

# Improving the thermoelectric properties of Half Heusler compounds

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# Outlines

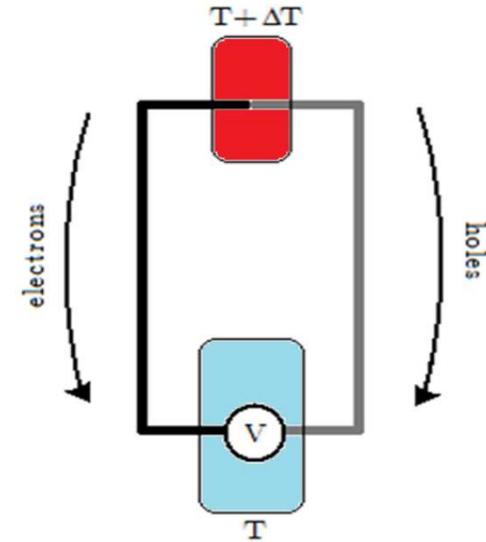
- Introduction of thermoelectrics and applications
- TE properties improvement via:
  - Seebeck coefficient
  - Thermal conductivity
- Bulk Half Heusler with nano-inclusions
- Nanostructured HH and Predictions

# Seebeck Effect

- Temperature gradient deducing Voltage gradient or vice visa

$$S = -\Delta V / \Delta T$$

- Thermal conductivity:  $\kappa$
- Dimensionless figure of Merit:  $ZT = S^2 T / \rho \kappa$
- Efficiency- the higher  $ZT$  is, the closer the efficiency of TE circuit getting to Carnot Engine.

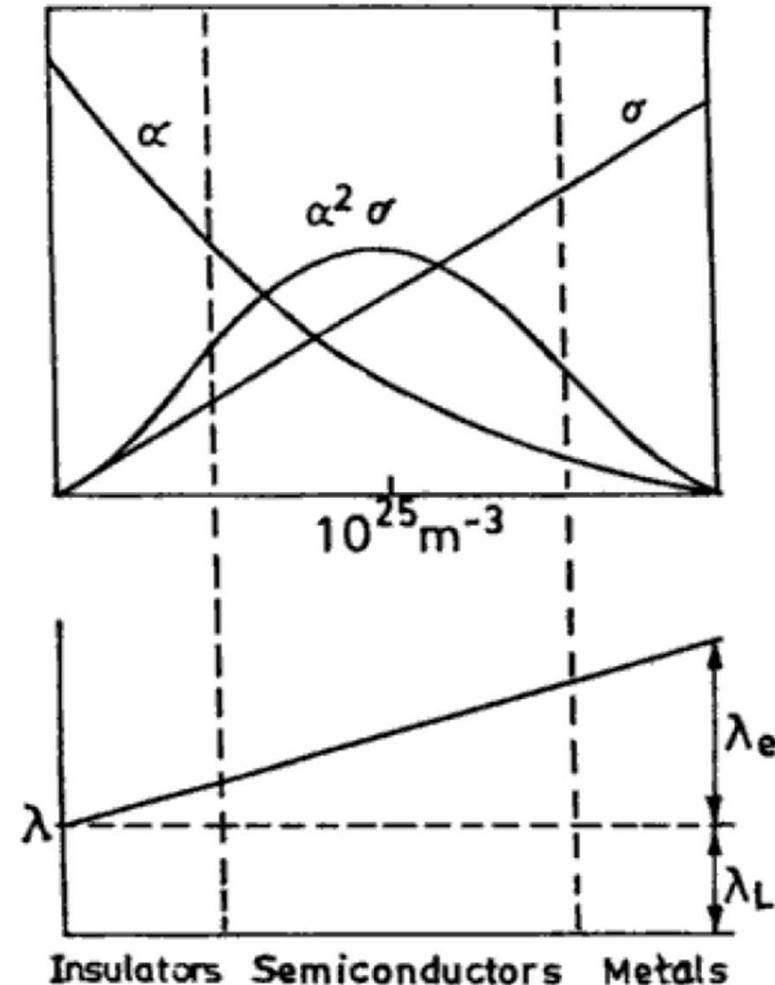


$$\eta = \frac{T_H - T_C}{T_H} \frac{\sqrt{1 + ZT} - 1}{\sqrt{1 + ZT} + \frac{T_C}{T_H}}$$

# Semiconductor is the best TE material

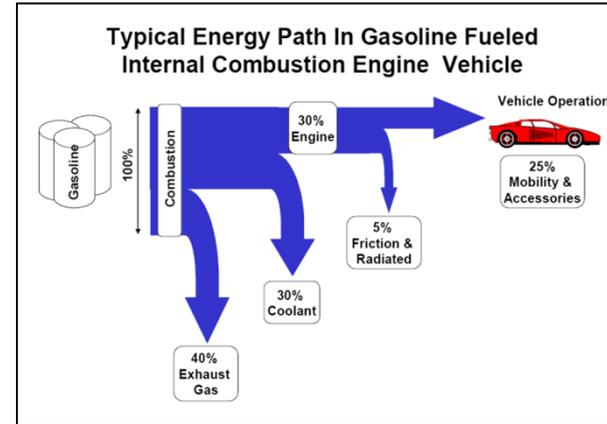
- $\alpha$  = Seebeck coefficient
- $\sigma$  = Electrical Conductivity
- $\lambda$  = Thermal Conductivity
  
- Power factor combined with thermal conductivity shows semiconductor is the best choice for TE materials

