



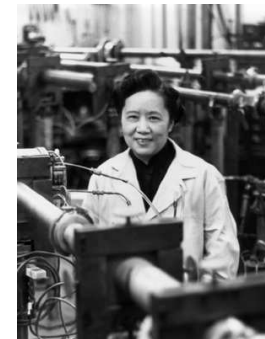
# **Measurement of CP Violation in $B_s \rightarrow J/\Psi\Phi$ Decay at CDF**

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## Introduction

- $CP$  violation means that the laws of nature are not invariant under the simultaneous transformation of Charge and Parity
- Charge conjugation transforms particles into anti-particles
- Parity transformation is a mirror reflection (space inversion)
- Parity conservation was first questioned by T.D. Lee and C.N. Yang in 1956 when they argued that there was no experimental evidence for parity conservation in weak interactions
- Same year, C.S. Wu showed that Parity is violated in beta decays of Cobalt nuclei
- The combined  $CP$  was soon adopted as the correct symmetry, just to be shown wrong by Cronin and Fitch in 1964 when they showed that  $CP$  is violated in neutral Kaon decays



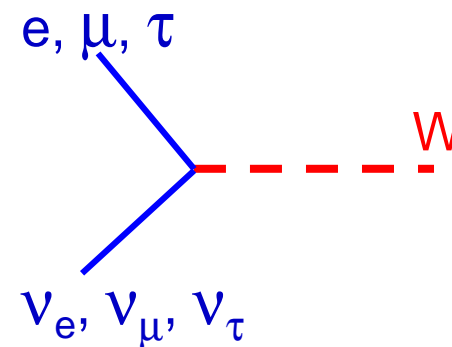
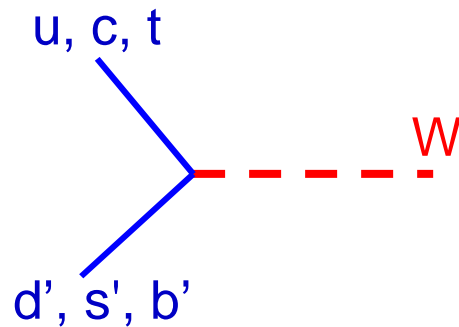
James Cronin



Val Fitch

## CP Violation in the Standard Model

- *CP* violation enters the Standard Model through complex phases in mixing matrices that connect up-type fermions with down-type fermions via *W* bosons:



$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

- Cabibbo-Kobayashi-Maskawa (CKM) quark mixing matrix transforms quark mass eigenstates into weak eigenstates and induces *CP* violation in the hadronic sector

- Pontecorvo-Maki-Nakagawa-Sakata (PMNS) neutrino mixing matrix  
→ induces neutrino oscillations and possibly *CP* violation in lepton sector

$$\begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{bmatrix}$$

## CKM Matrix

- Expand CKM matrix in  $\lambda = V_{us} = \sin(\theta_{Cabibbo}) \approx 0.23$

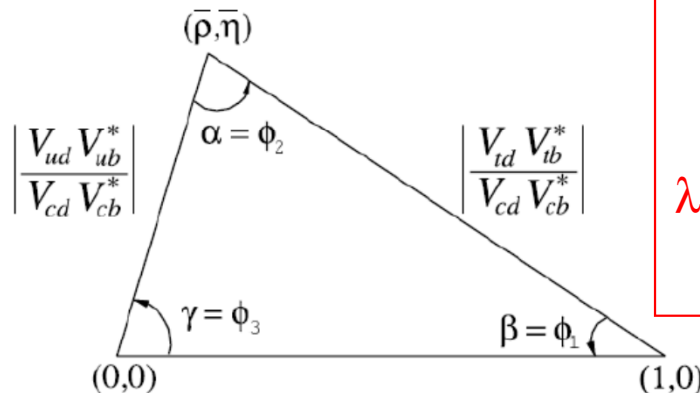
$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \approx \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda + \frac{1}{2}A^2\lambda^5[1 - 2(\rho + i\eta)] & 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4(1 + 4A^2) & A\lambda^2 \\ A\lambda^3[1 - (1 - \frac{1}{2}\lambda^2)(\rho + i\eta)] & -A\lambda^2 + \frac{1}{2}A\lambda^4[1 - 2(\rho + i\eta)] & 1 - \frac{1}{2}A^2\lambda^4 \end{pmatrix}$$

- To conserve probability CKM matrix must be unitary  
→ Unitary relations can be represented as “unitarity triangles”

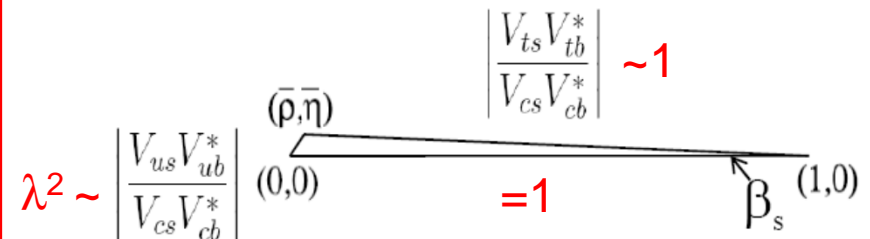
unitarity relations:

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

unitarity triangles:



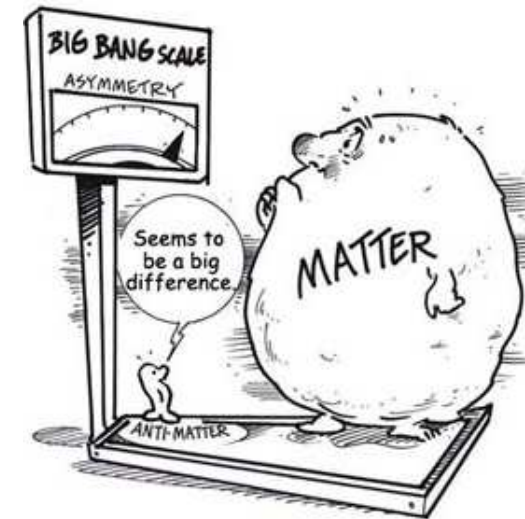
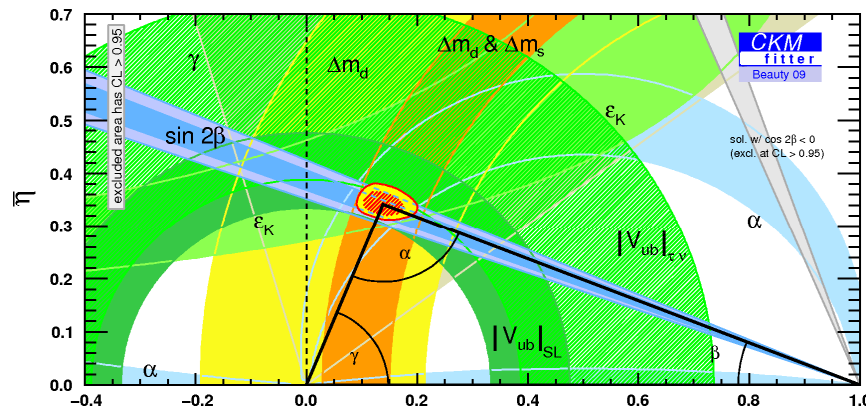
$$V_{us}V_{ub}^* + V_{cs}V_{cb}^* + V_{ts}V_{tb}^* = 0$$



Small  $CP$  violation phase  $\beta_s$  accessible in  $B_s \rightarrow J/\psi \Phi$  decays

## Why Look for $CP$ in $B_s$ System ?

- $CP$  violation has been studied in various Kaon and  $B$ -meson decays
- CKM matrix is well constrained by experimental data



- Within the SM framework,  $CP$  violation in the quark sector is too small to explain the matter - antimatter asymmetry in the universe
- Could find additional  $CP$  violation within the SM in the lepton sector
  - initial asymmetry between leptons and anti-leptons may induce baryon asymmetry through baryon number violation processes (lepto-genesis)
  - long baseline neutrino experiments will investigate  $CP$  violation in neutrino sector
- Alternatively we look for sources of  $CP$  violation beyond the SM in the quark sector
- Promising place to look for non-SM  $CP$  violation is the neutral  $B_s$  meson system

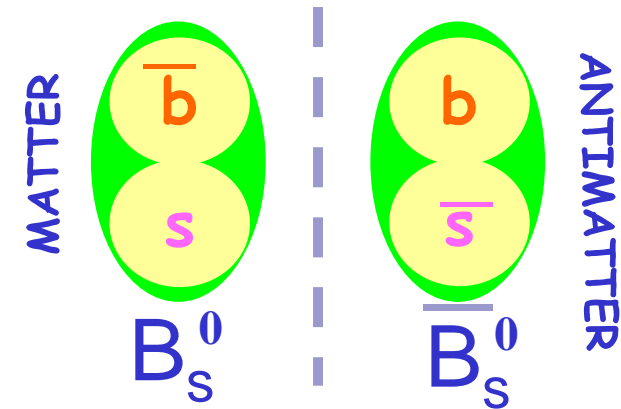
## Neutral $B_s$ System

- Time evolution of  $B_s$  flavor eigenstates described by Schrodinger equation:

$$i \frac{d}{dt} \begin{pmatrix} |B_s^0(t)\rangle \\ |\bar{B}_s^0(t)\rangle \end{pmatrix} = \left( \mathbf{M} - \frac{i}{2} \mathbf{\Gamma} \right) \begin{pmatrix} |B_s^0(t)\rangle \\ |\bar{B}_s^0(t)\rangle \end{pmatrix}$$

- Diagonalize mass ( $M$ ) and decay ( $\Gamma$ ) matrices  
→ mass eigenstates :

$$|B_s^H\rangle = p |B_s^0\rangle - q |\bar{B}_s^0\rangle \quad |B_s^L\rangle = p |B_s^0\rangle + q |\bar{B}_s^0\rangle$$



- Flavor eigenstates differ from mass eigenstates and mass eigenvalues are also different:

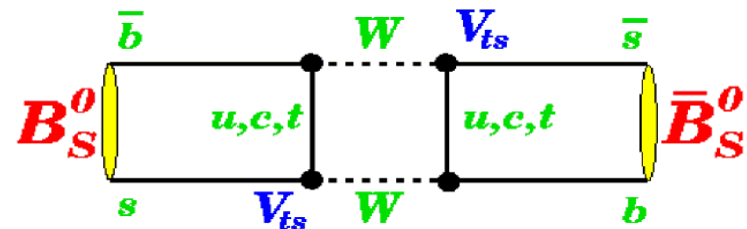
$$\Delta m_s = m_H - m_L \approx 2|M_{12}|$$

→  $B_s$  oscillates with frequency  $\Delta m_s$

precisely measured by

$$\text{CDF} \quad \Delta m_s = 17.77 \pm 0.12 \text{ ps}^{-1}$$

$$\text{DØ} \quad \Delta m_s = 18.56 \pm 0.87 \text{ ps}^{-1}$$

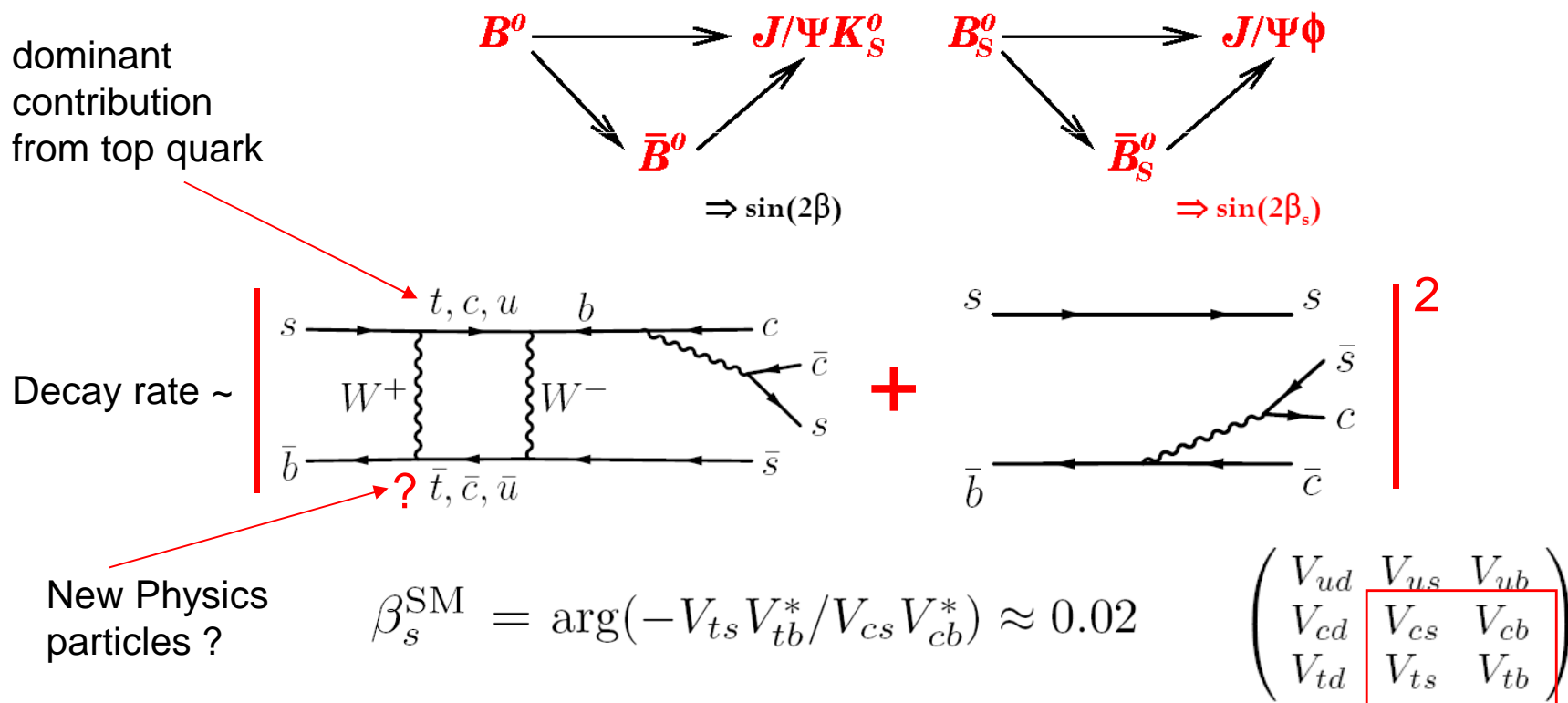


- Mass eigenstates have different decay widths

$$\Delta\Gamma = \Gamma_L - \Gamma_H \approx 2|\Gamma_{12}| \cos(\Phi_s) \quad \text{where} \quad \phi_s^{\text{SM}} = \arg\left(-\frac{M_{12}}{\Gamma_{12}}\right) \approx 4 \times 10^{-3}$$

## CP Violation in $B_s \rightarrow J/\Psi \Phi$ Decays

- Analogously to the neutral  $B^0$  system, CP violation in  $B_s$  system is accessible through interference of decays with and without mixing:

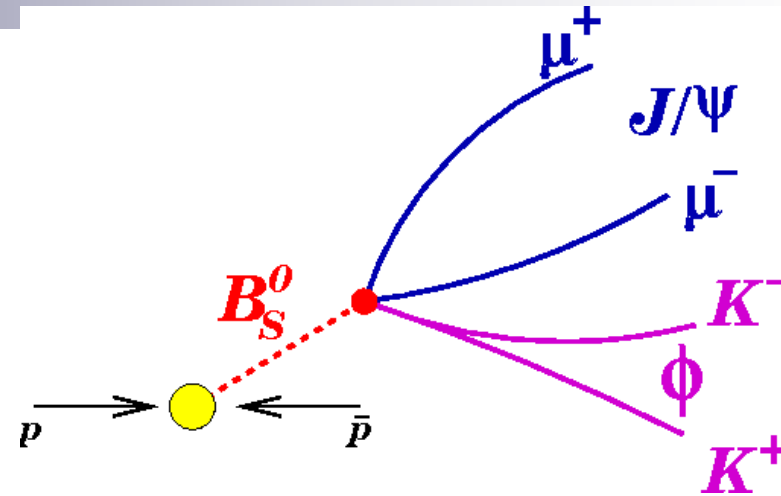


- CP violation phase  $\beta_s$  in SM is predicted to be very small,  $O(\lambda^2)$
- New physics particles running in the mixing diagram may enhance  $\beta_s$ 
  - large  $\beta_s \rightarrow$  clear indication of New Physics !

