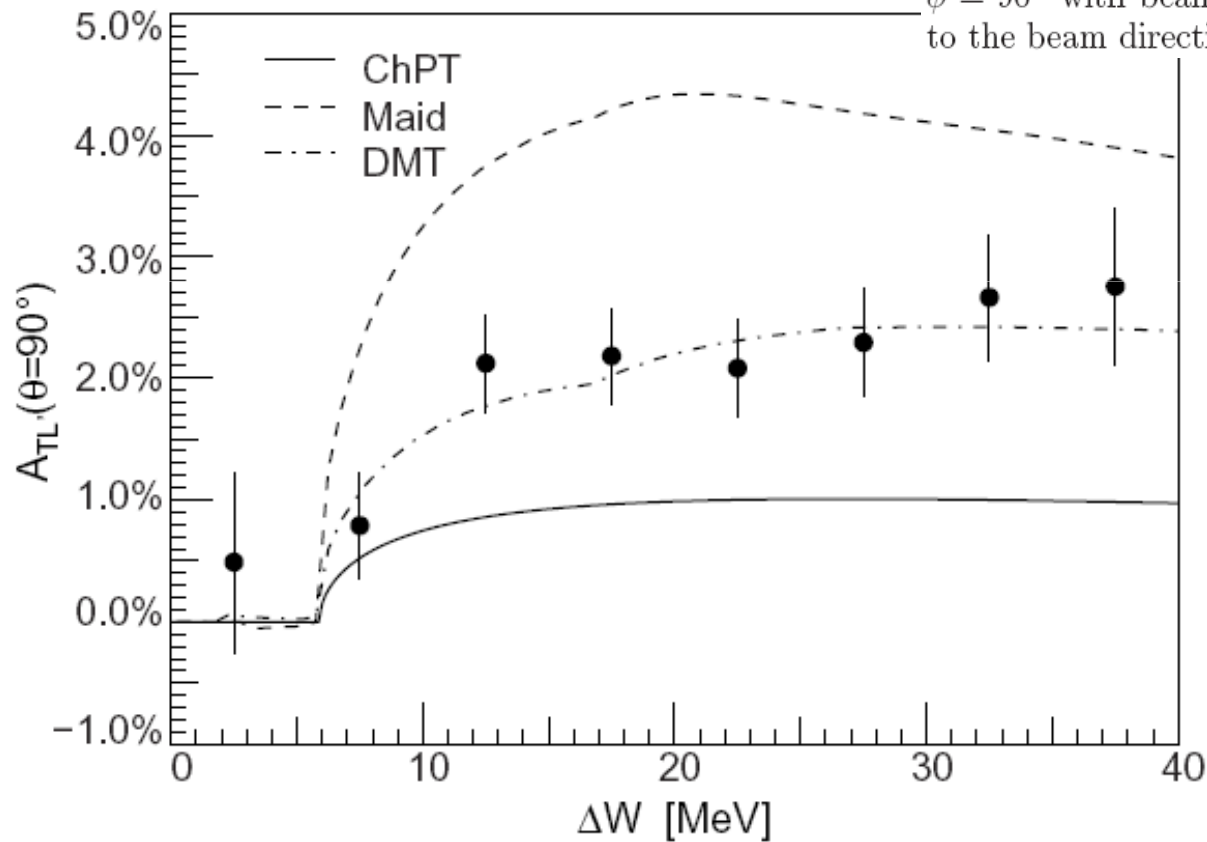
Analysis tool developed using previous data(G0 in Hall C) preliminary error < 0.1%

Miha Mihovilovic
(University of Ljubljana)

Asymmetry

$$A_{LT'}(\theta) = \frac{\sigma^+ - \sigma^-}{\sigma^+ + \sigma^-} = \frac{\sqrt{2\epsilon(1-\epsilon)} \sigma_{LT'}(\theta)}{\sigma_T(\theta) + \epsilon \sigma_L(\theta) - \epsilon \sigma_{TT}(\theta)}$$

where σ^+ and σ^- are the differential cross-sections for $\phi = 90^\circ$ with beam polarization parallel and antiparallel to the beam direction, respectively.