$$ZT = \alpha^2 \sigma T / \lambda$$

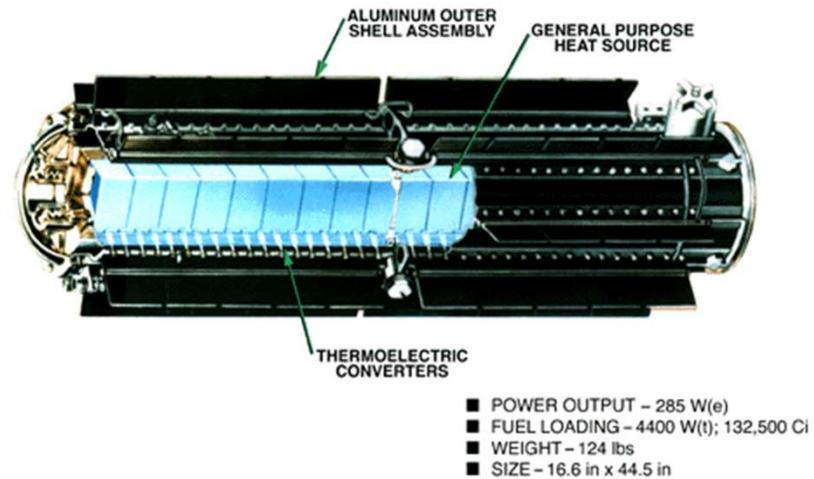


# Thermoelectrics Applications

Waste Heat Recovery

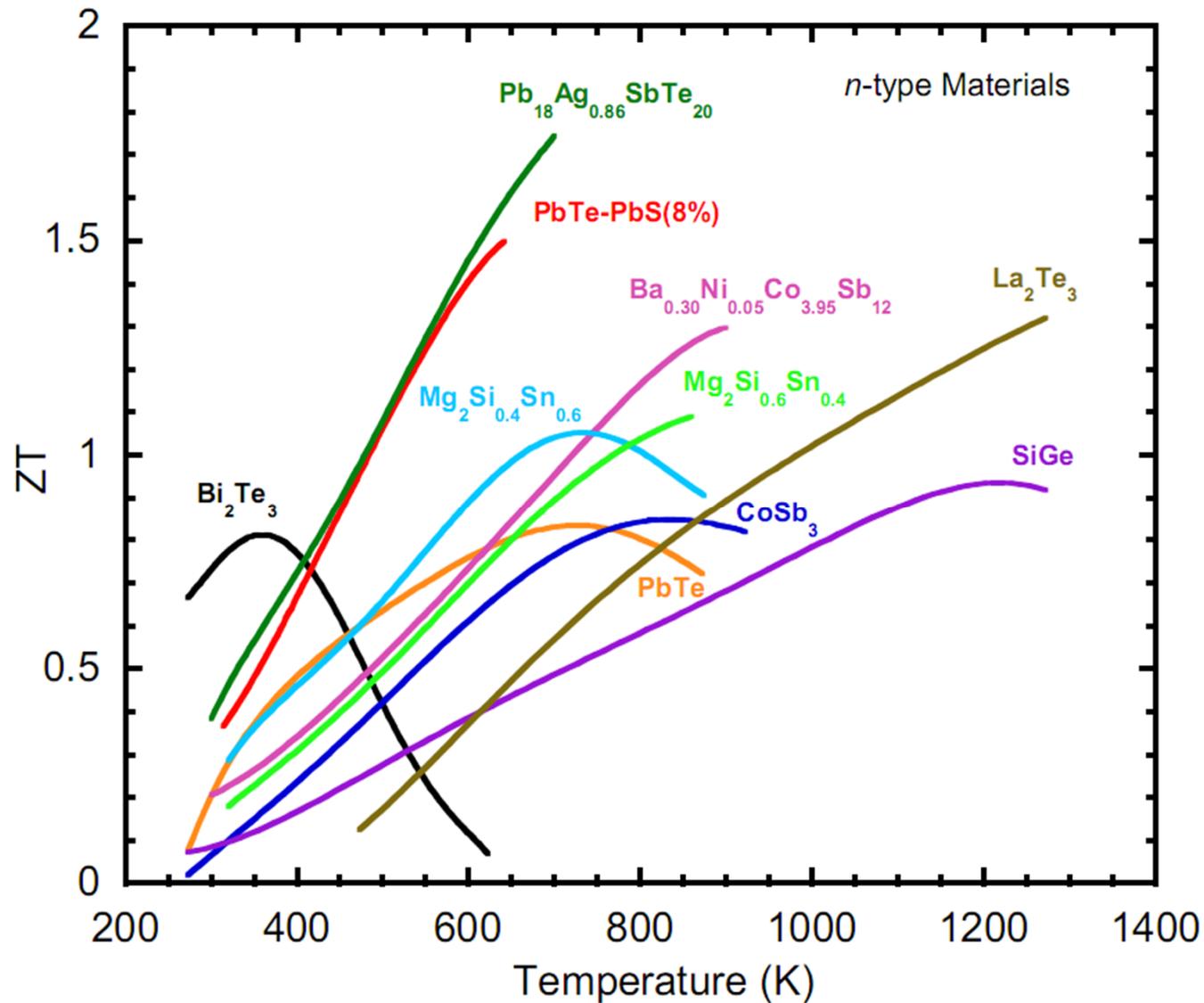


Thermoelectric Generator

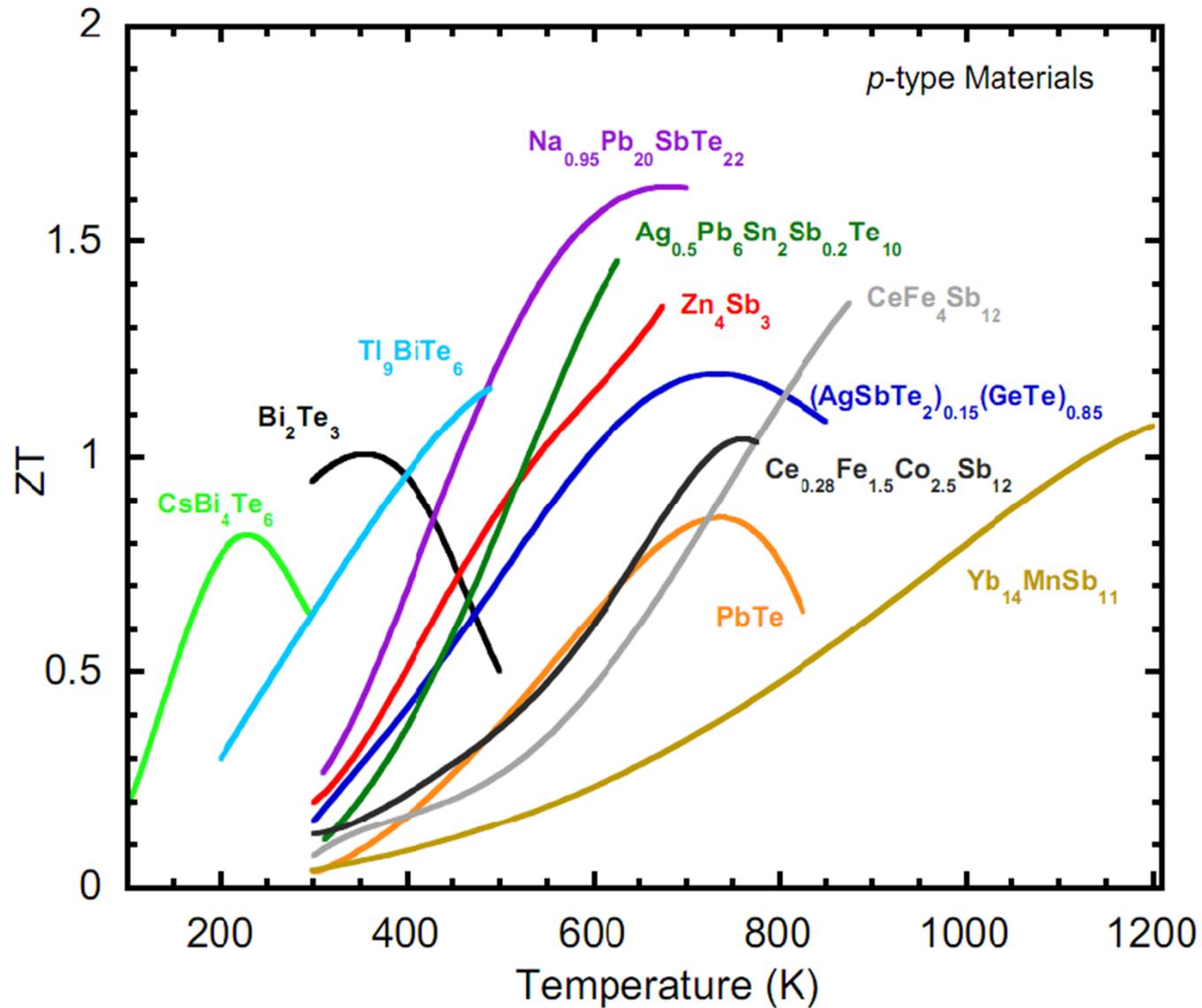


Thermoelectric Cooler

# State of the Art TE materials (n-type)

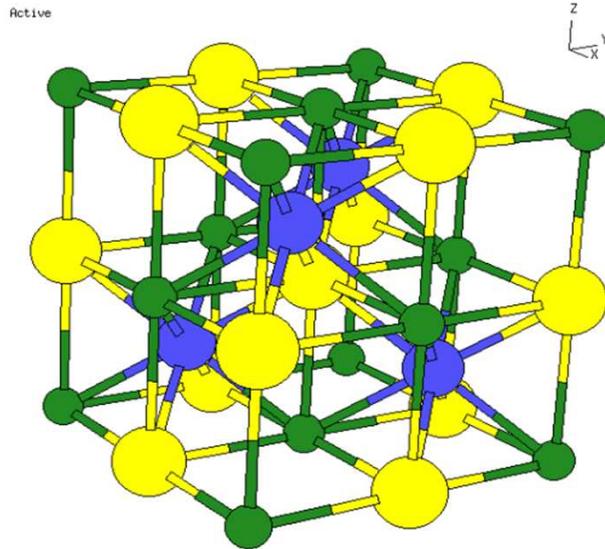


# State of the Art TE materials (p-type)



# Half Heusler alloys

Ti-Ni-Sn

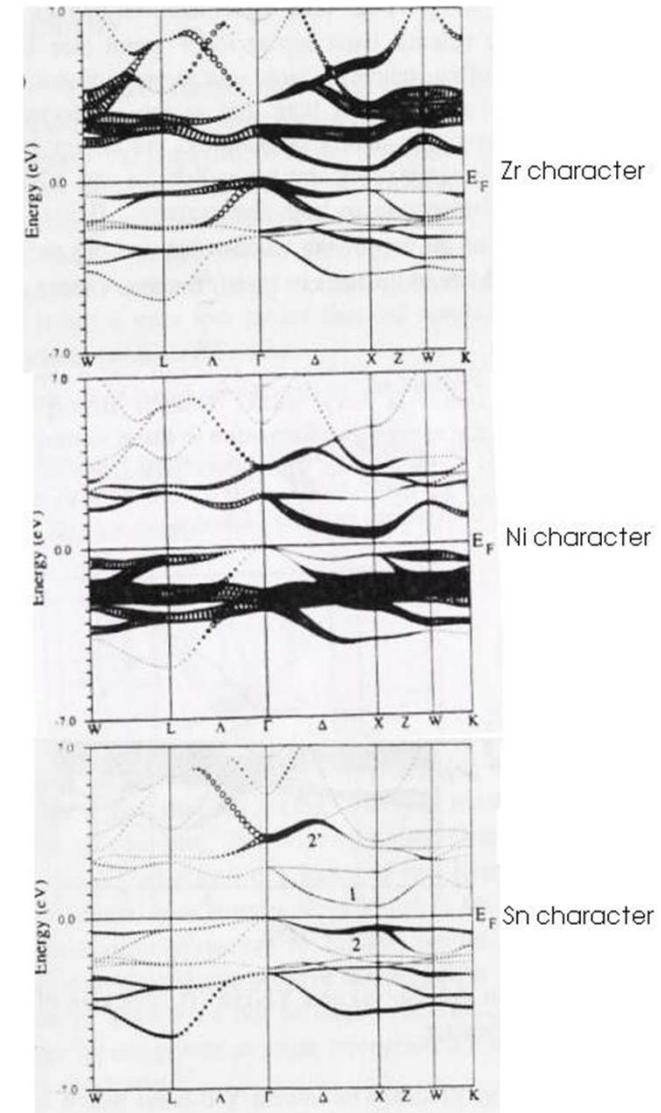


Ti and Sn atoms form a rock salt structure and Ni atoms fill half of the hollows at the center of Ti-Sn cubic.

Pros: Easy preparation, multiple doping options, non-toxic, high electrical conductivity