## $B_s \rightarrow J/\psi \phi$ Decays

- Measure:

- $B_s$  lifetime  $\tau_s$
- $B_{sH}, B_{sL}$  decay width difference  $\Delta\Gamma_s$
- $CP$  violating phase  $\beta_s$

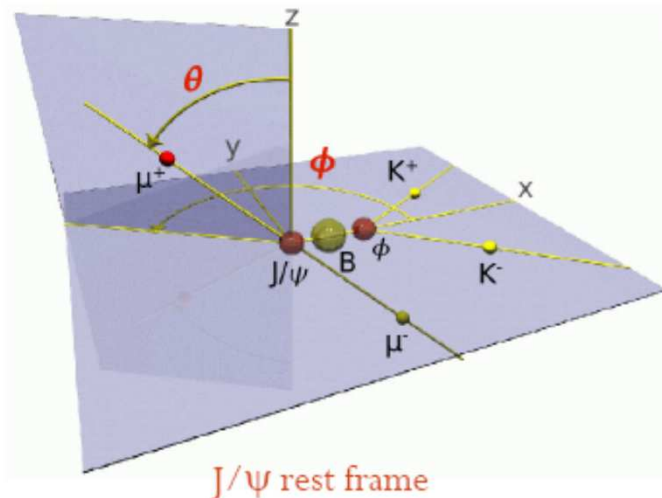


- Decay of  $B_s$  (spin 0) to  $J/\psi$  (spin 1) and  $\phi$  (spin 1) leads to three different angular momentum final states:

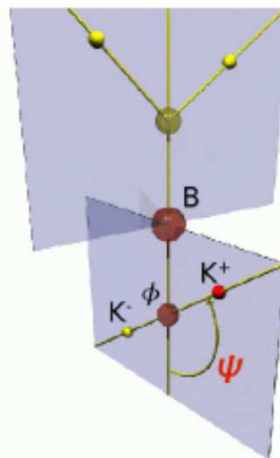
$L = 0$  (s-wave), 2 (d-wave)  $\rightarrow CP$  even ( = short lived or light  $B_s$  if no  $CPV$  )

$L = 1$  (p-wave)

$\rightarrow CP$  odd ( = long lived or heavy  $B_s$  if no  $CPV$  )



$J/\psi$  rest frame



$\phi$  rest frame

- Three decay angles  $\vec{\rho} = (\theta, \phi, \psi)$  describe directions of final decay products  $\mu^+ \mu^- K^+ K^-$



## Transversity Basis

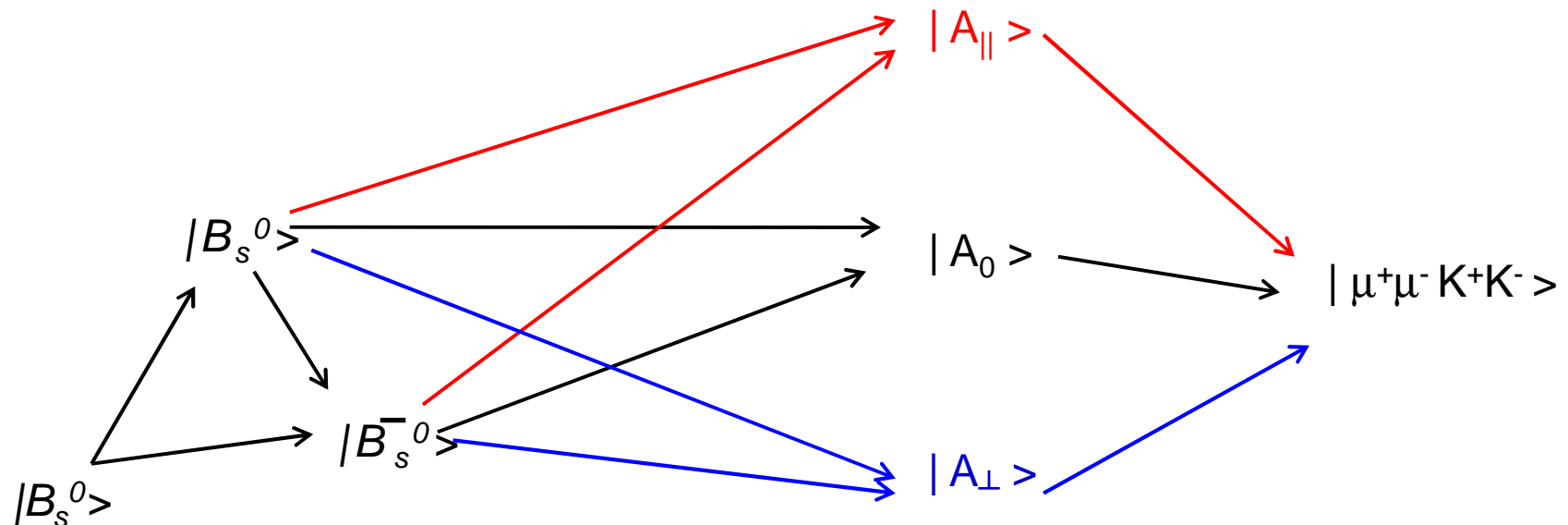
- Use “transversity basis” in which the vector meson polarizations w.r.t. direction of motion are either (Phys. Lett. B 369, 144 (1996), 184 hep-ph/9511363 ):

- transverse ( $\perp$  perpendicular to each other)  $\rightarrow CP$  odd

- transverse ( $\parallel$  parallel to each other)  $\rightarrow CP$  even

- longitudinal (0)  $\rightarrow CP$  even

- Corresponding decay amplitudes:  $A_0, A_{\parallel}, A_{\perp}$



# Decay Rate

-  $B_s \rightarrow J/\psi \phi$  decay rate as function of time, decay angles and initial  $B_s$  flavor:

$$\frac{d^4 P(t, \vec{\rho})}{dt d\vec{\rho}} \propto |A_0|^2 T_+ f_1(\vec{\rho}) + |A_{||}|^2 T_+ f_2(\vec{\rho})$$

$$+ |A_{\perp}|^2 T_- f_3(\vec{\rho}) + |A_{||}| |A_{\perp}| \mathcal{U}_+ f_4(\vec{\rho})$$

$$+ |A_0| |A_{||}| \cos(\delta_{||}) T_+ f_5(\vec{\rho})$$

$$+ |A_0| |A_{\perp}| \mathcal{V}_+ f_6(\vec{\rho}),$$

time dependence terms

angular dependence terms

terms with  $\beta_s$  dependence

$$T_{\pm} = e^{-\Gamma t} \times [\cosh(\Delta\Gamma t/2) \mp \cos(2\beta_s) \sinh(\Delta\Gamma t/2)$$

$$\mp \eta \sin(2\beta_s) \sin(\Delta m_s t)],$$

terms with  $\Delta m_s$  dependence present if initial state of B meson (B vs anti-B) is determined (flavor tagged)

$$\mathcal{U}_{\pm} = \pm e^{-\Gamma t} \times [\sin(\delta_{\perp} - \delta_{||}) \cos(\Delta m_s t)$$

$$- \cos(\delta_{\perp} - \delta_{||}) \cos(2\beta_s) \sin(\Delta m_s t)$$

$$\pm \cos(\delta_{\perp} - \delta_{||}) \sin(2\beta_s) \sinh(\Delta\Gamma t/2)]$$

$$\mathcal{V}_{\pm} = \pm e^{-\Gamma t} \times [\sin(\delta_{\perp}) \cos(\Delta m_s t)$$

$$- \cos(\delta_{\perp}) \cos(2\beta_s) \sin(\Delta m_s t)$$

$$\pm \cos(\delta_{\perp}) \sin(2\beta_s) \sinh(\Delta\Gamma t/2)].$$

'strong' phases:

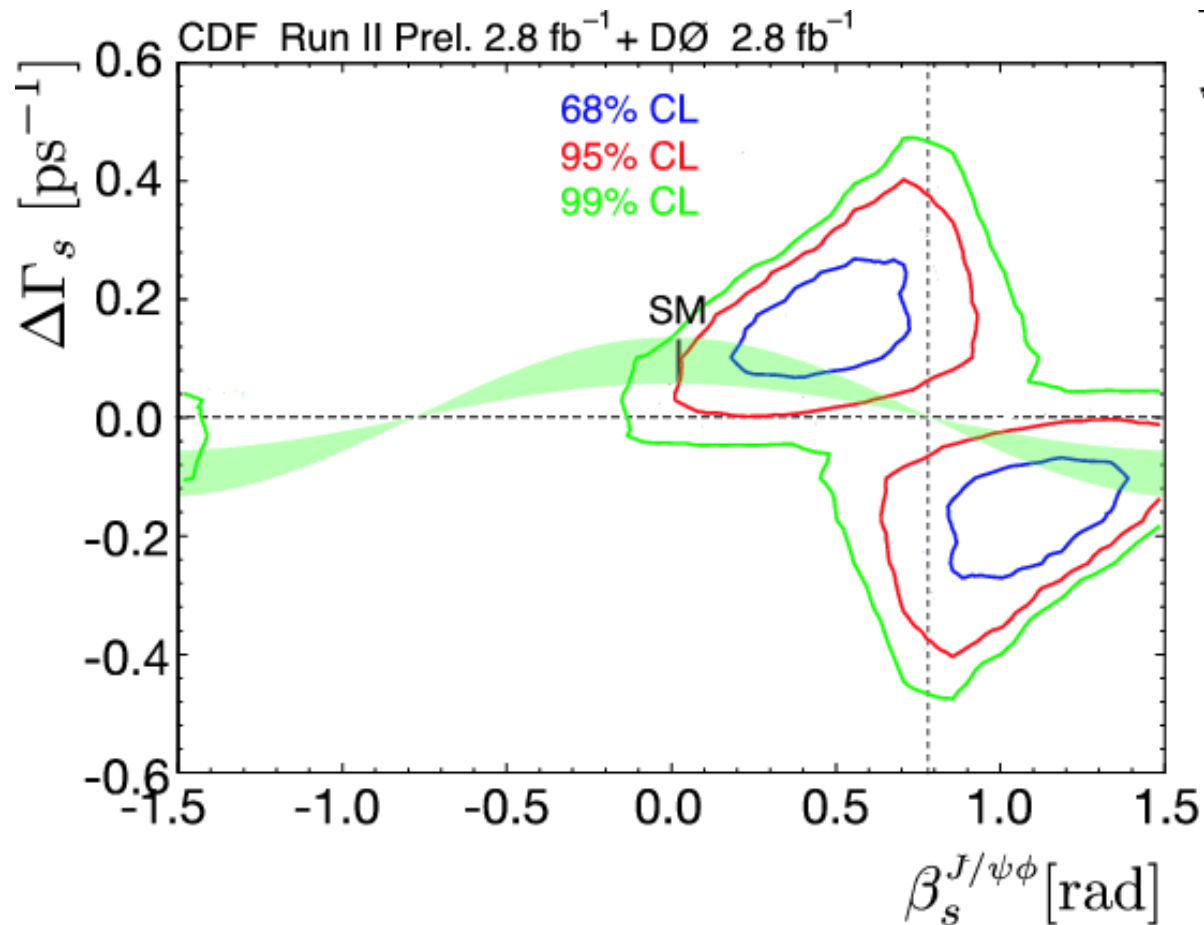
$$\delta_{||} \equiv \text{Arg}(A_{||}(0)A_0^*(0))$$

$$\delta_{\perp} \equiv \text{Arg}(A_{\perp}(0)A_0^*(0))$$

- Identification of  $B$  flavor at production (flavor tagging)  $\rightarrow$  better sensitivity to  $\beta_s$

## Some History

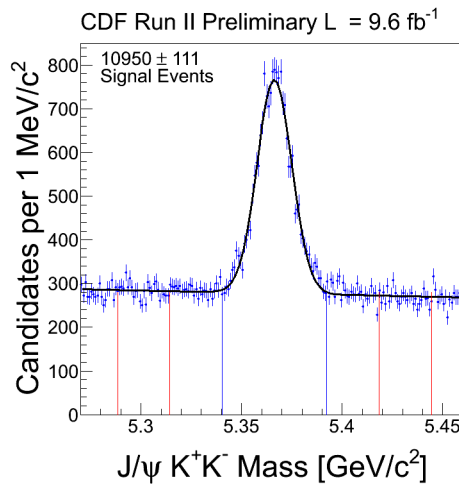
- Tagged analysis first performed by CDF in 2007 and soon followed by D0
- In 2009, CDF + DØ combination with 2.8/fb done by the Tevatron B Working Group ( <http://tevbwg.fnal.gov/> ) showed intriguing  $2.1\sigma$  deviation from SM expectation