Weis Eur. Phys. J. A 38, 27-33(2008)

From MAMI recent experiment

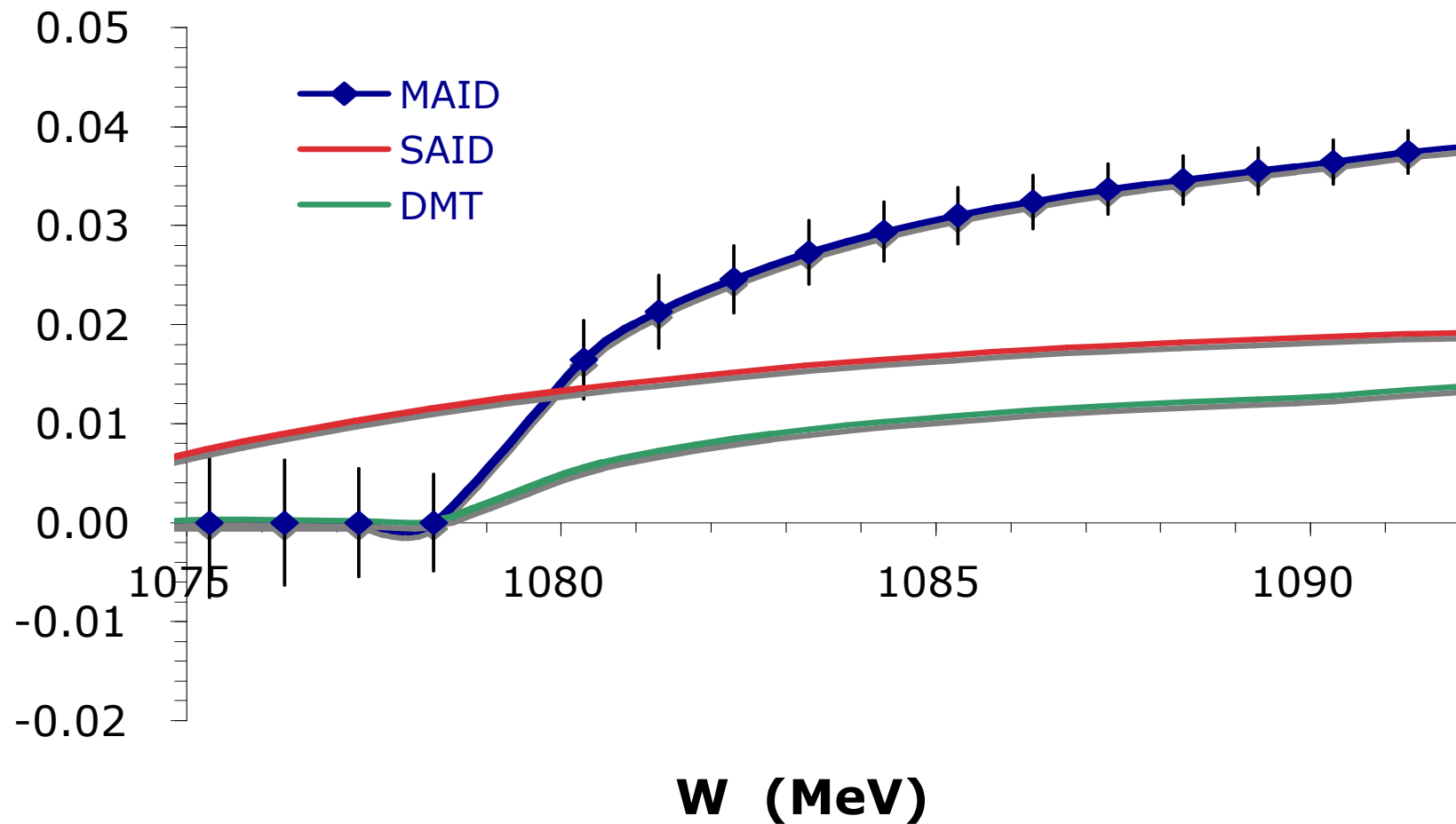
Our accumulated charge will give us

- stat. error from 20% to 5 %

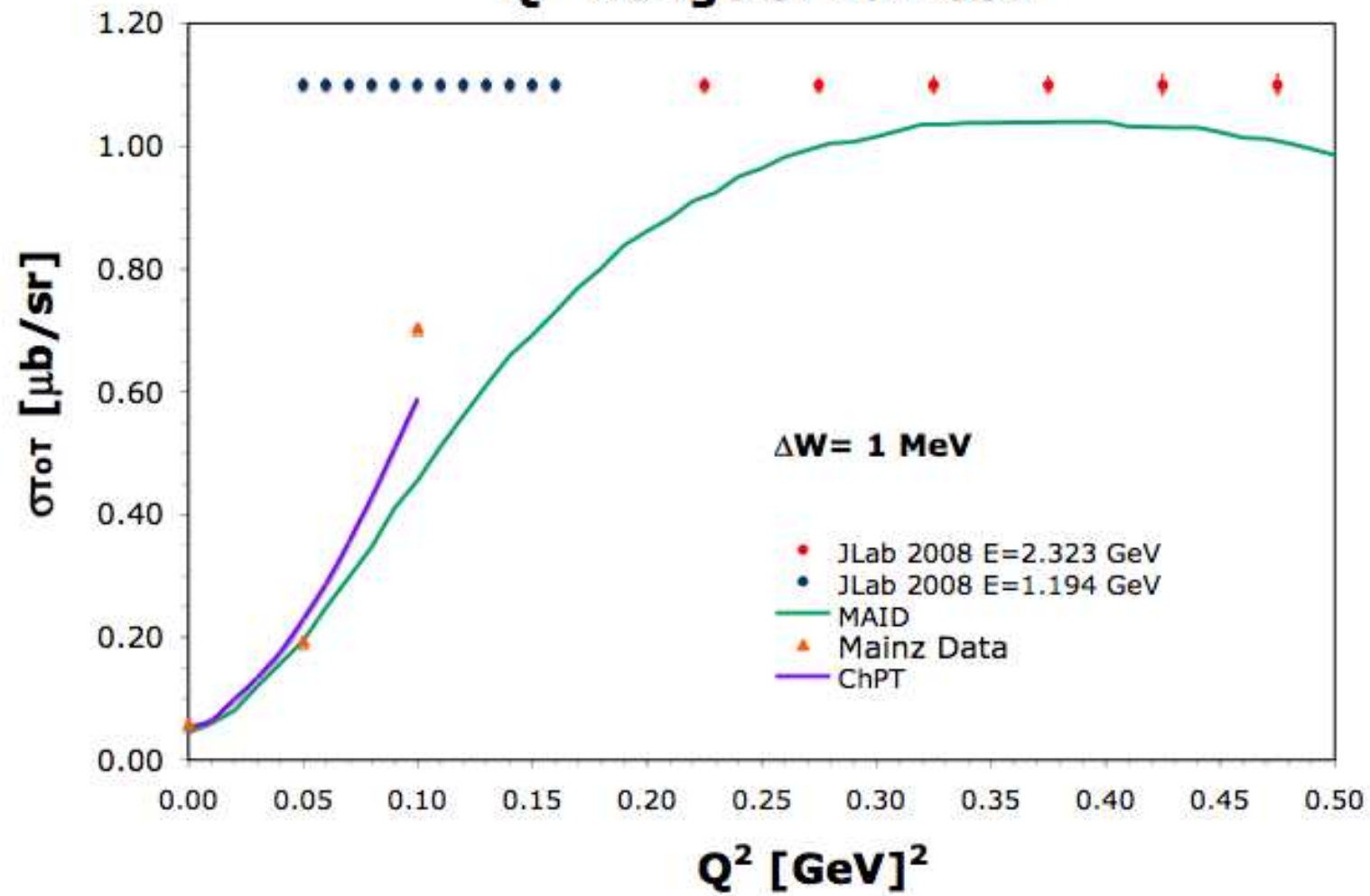
0.67 polarization, ave phi ~ 0.5

$Q^2 = 0.058 \text{ GeV}^2$

$E = 1.194 \text{ GeV}$



Q^2 Range of E04-007



Summary

The experiment is done
Data look good

Expect to finish analysis in 1 ½ year