Cons: comparably high thermal conductivity

Band Structure of  $MNiSn$





# *How can we improve the properties of Thermoelectric materials*

$$ZT = \frac{S^2 T}{\rho \kappa} = \frac{S^2}{L_e + \frac{\kappa_L \rho}{T}}$$

$L_e$  – electrical Lorentz number

$\kappa_L$  – Lattice thermal conductivity

$\rho$  – electrical resistivity

$$K_e = L * \sigma * T$$

$\kappa_L$

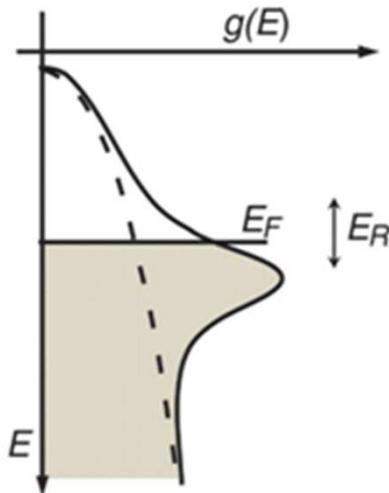


S



# *resonant states*

Mahan-Sofo Theory



Mott Expression

$$S = \frac{\pi^2}{3} \frac{k_B}{q} k_B T \left\{ \frac{d[\ln(\sigma(E))]}{dE} \right\}_{E=E_F}$$
$$= \frac{\pi^2}{3} \frac{k_B}{q} k_B T \left\{ \frac{1}{n} \frac{dn(E)}{dE} + \frac{1}{\mu} \frac{d\mu(E)}{dE} \right\}_{E=E_F}$$