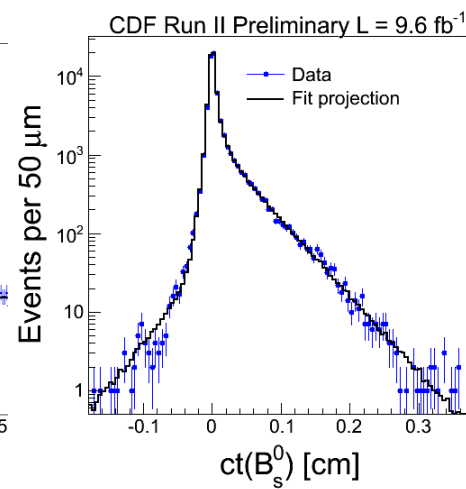
# Analysis Components

- Multi-dimensional likelihood fit

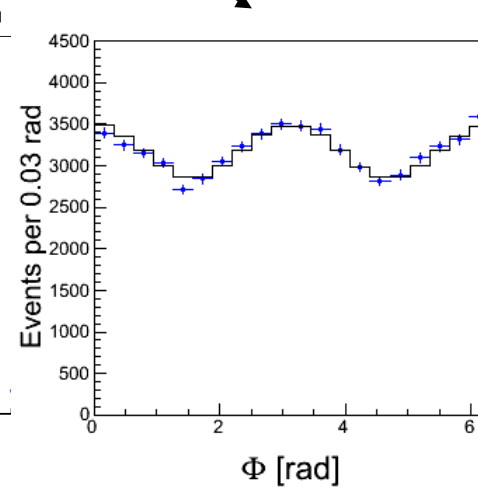
$$f_s P_s(m|\sigma_m) P_s(t, \vec{\rho}, \xi | \mathcal{D}, \sigma_t) P_s(\sigma_t) P_s(\mathcal{D})$$



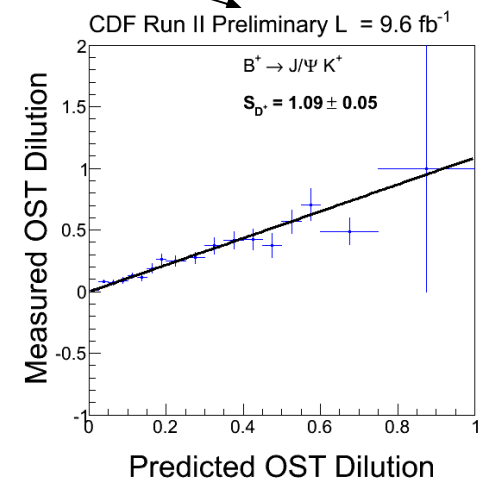
**Mass**  
discriminate signal  
against background



**Decay-time**  
determines lifetime  
of each mass  
eigenstate



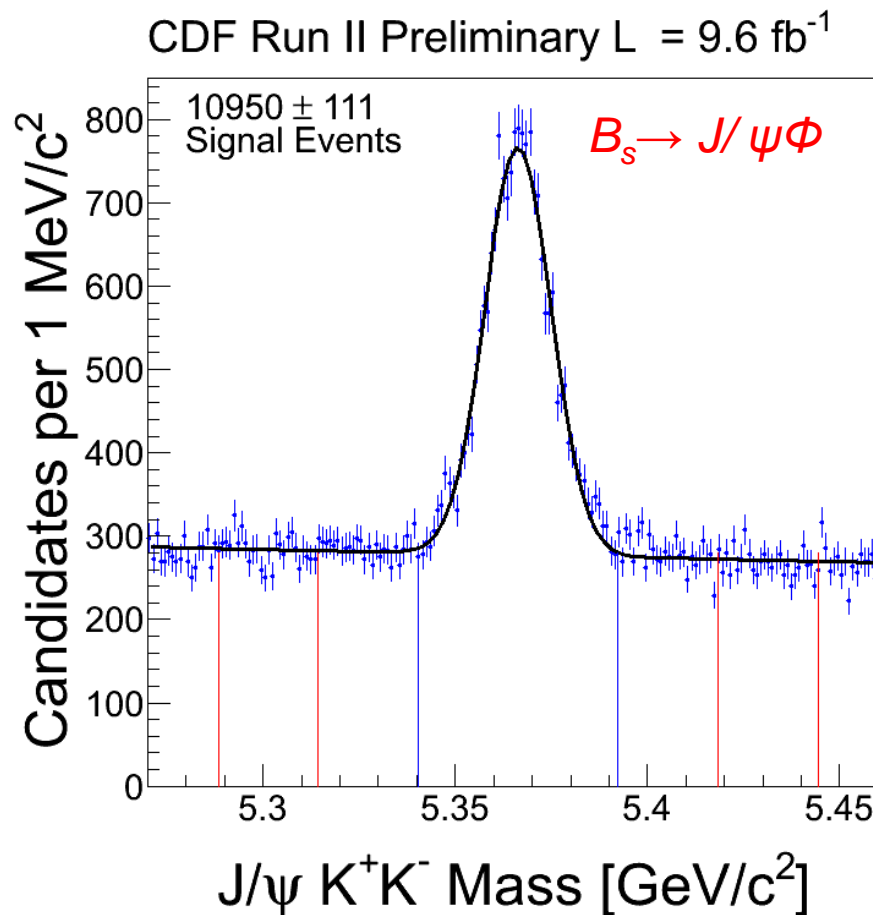
**Angles**  
separate CP-even  
from CP-odd final  
states



**Tagging**  
determines flavor  
of initial B<sub>s</sub> state

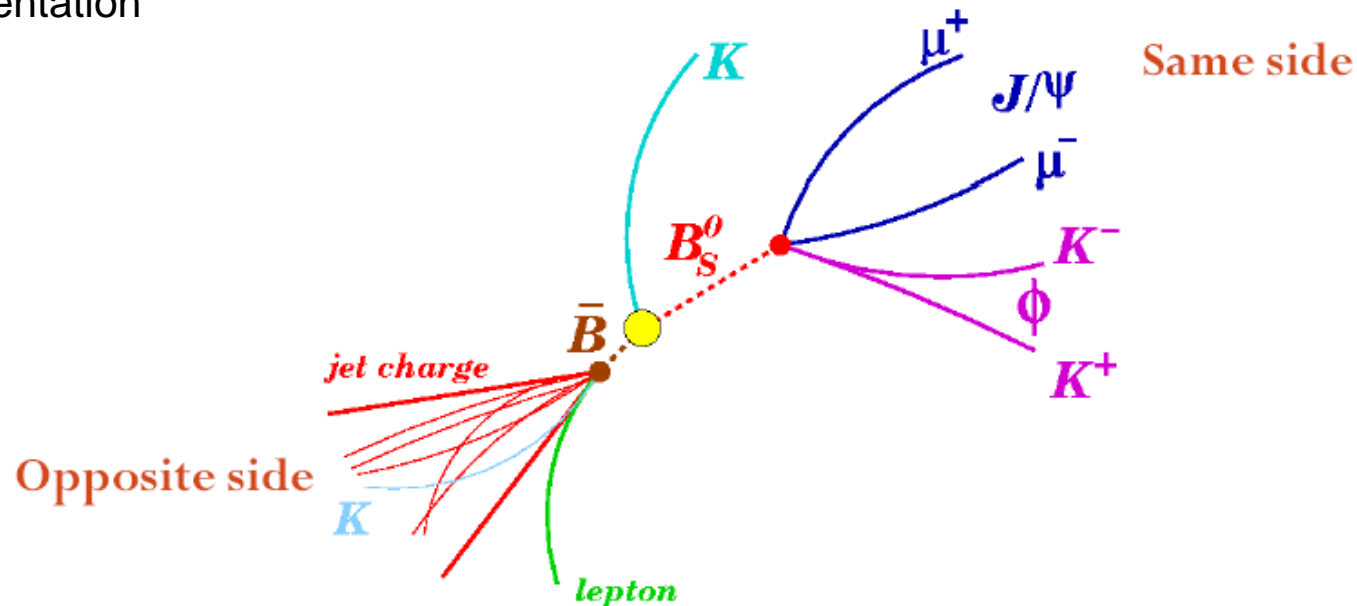
## Signal Reconstruction

- Reconstruct  $B_s^0 \rightarrow J/\psi \Phi$  in  $9.6 \text{ fb}^{-1}$  of data from sample selected by di-muon trigger
- Combine kinematic variables with particle ID information (dE/dx, TOF) in neural network to discriminate signal from background
- Yield of  $\sim 11000$   $B_s$  events with  $S/B \sim 1$



## Flavor Tagging

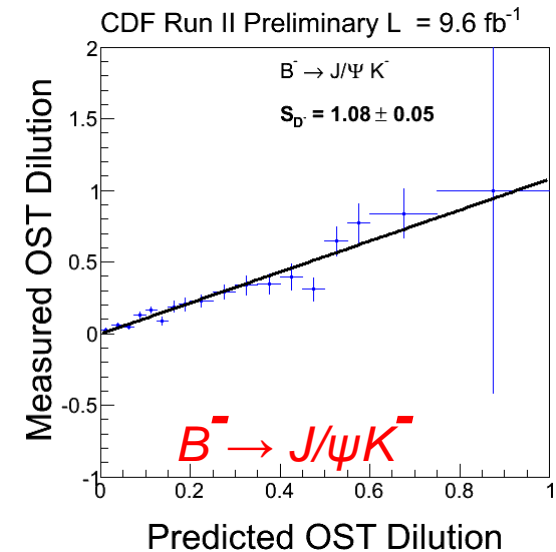
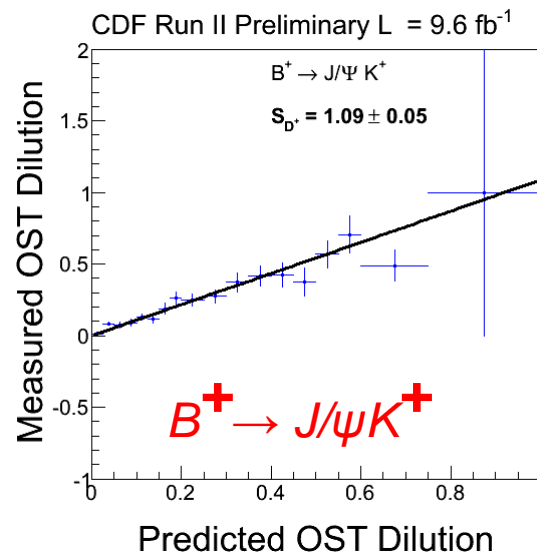
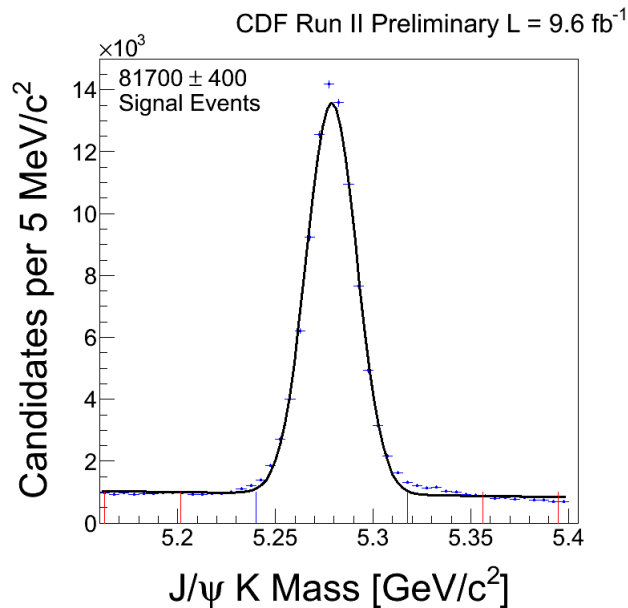
- Tevatron:  $b$ -quarks mainly produced in pairs of *bottom anti-bottom*  
→ flavor of the  $B$  meson at production inferred with:
- Opposite Side Tagger (OST): exploits decay products of other  $b$ -hadron in the event
- Same Side Kaon Tagger (SSKT): exploits correlations with particles produced in fragmentation



- Output of flavor tagger:
  - flavor decision ( $b$ -quark or anti- $b$ -quark)
  - probability that the decision is correct:  $P = (1 + \text{Dilution}) / 2$

# Opposite Side Tagging Calibration and Performance

- OST combines in a NN opposite side lepton and jet charge information
- Initially calibrated using a sample of inclusive semileptonic  $B$  decays
  - predicts tagging probability on event-by-event basis
- Re-calibrated using  $\approx 82,000$   $B^{+/-} \rightarrow J/\psi K^{+/-}$  decays



- OST efficiency = 93%, OST dilution = 11.5  $\pm$  0.2 % (correct tag probability  $\sim$ 56%)
- Total tagging power = 1.2%

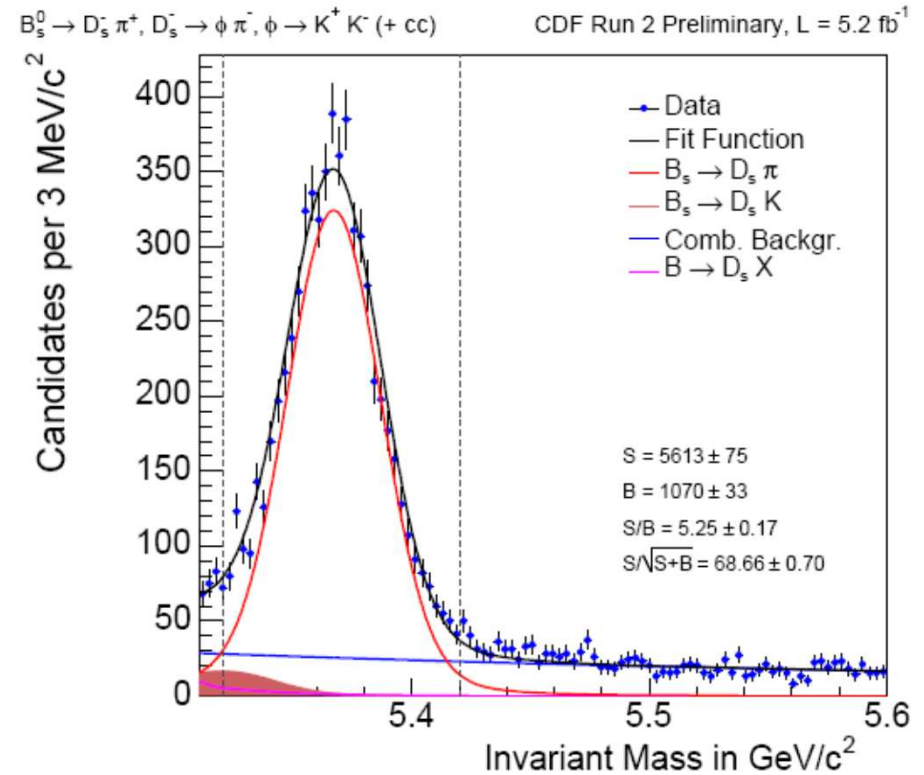
## Same Side Tagging Calibration

- Event-by-event predicted dilution based on simulation
- Calibrated with  $5.2 \text{ fb}^{-1}$  of data; **only use SSKT for corresponding  $5.2/\text{fb}$**
- Simultaneously measuring the  $B_s$  mixing frequency  $\Delta m_s$  and the dilution scale factor  $A$

$$P_{Sig}(ct|\sigma_{ct}, \xi = \xi_D \cdot \xi_P, D) = \frac{1}{N} \cdot \left[ \frac{1}{\tau} e^{-\tilde{t}/\tau} \cdot (1 + \xi A D \cdot \cos(\Delta m_s \tilde{t})) \right] \otimes \mathcal{G}(\tilde{ct}|\sigma_{ct}) \cdot \epsilon(ct|\sigma_{ct})$$