$$n(E) = g(E) * f(E)$$

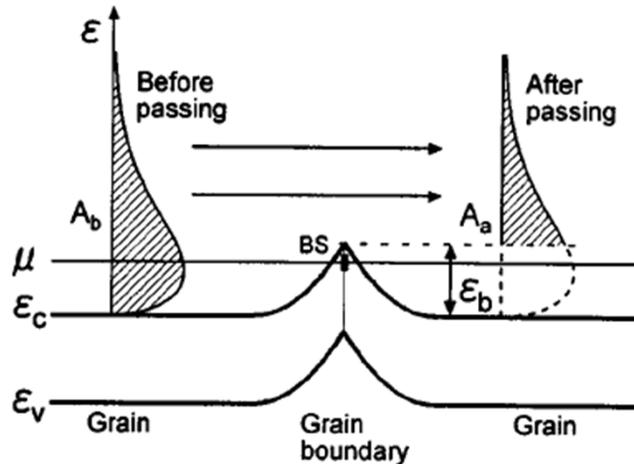
*Band Structure Engineering*

***Doping isovalent atoms with higher/lower electronegativity to resonate with corresponding conduction(n-type)/valence band edge of the majority component.***

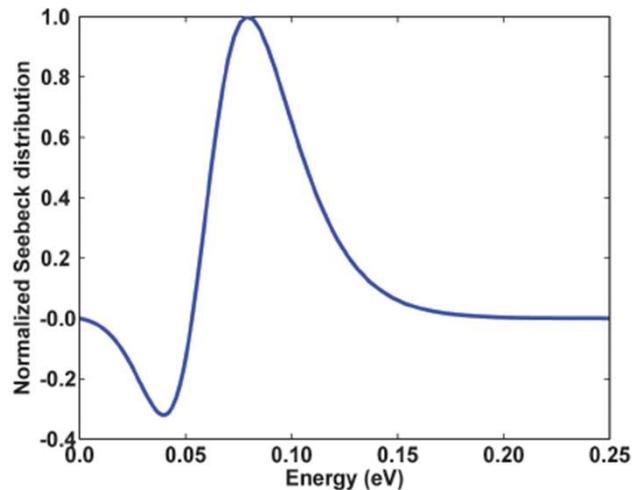
# Energy Filtering

Carriers →

(1)



Carriers which have lower energy than  $\epsilon_b$  are greatly scattered



(2)

Calculated normalized seebeck distribution vs electron energy for heavily doped bulk n-type  $\text{Si}_{80}\text{Ge}_{20}$  at RT. **Low energy electrons** contribute **negatively** to the Seebeck coefficient. This is also one of the motivation of our nano-inclusions bulk materials.

1) K.kishimoto, M.Tsukamoto, T. Koyanagi *Journal of Allplied Physics*, v92, n9, 2002

2)Minnich,A.J.;Dresselhaus, M.S.; Ren, Z.F.; Chen, G. *Energy and Environmental Science*, v 2, n 5, p 466-479, 2009

# *Thermal conductivity*

thermal conductivity

$$\kappa_T = \kappa_C + \kappa_e + \kappa_p$$

photon contribution  $\kappa_p$  negligible

electronic contribution  $\kappa_e$

## ***Wiedemann–Franz law***

$\kappa_e = L * \sigma * T$ , where L is Lorentz number  $L=2.44*10^{-8} \text{ W}*\Omega*\text{K}^{-2}$

Lattice contribution  $\kappa_C$  ***is exactly what we are working on.....***

# *Lattice TC model*

*Callaway's Lattice TC  
relaxation time*

*where :*

*Impurity scattering*

*Umklapp scattering*

*Boundary scattering*

$$\kappa_C = \frac{k_B}{2\pi^2 v} \left( \frac{k_B T}{\hbar} \right)^3 \int_0^{\theta/T} \tau_C(x, T) \frac{x^4 e^x}{(e^x - 1)^2} dx$$

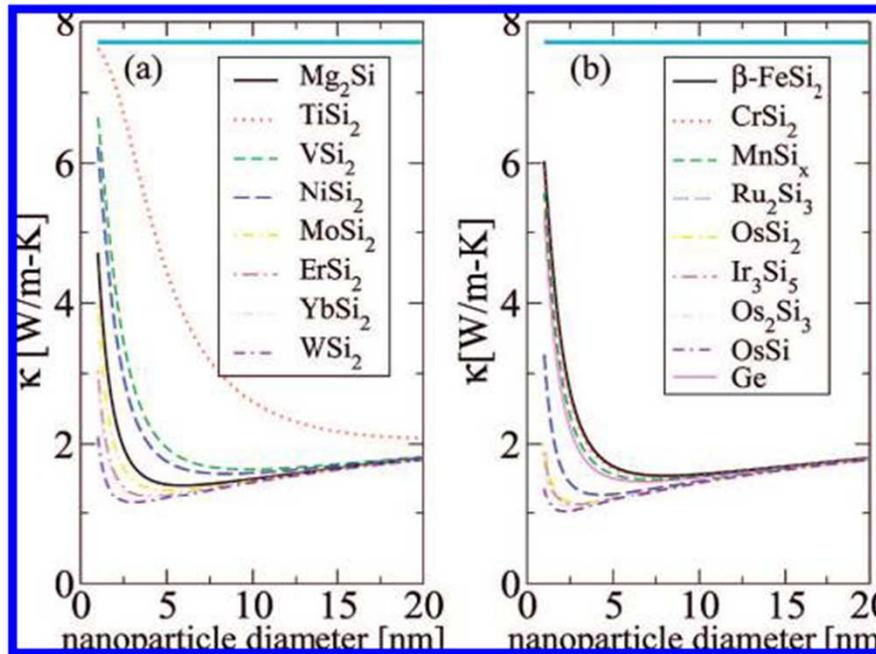
$$\tau_C^{-1} = \tau_I^{-1} + \tau_U^{-1} + \tau_B^{-1}$$

$$x = \hbar\omega / k_B T$$

$$\tau_I^{-1} = A\omega^4$$

$$\tau_U^{-1} = B_U T^3 \omega^2$$

$$\tau_B^{-1} = v/L$$



Mingo developed the grain boundary term to deal with bulk materials involving nanoparticles

$$\tau_{np}^{-1} = \nu(\sigma_s^{-1} + \sigma_l^{-1})^{-1} \rho$$

Short wavelength

$$\sigma_s = 2\pi R^2$$

Long wavelength

$$\sigma_l = \pi R^2 \frac{4}{9} (\Delta D/D)^2 (\omega R/\nu)^4$$

$\rho$  is the volume density of the nano-inclusions

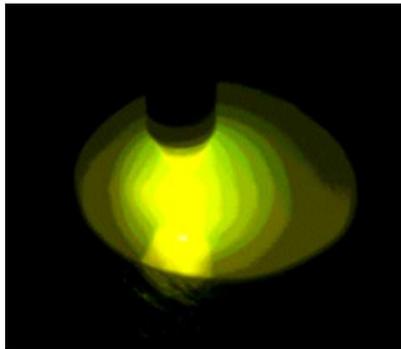
This is TC of various silicide nanoparticles (0.8% volume fraction) into  $\text{Si}_{50}\text{Ge}_{50}$  main matrix at  $T=300\text{K}$ :

- 1) TC decrease greatly even with small fraction of nano-inclusions.
- 2) It is not necessary to make accurate nanoparticle size control

# *Preparing bulk HH with nano-inclusions*

2% ZrO<sub>2</sub> nanoparticles dispersed Hf<sub>0.3</sub>Zr<sub>0.7</sub>CoSn<sub>0.3</sub>Sb<sub>0.7</sub>

Arc Melting



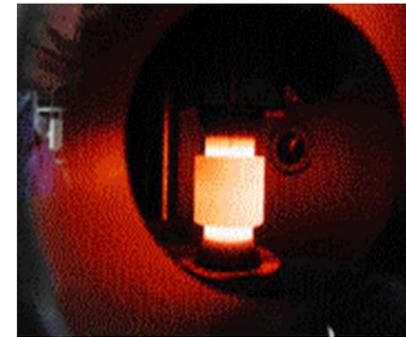
Main Matrix preparation

Ball milling/mixing



ZrO<sub>2</sub> nanoparticles involving

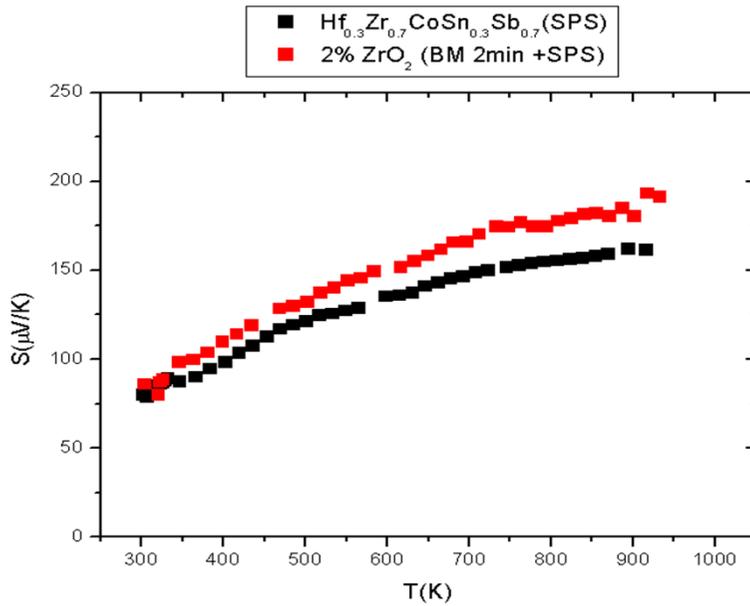
SPS (Spark Plasma Sintering)