- $D$  – event by event predicted dilution
- $\xi$  – tagging decision = +1, -1, 0 for  $B_s$ ,  $\bar{B}_s$  and un-tagged events
- Fully reconstructed  $B_s$  decays selected by displaced track trigger

Decay Channel	$S$
$B_s^0 \rightarrow D_s^- \pi^+, D_s^- \rightarrow \phi \pi^-$	$5613 \pm 75$
$B_s^0 \rightarrow D_s^- \pi^+, D_s^- \rightarrow K^* K^-$	$2761 \pm 53$
$B_s^0 \rightarrow D_s^- \pi^+, D_s^- \rightarrow (3\pi)^-$	$2652 \pm 52$
$B_s^0 \rightarrow D_s^- (3\pi)^+, D_s^- \rightarrow \phi \pi^-$	$1852 \pm 43$
<b>Sum</b>	<b><math>12877 \pm 113</math></b>





## Same Side Tagging Performance

- $B_s$  oscillation frequency measured  $\Delta m_s = (17.79 \pm 0.07) \text{ ps}^{-1}$  (statistical error only)

- In good agreement with the published CDF measurement with  $1 \text{ fb}^{-1}$

PRL 97, 242003 2006, PRL 97, 062003 2006

$\Delta m_s = 17.77 \pm 0.10 \text{ (stat)} \pm 0.07 \text{ (syst)} \text{ ps}^{-1}$   
used as external constraint in  $\beta_s$  measurement

- Dilution scale factor (amplitude) in good agreement with 1:

$$\mathcal{A} = 0.94 \pm 0.15 \text{ (stat.)} \pm 0.13 \text{ (syst.)}$$

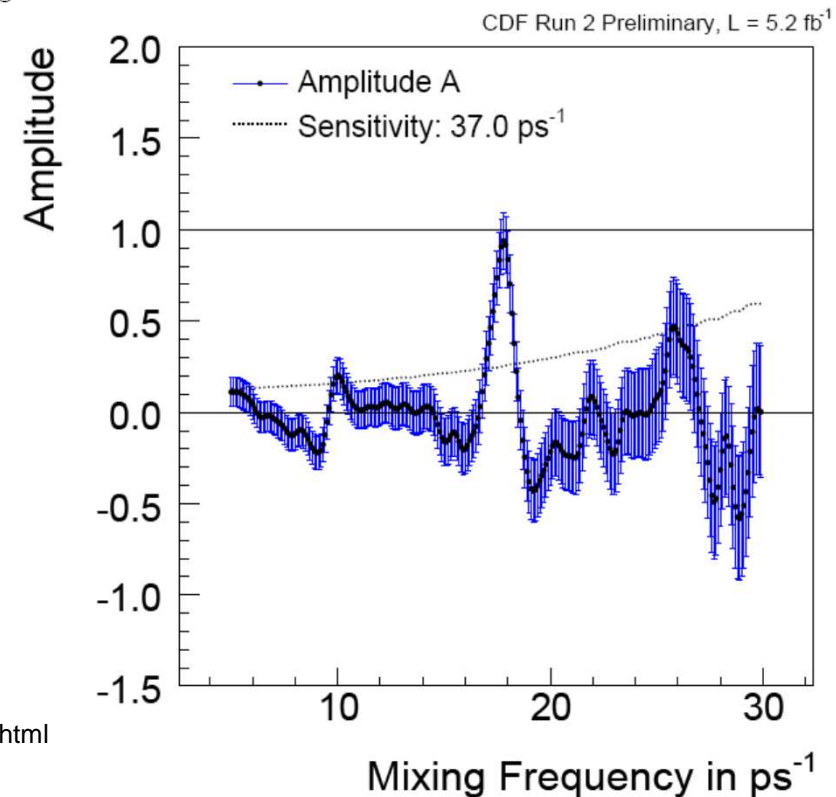
- Largest systematic uncertainty from decay time resolution modeling

- Total SSKT tagging power:

$$\varepsilon \mathcal{A}^2 D^2 = (3.2 \pm 1.4) \%$$

<http://www-cdf.fnal.gov/physics/new/bottom/100204.blessed-sskt-calibration/index.html>

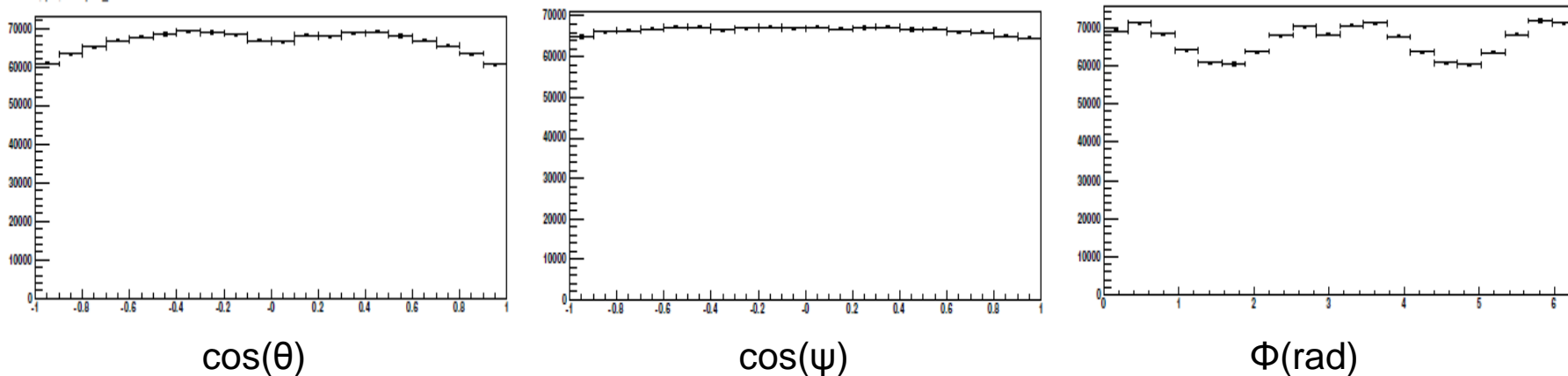
CDF public note 10108



## Detector Angular Efficiency

- *CP even* and *CP odd* final states have different angular distributions
  - use angles  $\rho = (\theta, \phi, \psi)$  to statistically separate *CP even* and *CP odd* components
- Detector acceptance distorts the angular distributions
  - determine 3D angular efficiency function from simulation and account for this effect in the fit

CDF Simulation of Detector Angular Sculpting



## $B_s$ Lifetime and Decay Width Difference

- Assuming SM value of  $\beta_s$  obtain lifetime  $\tau_s$  and decay width difference  $\Delta\Gamma_s$ :

$$\tau(B_s^0) = 1.528 \pm 0.019 \text{ (stat)} \pm 0.009 \text{ (syst)} \text{ ps},$$

$$\Delta\Gamma_s = 0.068 \pm 0.026 \text{ (stat)} \pm 0.007 \text{ (syst)} \text{ ps}^{-1}$$

- Compared to LHCb

Phys. Rev. Lett. 108, 101803 (2012), arXiv:1112.3183v3

$$\Gamma_s = 0.657 \pm 0.009 \text{ (stat)} \pm 0.008 \text{ (syst)} \text{ ps}^{-1},$$

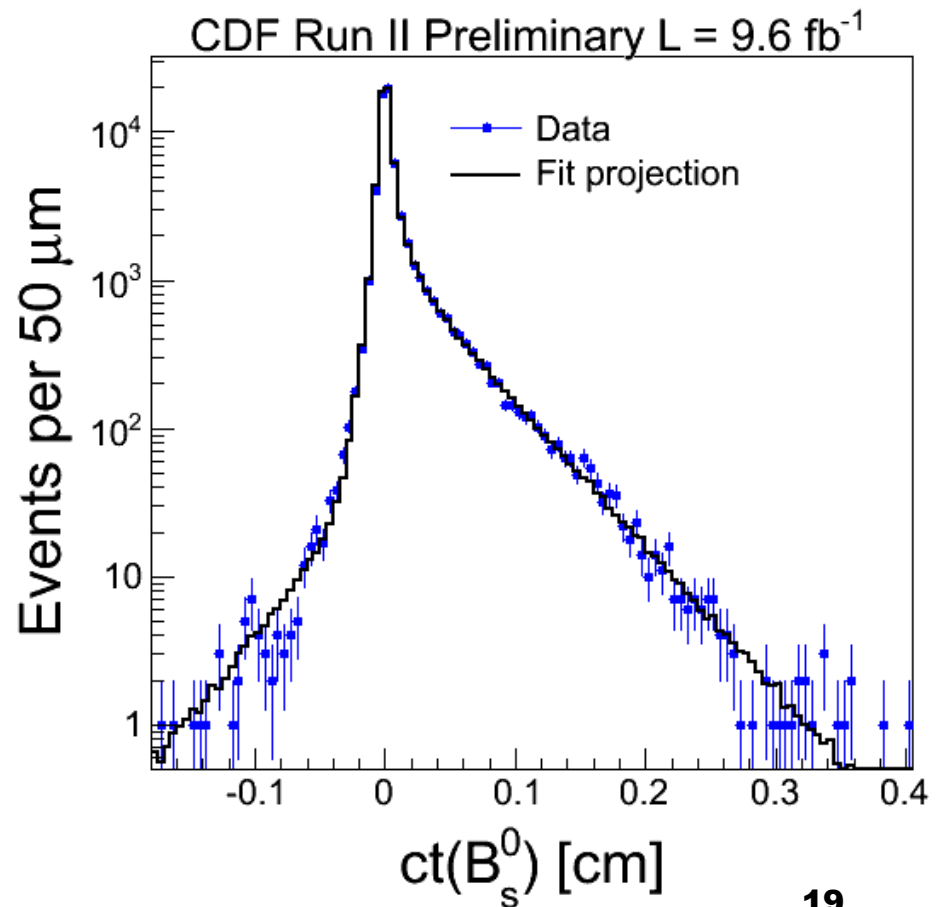
$$\Delta\Gamma_s = 0.123 \pm 0.029 \text{ (stat)} \pm 0.011 \text{ (syst)} \text{ ps}^{-1},$$

- Compared to D0

Phys. Rev. D **85**, 032006 (2012), arXiv:1109.3166

$$\bar{\tau}_s = 1.426^{+0.035}_{-0.032} \text{ ps},$$

$$\Delta\Gamma_s = 0.129^{+0.076}_{-0.053} \text{ ps}^{-1}$$



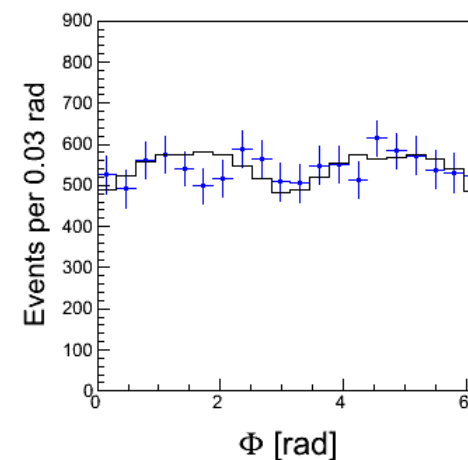
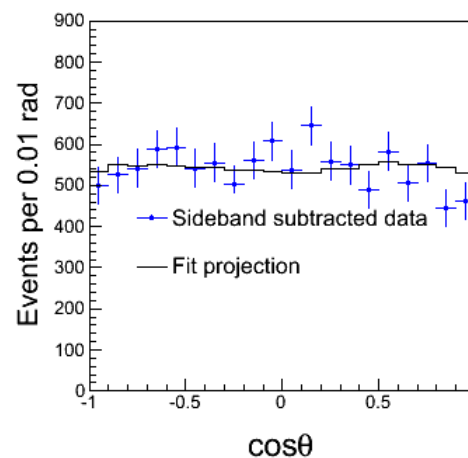
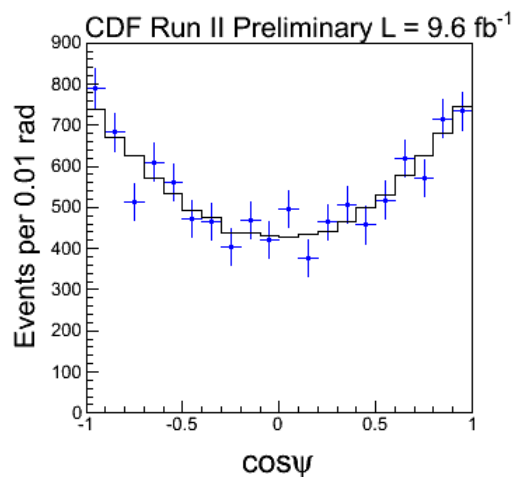
## Polarization Amplitudes

$$|A_0(0)|^2 = 0.512 \pm 0.012 \text{ (stat)} \pm 0.017 \text{ (syst)},$$

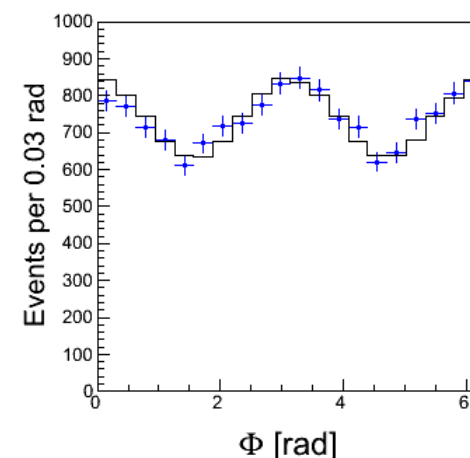
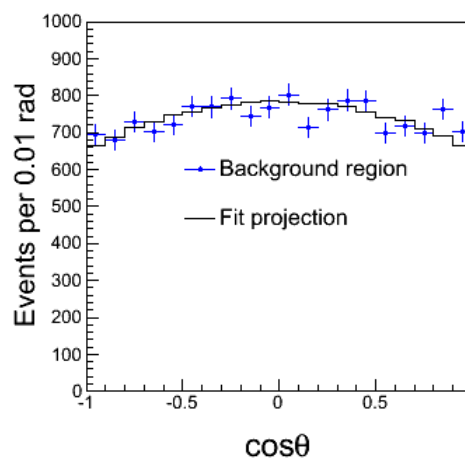
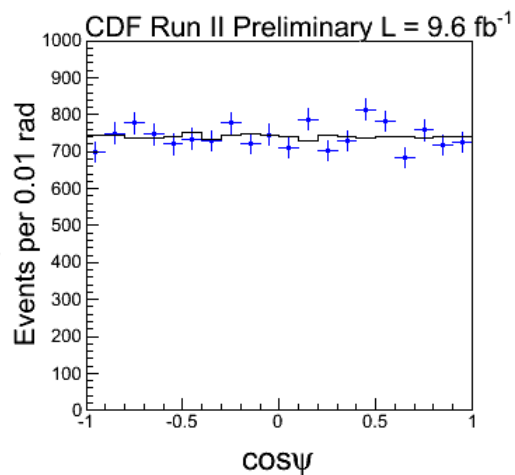
$$|A_{\parallel}(0)|^2 = 0.229 \pm 0.010 \text{ (stat)} \pm 0.014 \text{ (syst)},$$