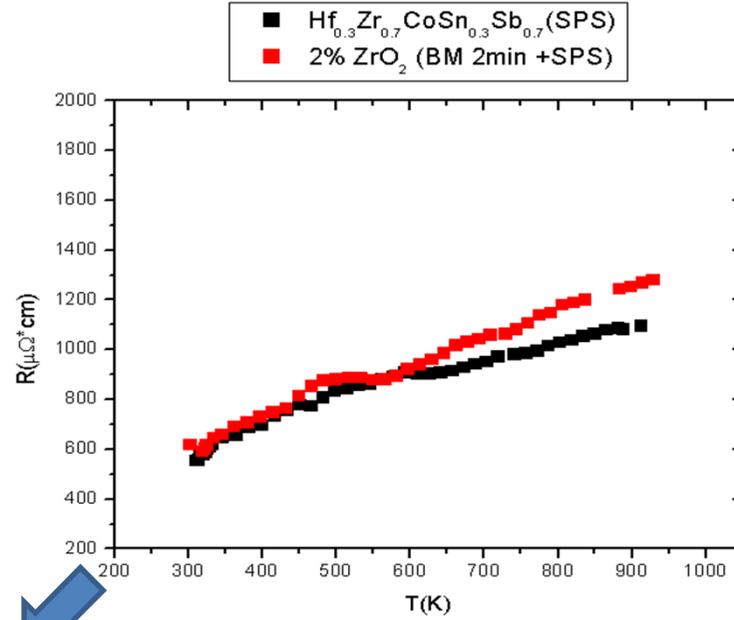
Clemson University, SC



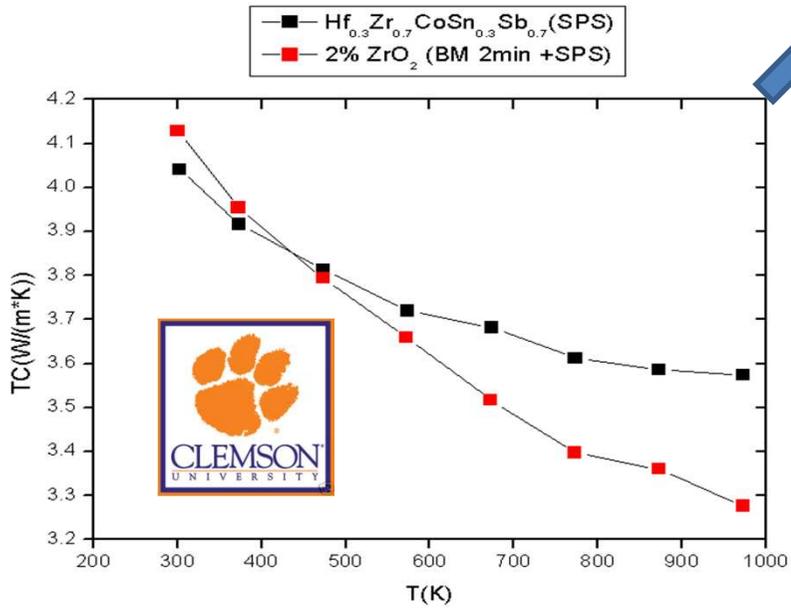
### Seebeck



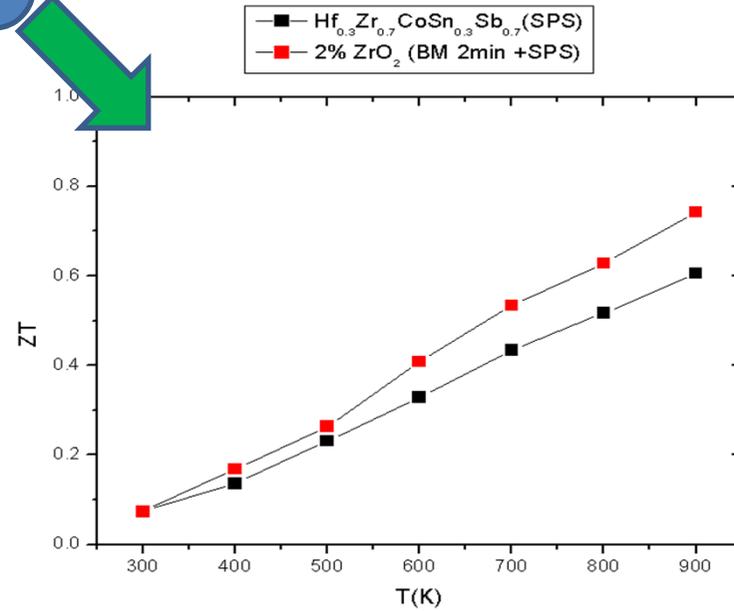
### Electrical Resistivity



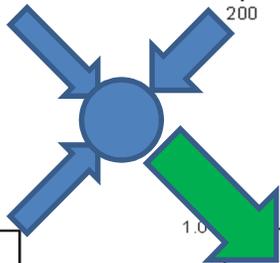
### Thermal Conductivity



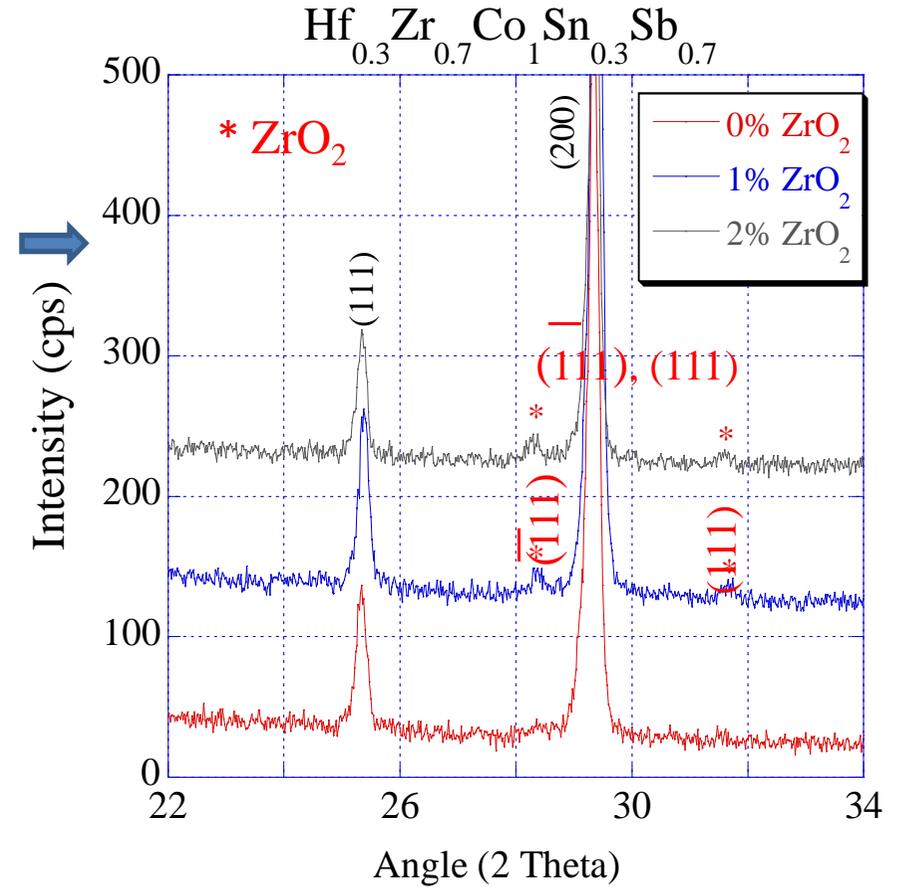
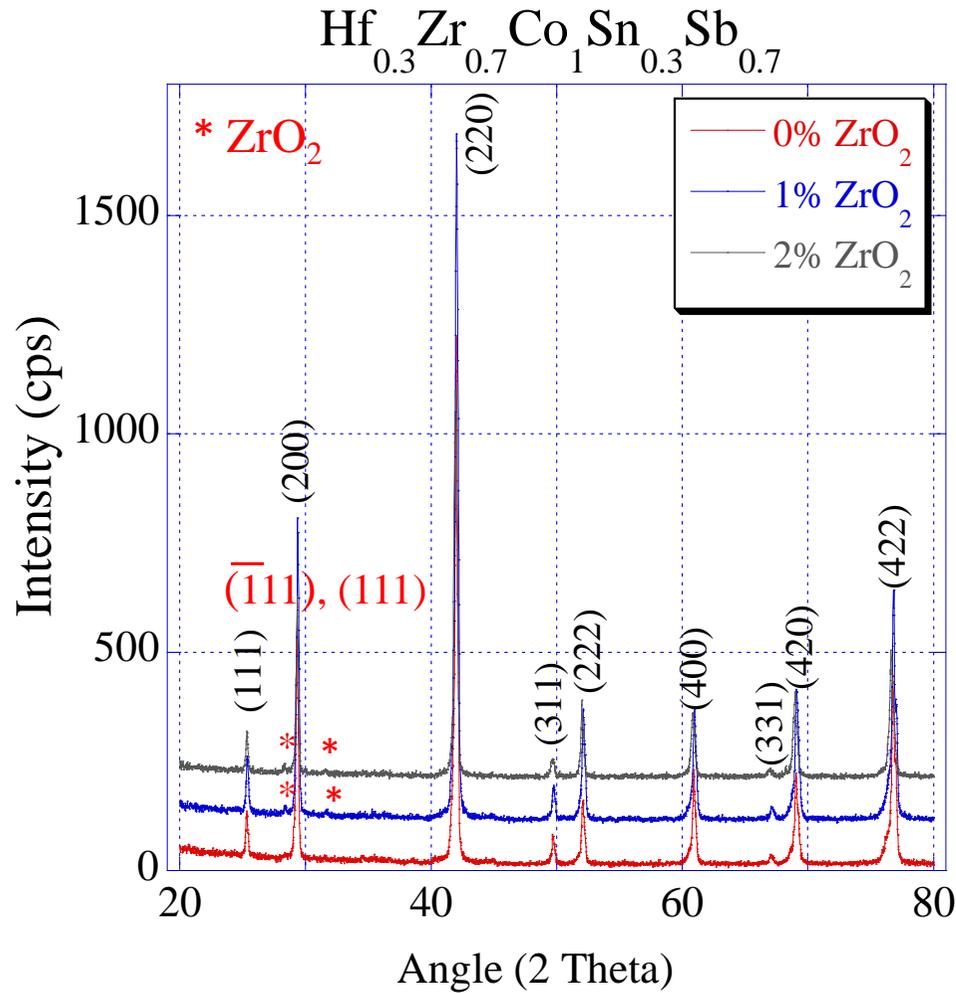
### ZT



25%



# X-Ray Pattern as proof of existence of ZrO<sub>2</sub>



# ***SEM and TEM in process....***

## ***SEM and EDS***

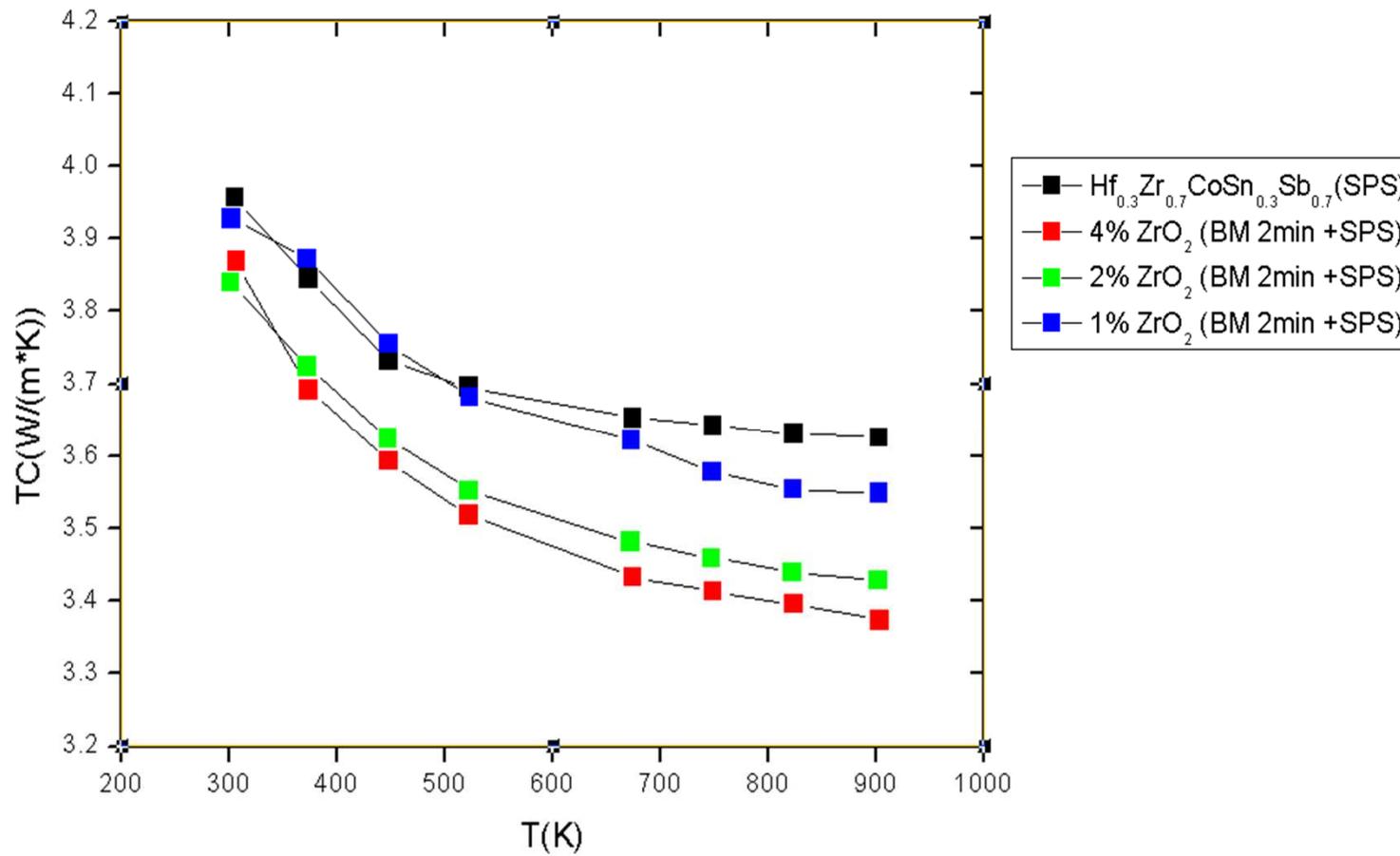
*SEM* is used to determine the grain size of the main matrix as well as existence of ZrO<sub>2</sub> nano-inclusions.

*EDS* is used to determine HH compound's uniform distribution as well as rough chemical composition.

## ***SEM***

Providing accurate proof for nano-inclusions existence as well as information of their grain size and position in main matrix