$$\delta_{\perp} = 2.79 \pm 0.53 \text{ (stat)} \pm 0.15 \text{ (syst) rad}.$$

Signal fit  
projections



Background  
fit projections



## S-Wave

- As noted in [arxiv:0812.2832v3](#), the KK pair in  $B_s \rightarrow J/\psi KK$  decays can be in an s-wave state with  $\sim 6\%$  contribution in a  $\pm 10$  MeV window around the  $\phi$  peak
- Systematic effects from neglecting such contribution were first investigated by [Clarke et al in arxiv:0908.3627v1](#)
- S-wave contribution can be either non-resonant KK or from the  $f^0(980)$  resonance
- To account for potential s-wave contribution, enhance the likelihood function to account for the s-wave amplitude  $A_S$  and interference between s-wave and p-wave
- Time dependence of the s-wave amplitude  $A_S$  is  $CP$ -odd, same as  $A_\perp$
- Mass and phase of s-wave component are assumed flat (good approximation in a narrow  $\pm 10$  MeV around the  $\phi$  mass)
- The fitted s-wave fraction is found to be very small in the KK mass range used in this analysis:  $[1.009, 1.028]$  GeV  
**s-wave fraction  $< 6\%$  at 95% C.L.**
- Interesting to compare with latest D0 result:  $\sim 15 \pm 4\%$  s-wave fraction  
Phys. Rev. D **85**, 032006 (2012), [arXiv:1109.3166](#)  
and LHCb result:  $\sim 4 \pm 2\%$  - // - [arXiv:1202.4717v2](#)

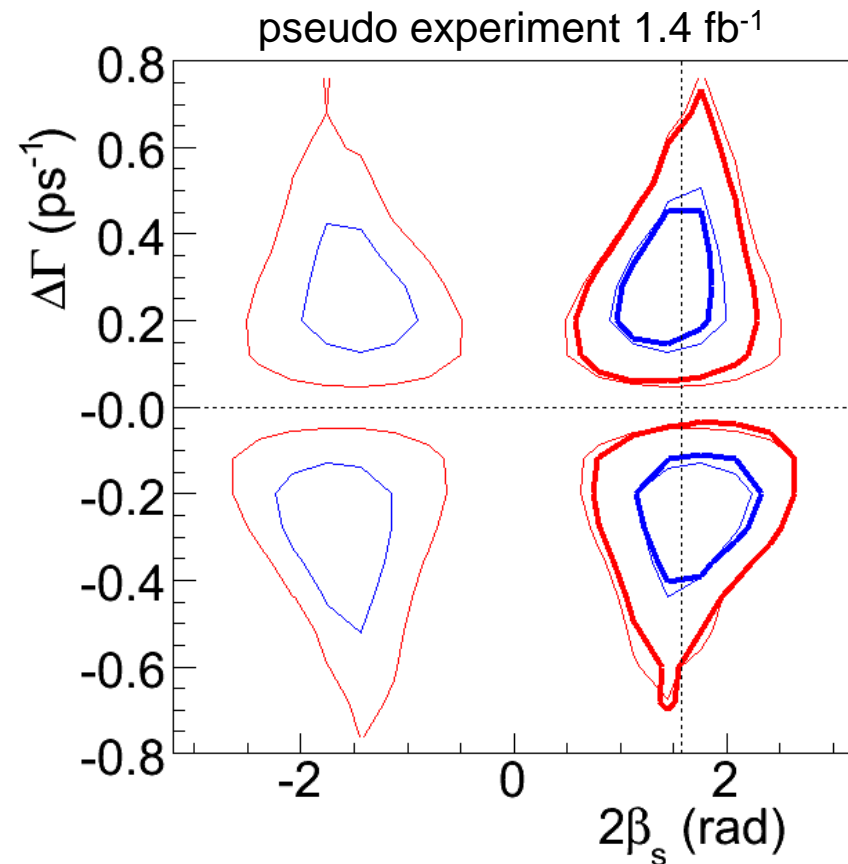
## CP Violation Phase $\beta_s$ in Tagged $B_s \rightarrow J/\Psi\Phi$ Decays

- Without the s-wave the likelihood function is symmetric under the transformation

$$2\beta_s \rightarrow \pi - 2\beta_s \quad \Delta\Gamma \rightarrow -\Delta\Gamma$$

$$\delta_{\parallel} \rightarrow 2\pi - \delta_{\parallel}; \quad \delta_{\perp} \rightarrow \pi - \delta_{\perp}$$

- Study expected effect of tagging using pseudo-experiments
- Improvement of parameter resolution is small due to limited tagging power ( $\epsilon D^2 \sim 4.5\%$  compared to B factories  $\sim 30\%$ )
- However,  $\beta_s \rightarrow -\beta_s$  no longer a symmetry  
 $\rightarrow$  4-fold ambiguity reduced to 2-fold ambiguity
- Adding the s-wave “slightly” breaks the symmetry due to asymmetric  $\Phi$  mass shape
- Symmetry still valid with good approximation...



$$2\Delta\log(L) = 2.3$$

$$2\Delta\log(L) = 6.0$$

— un-tagged

— tagged

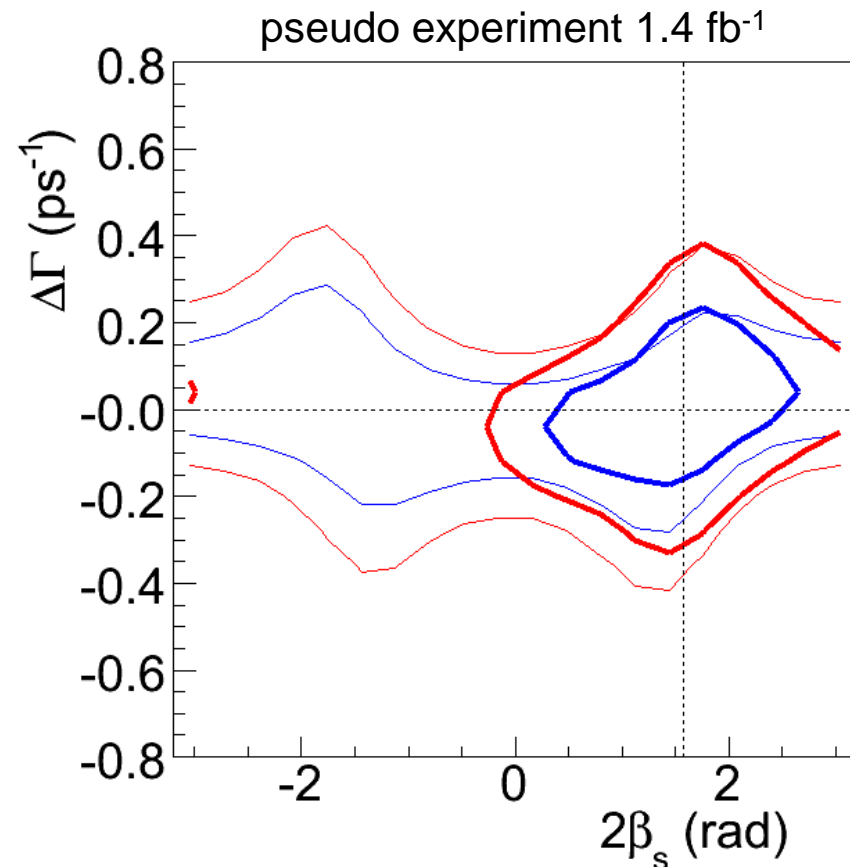
## CP Violation Phase $\beta_s$ in Tagged $B_s \rightarrow J/\psi\Phi$ Decays

- Without the s-wave the likelihood function is symmetric under the transformation

$$2\beta_s \rightarrow \pi - 2\beta_s \quad \Delta\Gamma \rightarrow -\Delta\Gamma$$

$$\delta_{\parallel} \rightarrow 2\pi - \delta_{\parallel}; \quad \delta_{\perp} \rightarrow \pi - \delta_{\perp}$$

- Study expected effect of tagging using pseudo-experiments
- Improvement of parameter resolution is small due to limited tagging power ( $\epsilon D^2 \sim 4.5\%$  compared to B factories  $\sim 30\%$ )
- However,  $\beta_s \rightarrow -\beta_s$  no longer a symmetry  $\rightarrow$  4-fold ambiguity reduced to 2-fold ambiguity
- Adding the s-wave “slightly” breaks the symmetry due to asymmetric  $\Phi$  mass shape
- Symmetry still valid with good approximation

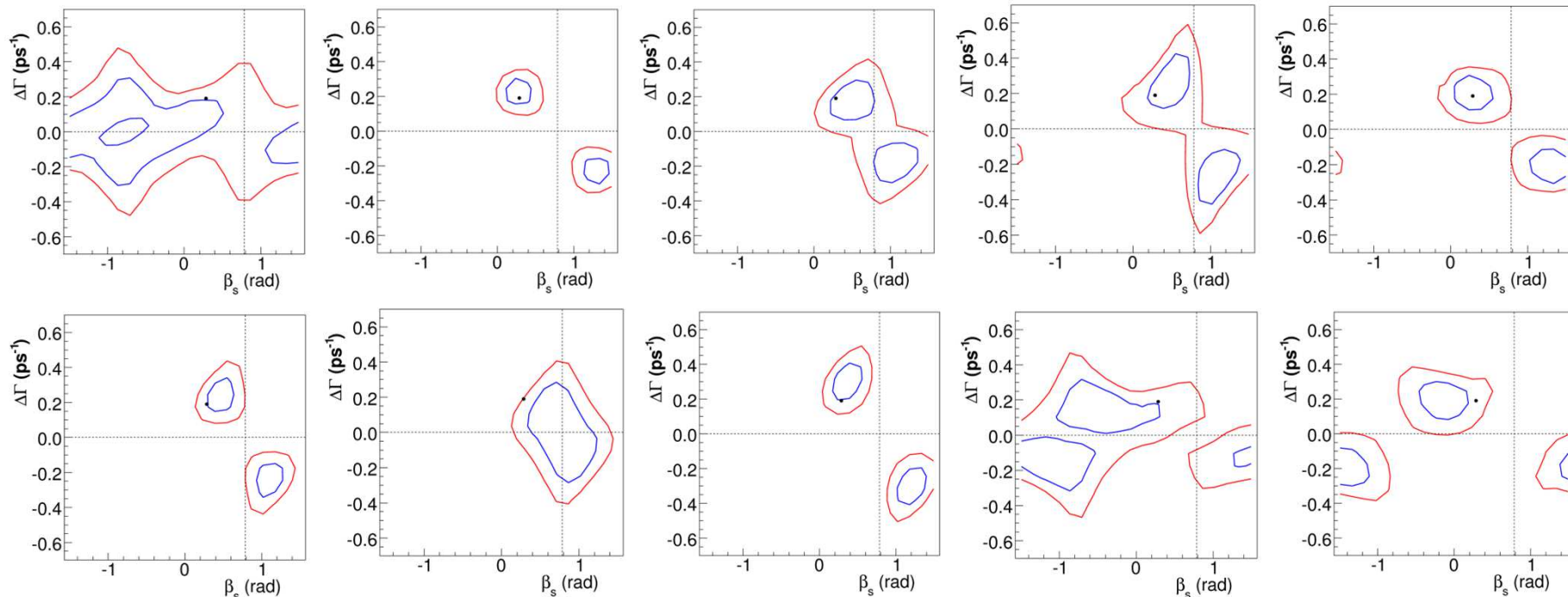


$2\Delta\log(L) = 2.3$  — un-tagged  
 $2\Delta\log(L) = 6.0$  — tagged

## Cross Checks With Pseudo-Experiments

- Generate 10 pseudo-experiments with  $\beta_s = 0.3$  and  $\Delta\Gamma = 0.2$  corresponding to  $1.4 \text{ fb}^{-1}$ 
  - same parameters, just different random seeds
- Large fluctuations expected in shape and size of confidence regions