*Higher nanoparticles dispersion level will further decrease TC*



## ***Nano-structure instead of nano-inclusions?***

***How about ball milling the main matrix over hours?***

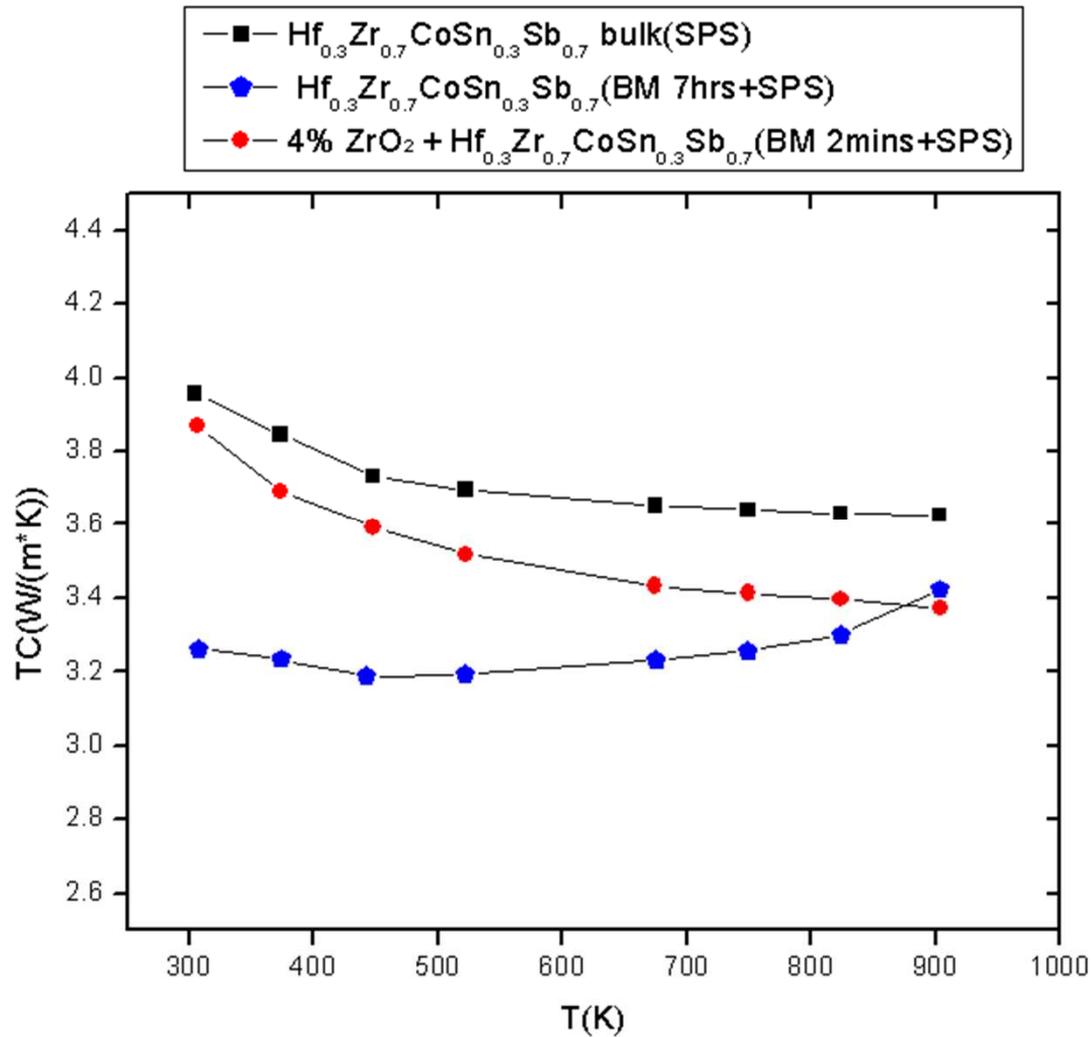
***grinding the main matrix to nano-scale?***

	<b>Main matrix grains</b>	<b>Inclusion grains</b>	<b>Ball milling time</b>
Nano-inclusions	Micron scale	Nano scale	<5 mins
Nano-structure	Nano scale	Nano scale	hours

***Investigation in process.....***

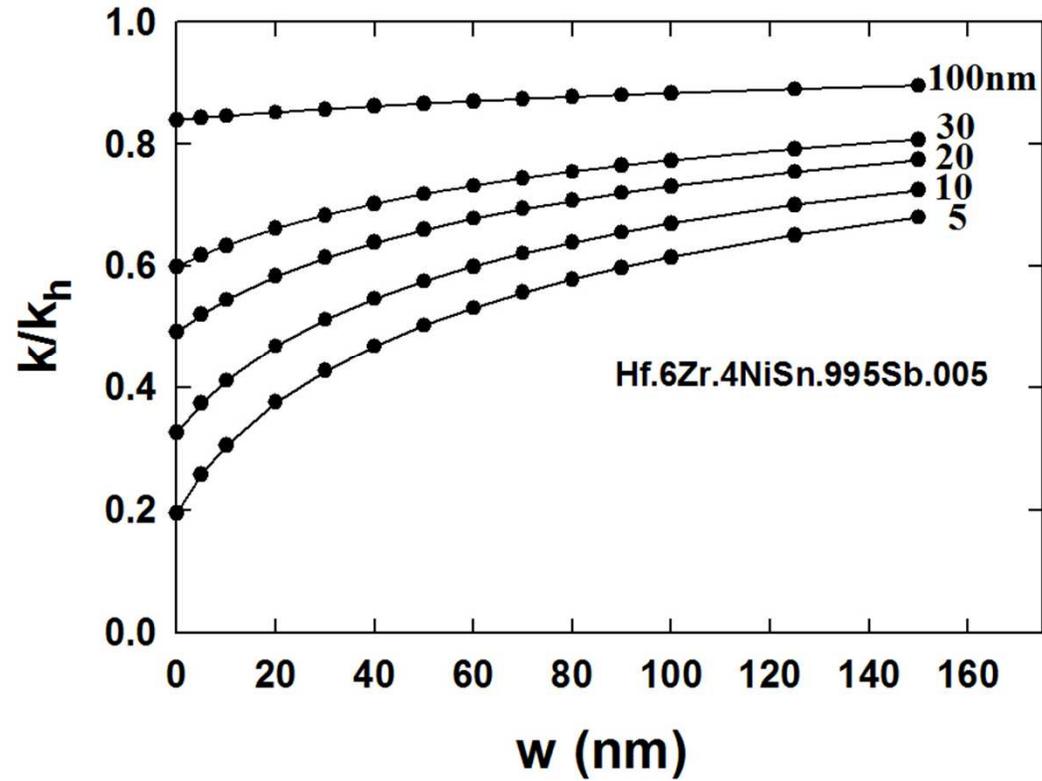
***1) Prevent oxidization while ball milling***

***2) Prevent contamination from the vial itself***



Further decreasing in thermal conductivity shows nano-structure bulk more promising than nano-inclusions bulk.

*Further predictions.....*



$k/k_h$  - Lattice TC of nano-structured Half Heusler alloy normalized to the reference regular bulk alloy  
 $w$  - the size range of the particles

*What ZT can we expect from this theoretical model?*

$$ZT = \frac{S^2 T}{\rho \kappa} = \frac{S^2}{L e + \frac{\kappa L \rho}{T}}$$

For N-type HH  $\text{Hf}_{0.6}\text{Zr}_{0.4}\text{NiSn}_{0.995}\text{Sb}_{0.005}$  at 900K

Grain size	Lattice TC	ZT
20 to 100 $\mu\text{m}$ (bulk)	1.10	0.91
100 to 200 nm	0.99	0.93
20 to 60 nm	0.704	0.99
5 to 25 nm	0.418	1.07

# *Acknowledgement*

- *Many thanks to Dr. Poon for his work on lattice TC prediction for nanostructured Half Heusler*
- *Appreciate the help of Thermal conductivity measurement and SPS from Clemson University*

*Thanks for your attendance!*