—  $2\Delta\log(L) = 2.3$   
—  $2\Delta\log(L) = 6.0$





# Comparison Between Different Data Periods

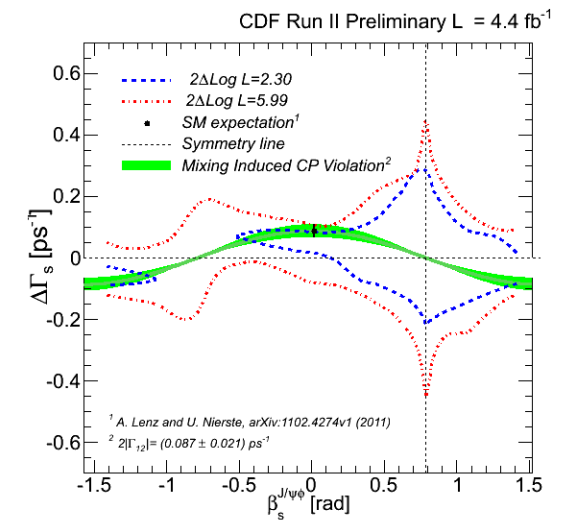
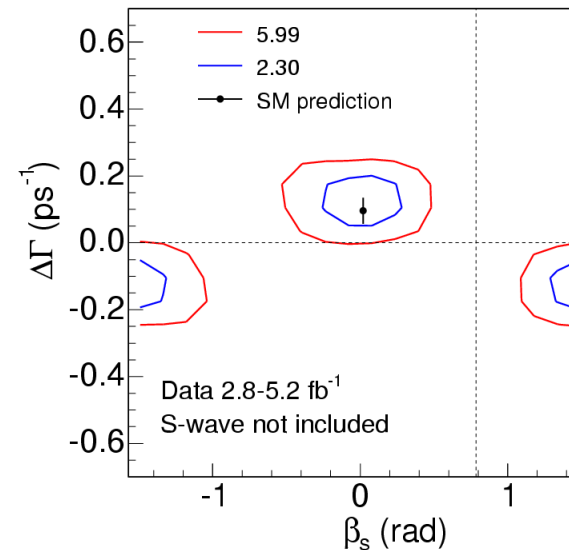
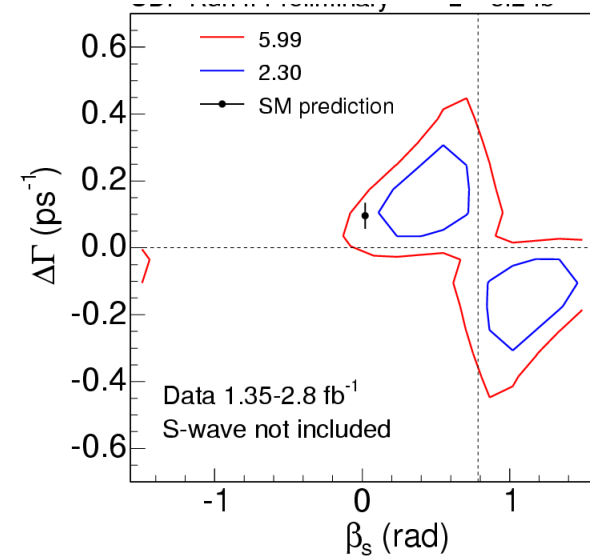
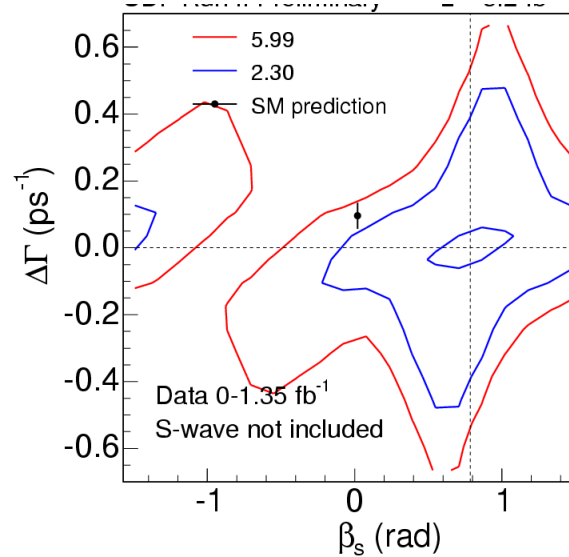
- Divide 9.6 fb<sup>-1</sup> sample in four sub-samples corresponding to four public releases:

0 - 1.4 fb<sup>-1</sup>

1.4 - 2.8 fb<sup>-1</sup>

2.8 - 5.2 fb<sup>-1</sup>

5.2 - 9.6 fb<sup>-1</sup>



<sup>1</sup> A. Lenz and U. Nierste, arXiv:1102.4274v1 (2011)

<sup>2</sup>  $2|\Gamma_{12}| = (0.087 \pm 0.021) \text{ ps}^{-1}$

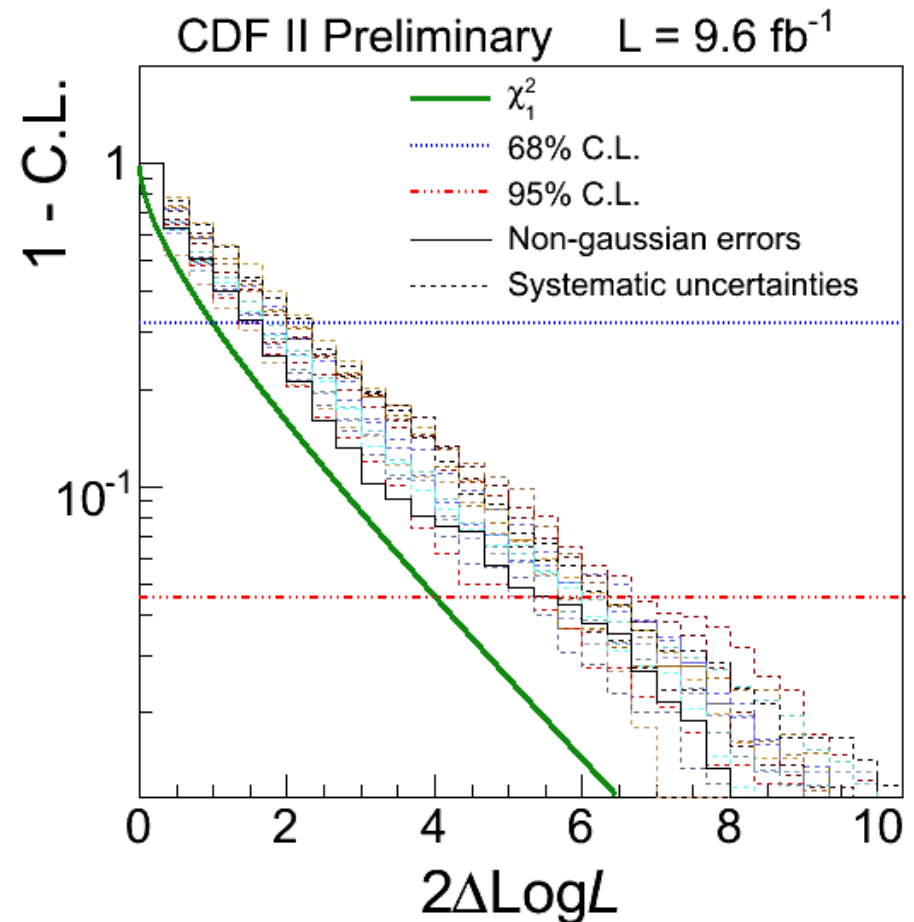
## Non-Gaussian Regime

- Pseudo-experiments show that we are not in Gaussian regime  
→ *quote confidence regions instead of point estimates*

- Using pseudo-experiments establish a “map” between Confidence Level and  $2\Delta\log(L)$

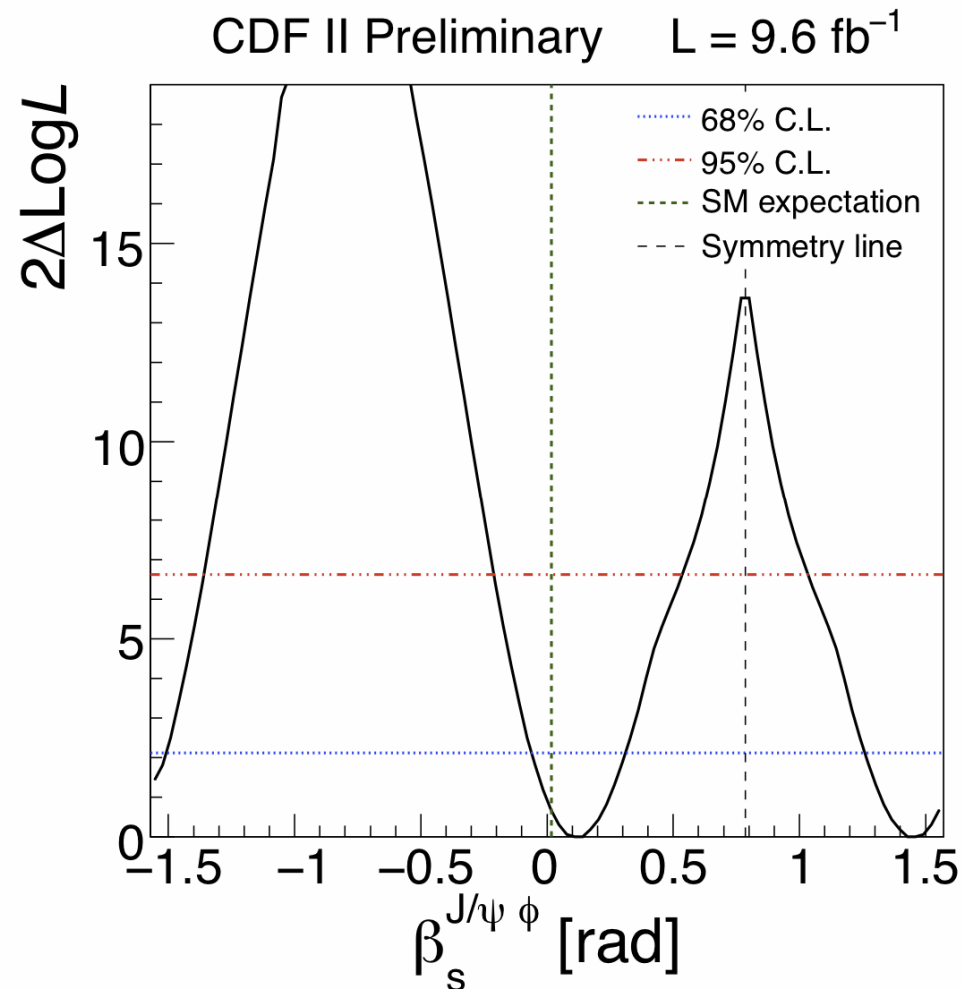
- All nuisance parameters are randomly varied within  $\pm 5\sigma$  from their best fit values and maps of CL vs  $2\Delta\log(L)$  re-derived

- To establish final confidence regions use most conservative case



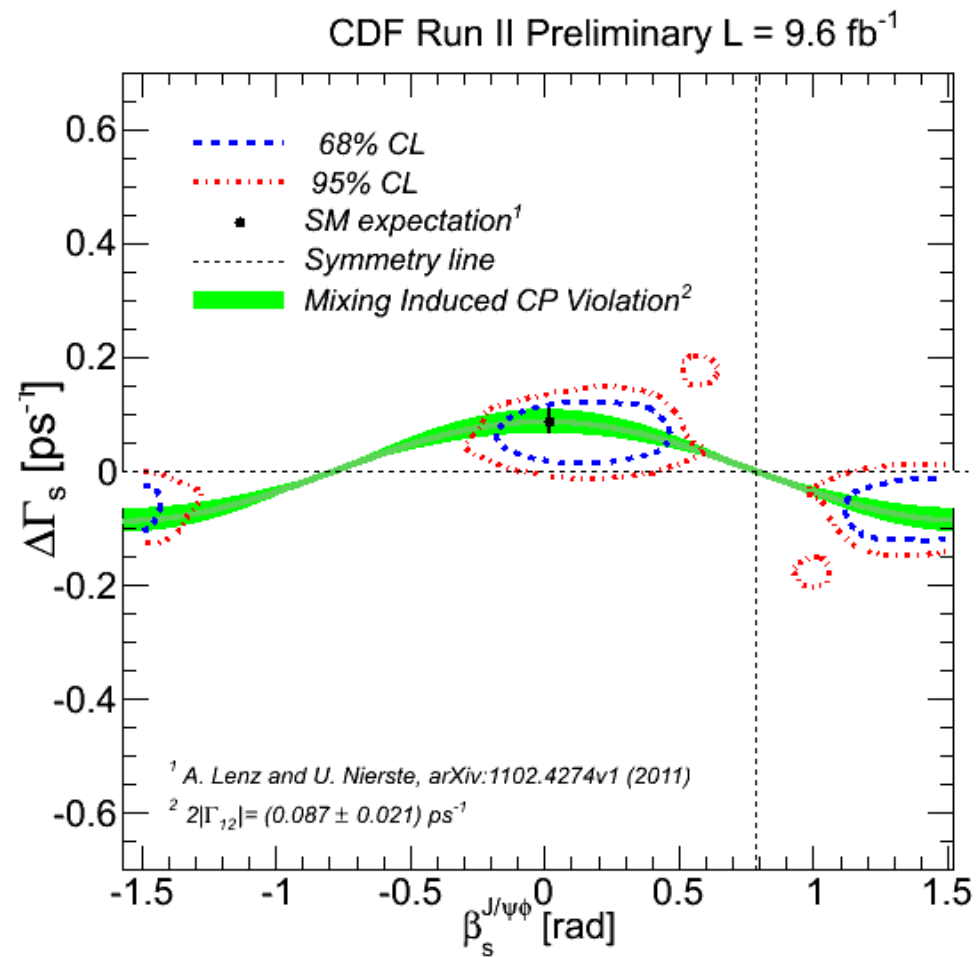
## *CP Violation Phase $\beta_s$ with $9.6 \text{ fb}^{-1}$ at CDF*

$$\beta_s^{J/\psi\phi} \in [-\pi/2, -1.51] \cup [-0.06, 0.30] \cup [1.26, \pi/2] \quad \text{at 68\% CL}$$
$$[-\pi/2, -1.36] \cup [-0.21, 0.53] \cup [1.04, \pi/2] \quad \text{at 95\% CL}$$



## CP Violation Phase $\beta_s$ with $9.6 \text{ fb}^{-1}$ at CDF

- Final confidence regions in  $\beta_s$ - $\Delta\Gamma_s$  space:





## Summary of CDF results

- Measurement of CP violation in  $B_s$  system updated by CDF with full 10/fb sample
- Tightened constraints in  $\beta_s$  space:

$$\beta_s^{J/\psi\phi} \in [-\pi/2, -1.51] \cup [-0.06, 0.30] \cup [1.26, \pi/2] \quad \text{at 68\% CL}$$

- Measurements of  $B_s$  lifetime, decay width difference  $\Delta\Gamma_s$  and polarization amplitudes

$$\tau(B_s^0) = 1.528 \pm 0.019 \text{ (stat)} \pm 0.009 \text{ (syst)} \text{ ps},$$

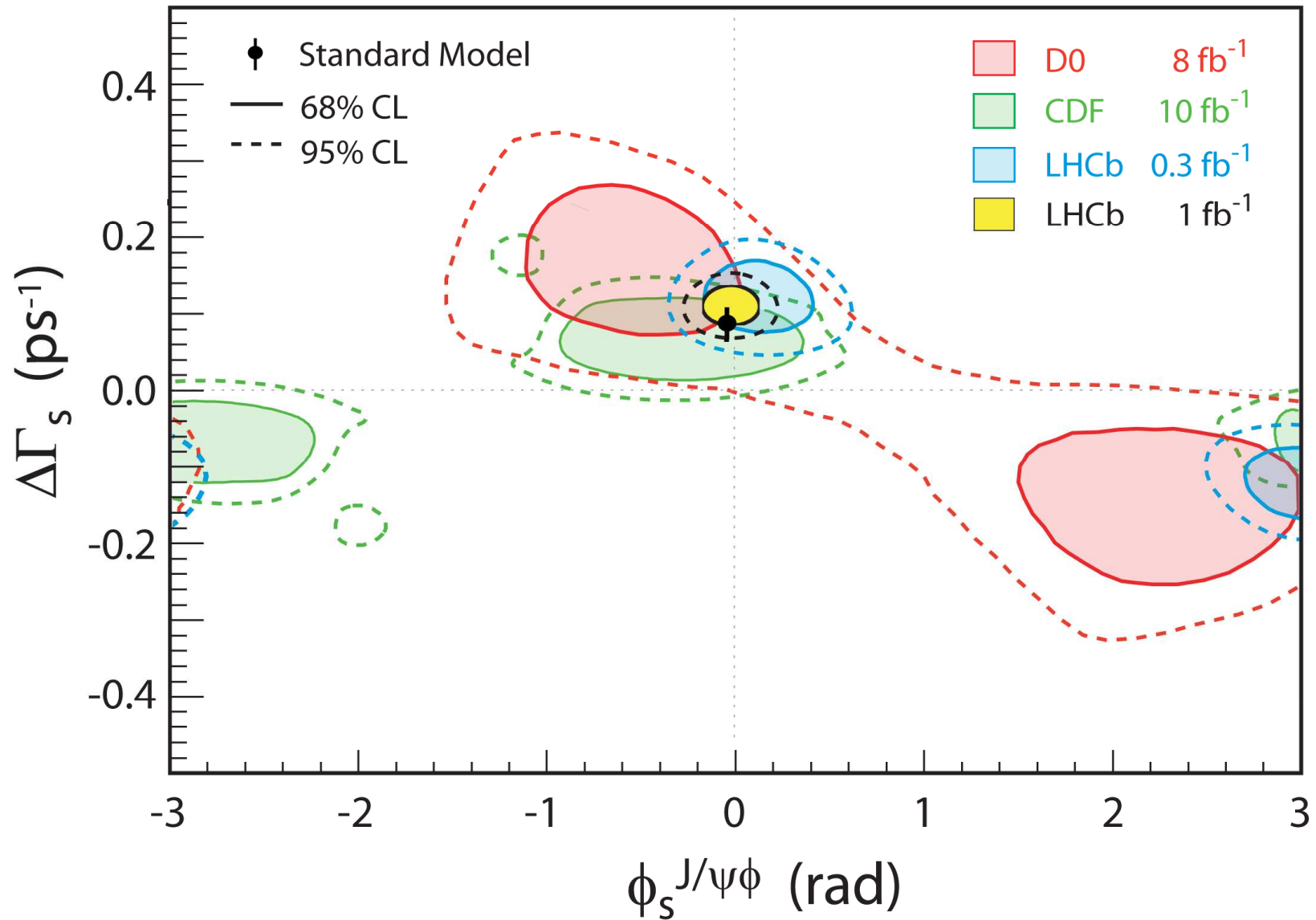
$$\Delta\Gamma_s = 0.068 \pm 0.026 \text{ (stat)} \pm 0.007 \text{ (syst)} \text{ ps}^{-1},$$

$$|A_0(0)|^2 = 0.512 \pm 0.012 \text{ (stat)} \pm 0.014 \text{ (syst)},$$

$$|A_{\parallel}(0)|^2 = 0.229 \pm 0.010 \text{ (stat)} \pm 0.017 \text{ (syst)},$$

$$\delta_{\perp} = 2.79 \pm 0.53 \text{ (stat)} \pm 0.15 \text{ (syst)} \text{ rad.}$$

## Comparison Between CDF, D0 and LHCb



## Note on s-wave and sign of $\Delta\Gamma_s$ (from P. Clarke at Moriond 2012)

- There are two ambiguous solutions related by  $\phi_s \Leftrightarrow \pi - \phi_s$  and  $\Delta\Gamma \Leftrightarrow -\Delta\Gamma$
- We can disambiguate using the P-Wave  $\Leftrightarrow$  S-Wave interference

[Y. Xie et al., JHEP 0909:074, 2009]

Similar to Babar measurement of sign of  $\cos(2\beta)$ , PRD 71, 032005 (2007)

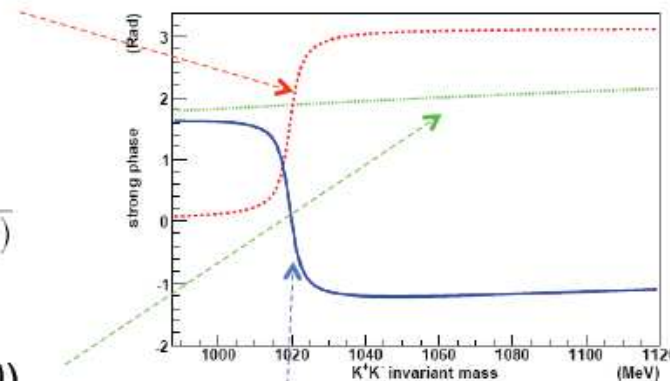
### **K<sup>+</sup>K<sup>-</sup> P-wave:**

Phase of Breit-Wigner amplitude increases rapidly across  $\phi(1020)$  mass region

$$BW(m_{KK}) = \frac{F_r F_D}{m_\phi^2 - m_{KK}^2 - im_\phi \Gamma(m_{KK})}$$

### **K<sup>+</sup>K<sup>-</sup> S-wave:**

Phase of Flatté amplitude for  $f_0(980)$  relatively flat (similar for non-resonance)



### **Phase difference between S- and P-wave amplitudes**

Decreases rapidly across  $\phi(1020)$  mass region

**Resolution method:** choose the solution with decreasing trend of  $\delta_s - \delta_P$  vs  $m_{KK}$  in the  $\phi(1020)$  mass region

5

$\beta_s$  ambiguity resolved by LHCb (from P. Clarke at Moriond 2012)  
**arxiv:1202.4717v2**

- Solution with  $\Delta\Gamma > 0$  has decreasing trend at 4.6 sigma significance

<http://lhcb-public.web.cern.ch/lhcb-public/>

“Recently LHCb physicists have succeeded to measure that the heavier strange-beauty  $B_s$  mesons live longer than the light one”

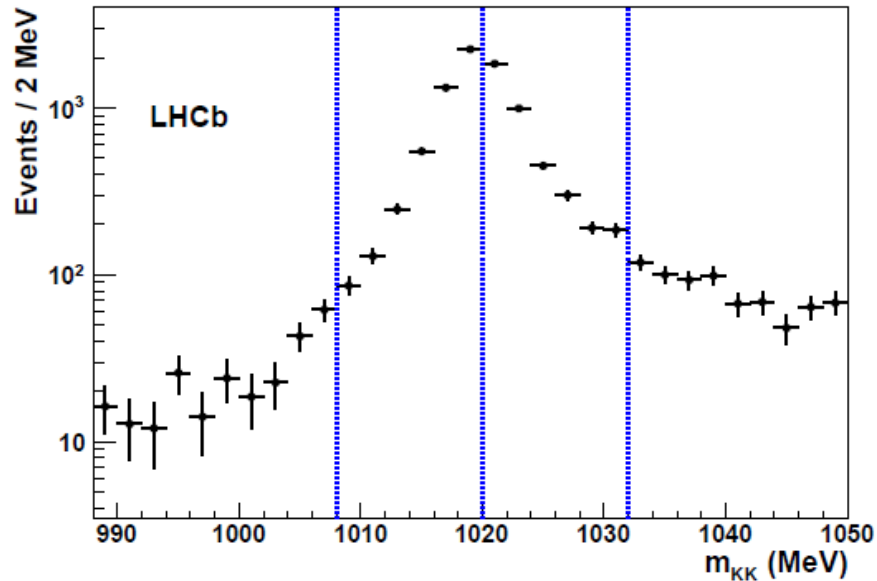


FIG. 2. Background subtracted  $K^+K^-$  invariant mass distribution for  $B_s^0 \rightarrow J/\psi K^+K^-$  candidates. The vertical dotted lines separate the four intervals.

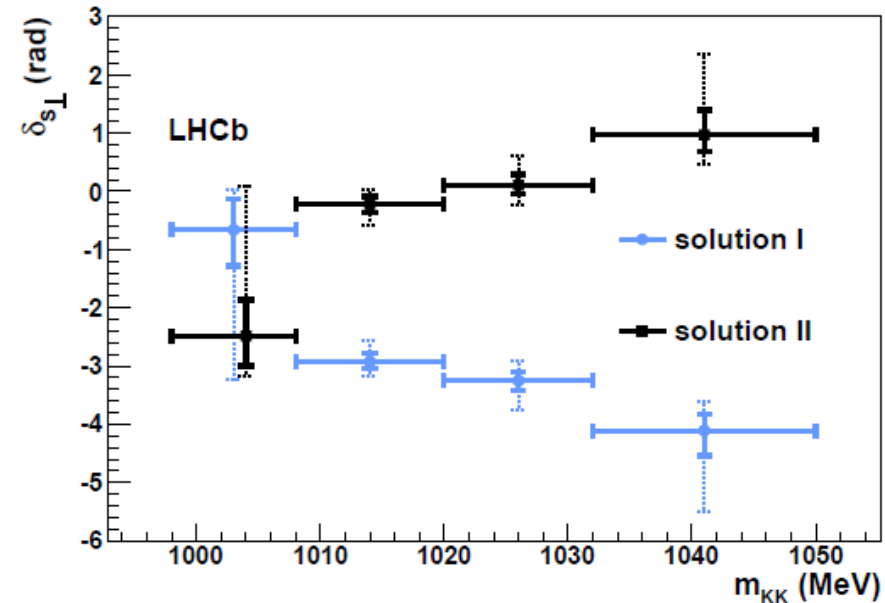
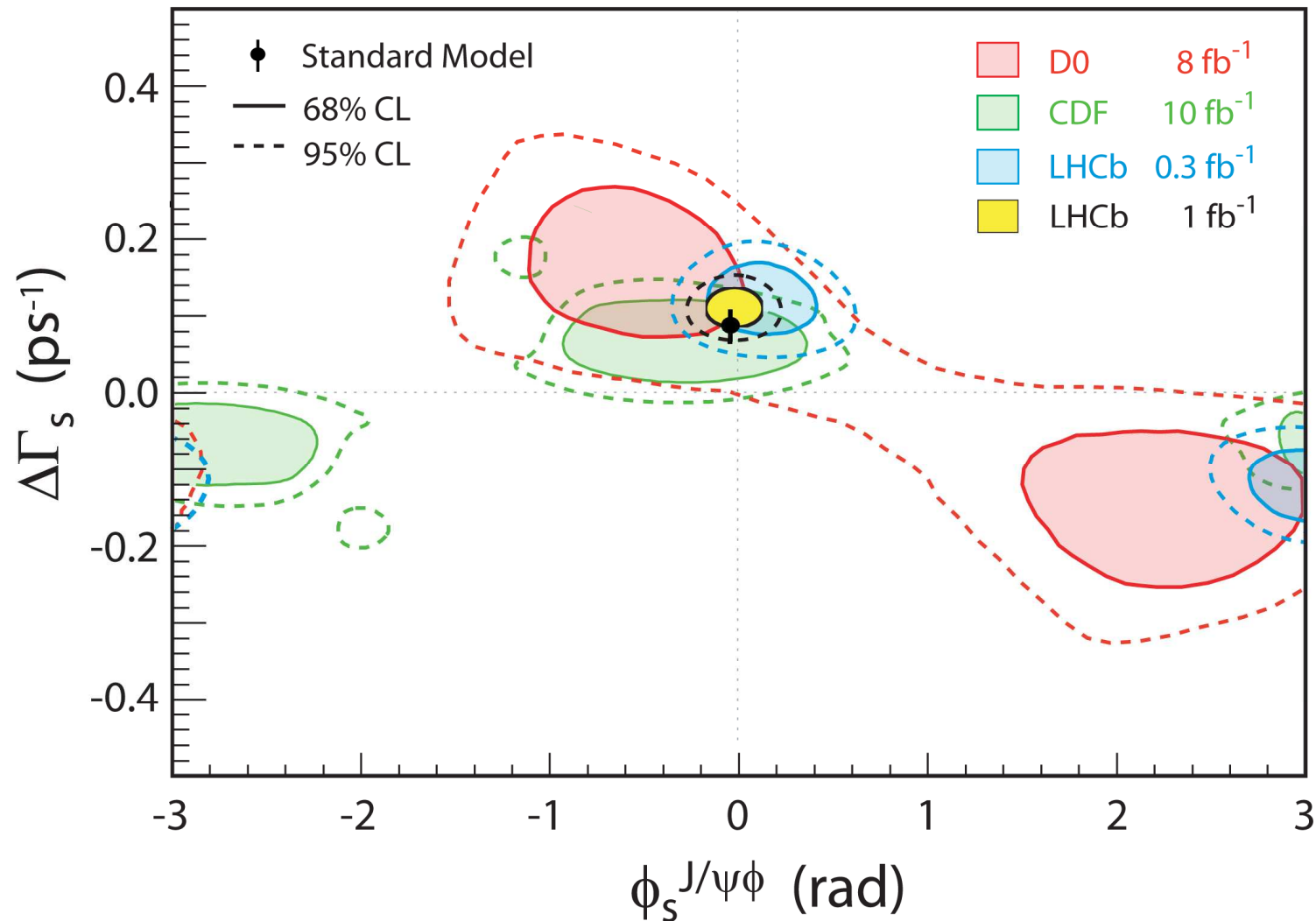


FIG. 4. Measured phase differences between S-wave and perpendicular P-wave amplitudes in four intervals of  $m_{KK}$  for solution I (blue full circles) and solution II (black full squares). The asymmetric error bars correspond to  $\Delta \ln L = -0.5$  (solid) and  $\Delta \ln L = -2$  (dotted).



## Summary

- CDF and D0 have performed first measurements of CP violation in  $B_s$  system
- New Physics may still show up in  $B_s$  decays, hopefully to be found by precision measurements at LHCb





More slides

# CDF Detector

High muon acceptance and  
precise muon ID

Calorimeter for electron ID  
used in flavor tagging

Excellent vertexing (silicon detector)  
→ decay time resolution  $\approx 0.1$  ps

Excellent momentum resolution for improving S/B  
(large radius drift chamber immersed in 1.4 T B field)

$dE/dx$  in drift chamber and TOF  
provide  $1.5\sigma$  pion/kaon ID crucial in  
flavor tagging and signal selection

## $\beta_s$ vs $\phi_s$

- Up to now, introduced two **different** phases:

$$\phi_s^{\text{SM}} = \arg\left(-\frac{M_{12}}{\Gamma_{12}}\right) \approx 4 \times 10^{-3} \quad \text{and} \quad \beta_s^{\text{SM}} = \arg(-V_{ts}V_{tb}^*/V_{cs}V_{cb}^*) \approx 0.02$$

- New Physics affects both phases by **same** quantity  $\phi_s^{\text{NP}}$  (arxiv:0705.3802v2):

$$2\beta_s = 2\beta_s^{\text{SM}} - \phi_s^{\text{NP}}$$

$$\phi_s = \phi_s^{\text{SM}} + \phi_s^{\text{NP}}$$

- If the new physics phase  $\phi_s^{\text{NP}}$  dominates over the SM phases  $2\beta_s^{\text{SM}}$  and  $\phi_s^{\text{SM}}$   
→ neglect SM phases and obtain:

$$2\beta_s = -\phi_s^{\text{NP}} = -\phi_s$$



## Decay Rate

- $B_s \rightarrow J/\psi \phi$  decay rate (A.S. Dighe *et al.*, Phys. Lett. B **369** 144 (1996)) :

$$P_B(\theta, \phi, \psi, t) = \frac{9}{16\pi} |\mathbf{A}(t) \times \hat{n}|^2$$

where:  $\mathbf{A}(t) = (\mathcal{A}_0(t) \cos \psi, -\frac{\mathcal{A}_\parallel(t) \sin \psi}{\sqrt{2}}, i \frac{\mathcal{A}_\perp(t) \sin \psi}{\sqrt{2}})$  and  $\hat{n} = (\sin \theta \cos \phi, \sin \theta \sin \phi, \cos \theta)$

- Time evolution of transversity amplitudes  $A_0, A_\parallel, A_\perp$ :

$$\mathcal{A}_i = \frac{e^{-\Gamma t/2}}{\sqrt{\tau_H + \tau_L \pm \cos 2\beta_s (\tau_L - \tau_H)}} [E_+(t) \pm e^{2i\beta_s} E_-(t)] a_i$$

where  $\pm$  corresponds to CP-even and CP-odd final states,  $\sum_i |a_i|^2 = 1$  and

$$E_\pm(t) \equiv \frac{1}{2} \left[ e^{+(-\frac{\Delta\Gamma}{4} + i\frac{\Delta m}{2})t} \pm e^{-(-\frac{\Delta\Gamma}{4} + i\frac{\Delta m}{2})t} \right]$$

- Finally:

$$\begin{aligned} P_B(\theta, \psi, \phi, t) &= \frac{9}{16\pi} \{ |\mathbf{A}_+(t) \times \hat{n}|^2 + |\mathbf{A}_-(t) \times \hat{n}|^2 + 2\text{Re}((\mathbf{A}_+(t) \times \hat{n}) \cdot (\mathbf{A}_-^*(t) \times \hat{n})) \} \\ &= \frac{9}{16\pi} \{ |\mathbf{A}_+ \times \hat{n}|^2 |f_+(t)|^2 + |\mathbf{A}_- \times \hat{n}|^2 |f_-(t)|^2 + 2\text{Re}((\mathbf{A}_+ \times \hat{n}) \cdot (\mathbf{A}_-^* \times \hat{n}) \cdot f_+(t) \cdot f_-^*(t)) \} \end{aligned}$$

$$|f_\pm(t)|^2 = \frac{1}{2} \frac{(1 \pm \cos 2\beta_s) e^{-\Gamma_L t} + (1 \mp \cos 2\beta_s) e^{-\Gamma_H t} \mp 2 \sin 2\beta_s e^{-\Gamma t} \sin \Delta m t}{\tau_L (1 \pm \cos 2\beta_s) + \tau_H (1 \mp \cos 2\beta_s)} \quad f_+(t) f_-^*(t) = \frac{e^{-\Gamma t} \cos \Delta m t + i \cos 2\beta_s e^{-\Gamma t} \sin \Delta m t + i \sin 2\beta_s (e^{-\Gamma_L t} - e^{-\Gamma_H t})/2}{\sqrt{[(\tau_L - \tau_H) \sin 2\beta_s]^2 + 4\tau_L \tau_H}}$$

## Decay Rate with S-Wave Included

- Including the s-wave contribution the probability density function becomes:

$$\rho_B(\theta, \phi, \psi, t, \mu) = \frac{9}{16\pi} \left| \left[ \sqrt{1 - F_s} g(\mu) \mathbf{A}(t) + e^{i\delta_s} \sqrt{F_s} \frac{h(\mu)}{\sqrt{3}} \mathbf{B}(t) \right] \times \hat{n} \right|^2$$

where:  $\mathbf{B}(t) = (B(t), 0, 0)$  and  $B(t) = \frac{e^{-\Gamma t/2}}{\sqrt{\tau_H + \tau_L - \cos 2\beta_s (\tau_L - \tau_H)}} [E_+(t) - e^{2i\beta_s} E_-(t)]$

CP-odd

$g(\mu)$  is relativistic Breit-Wigner to describe asymmetric  $\Phi$  mass shape and  $h(\mu)$  is constant

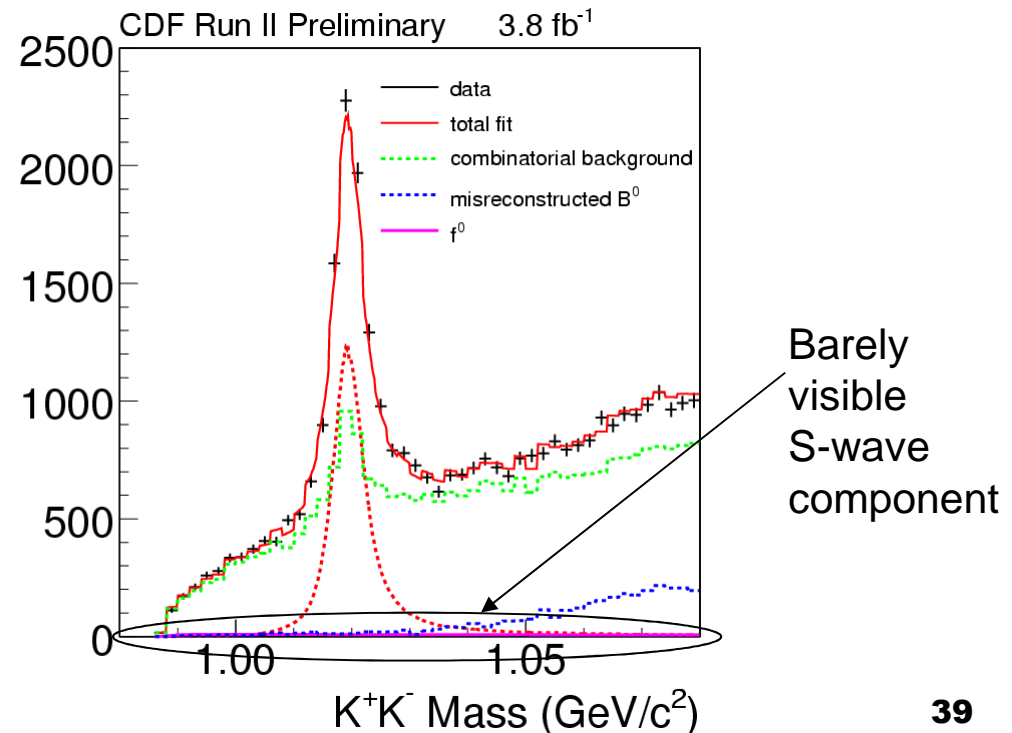
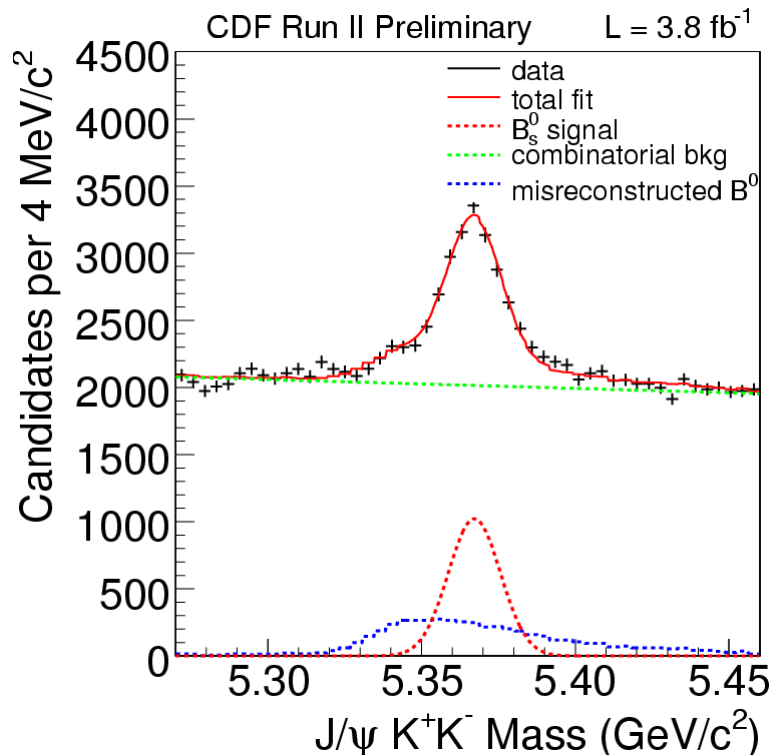
- Integrating out the dependence on the KK mass:

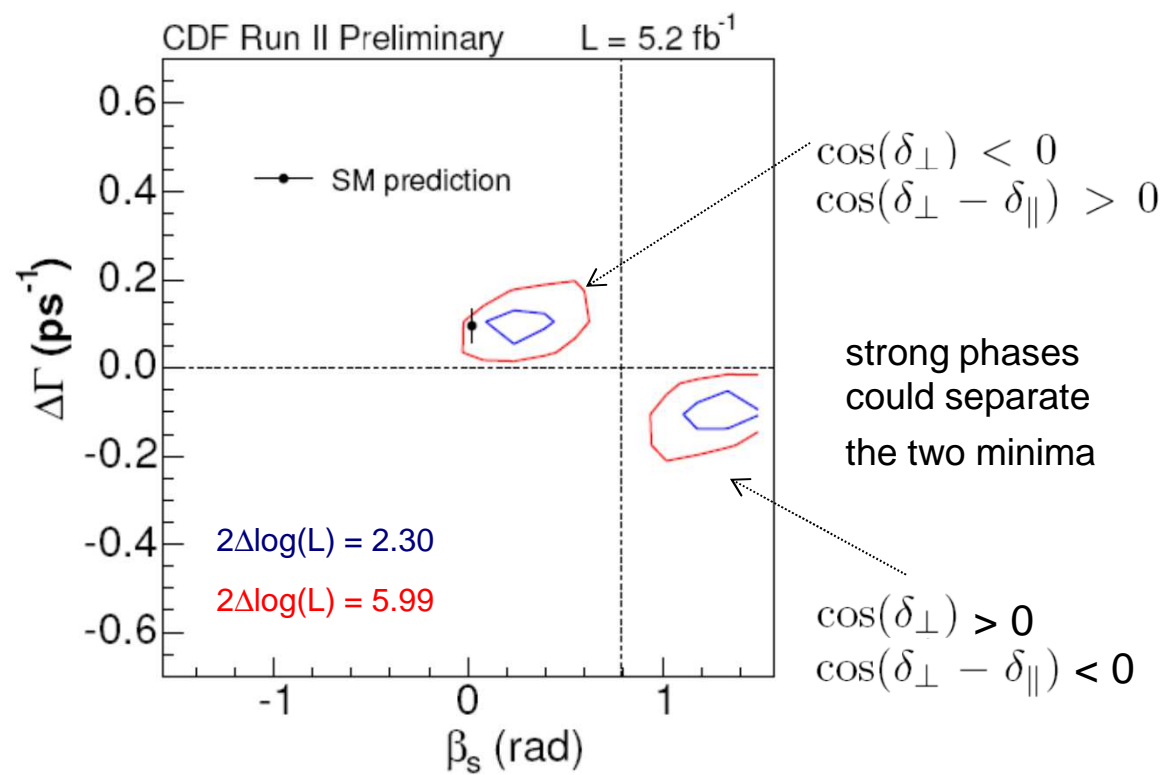
$$\begin{aligned} \rho_B(\theta, \psi, \phi, t) = & (1 - F_s) \cdot P_B(\theta, \psi, \phi, t) + F_s Q_B(\theta, \psi, \phi, t) \\ & + 2 \frac{\sqrt{27}}{16\pi} \text{Re} \left[ \mathcal{I}_\mu \left( (\mathbf{A}_- \times \hat{n}) \cdot (\mathbf{B} \times \hat{n}) \cdot |f_-(t)|^2 + (\mathbf{A}_+ \times \hat{n}) \cdot (\mathbf{B} \times \hat{n}) \cdot f_+(t) \cdot f_-^*(t) \right) \right] \end{aligned}$$

where:  $I(\mu)$  is a function of the s-wave phase and  $Q_B(\theta, \phi, \psi, t) = \frac{3}{16\pi} |\mathbf{B}(t) \times \hat{n}|^2$

## S-Wave Cross Check Using KK Mass Spectrum

- Cross check the result from angular fit by fitting the KK invariant mass spectrum
- From a fit to the  $B_s$  mass distribution with wide KK mass range selection (0.980, 1.080 GeV), determine contributions of combinatorial background, mis-reconstructed  $B^0$ , and  $B_s$  events
- Good fit of the KK mass spectrum with 2%  $f^0$  contributions

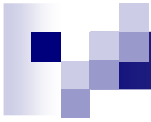






## Fit parameters

$\beta_s$	$\beta_s$ CP -violating phase
$\Delta\Gamma$	$\Gamma_L - \Gamma_H$
$\alpha_{\perp}$	CP odd fraction
$\alpha_{\parallel}$	fraction in CP even states
$\delta_{\perp}$	$\arg(A_{\perp}A_0)$
$\delta_{\parallel}$	$\arg(A_{\parallel}A_0)$
$c\tau$	$\frac{1}{\Gamma_s} = \frac{2}{\Gamma_L + \Gamma_H}$
$A_{SW}$	fraction of S-wave KK component in the signal
$\delta_{SW}$	phase of S-wave component
$\Delta m_s$	$B_s^0$ mixing frequency
$f_s$	Signal fraction
$s_m$	Mass error scale factor
$p_1$	mass background slope
$s_{c\tau 1}$	lifetime error scale factor 1
$s_{c\tau 2}$	lifetime error scale factor 2
$f_{sf1}$	fraction of first lifetime error scale factor
$f_p$	fraction of prompt background
$f_{-}$	fraction of bkg which decays with $\lambda_{-}$
$f_{++}$	fraction of bkg which decays with $\lambda_{++}$
$\lambda_{-}$	Effective bkg lifetime, neg. component
$\lambda_{+}$	Effective bkg lifetime, pos. component 1
$\lambda_{++}$	Effective bkg lifetime, pos. component 2
$\phi_1$	parameter in bkg fit to $\Phi$
$\cos(\vartheta)_1$	parameter in bkg fit to $\cos(\Theta)$
$S_D(OST)$	OST dilution scale factor
$S_D(SST)$	SST dilution scale factor
$\varepsilon_b(OST)$	OST tagging efficiency for background
$\varepsilon_b(SST)$	SST tagging efficiency for background
$A^+(OST)$	OST background positive tag asymmetry
$A^+(SST)$	SST background positive tag asymmetry
$\varepsilon_s(OST)$	OST tagging efficiency for signal
$\varepsilon_s(SST)$	SST tagging efficiency for signal



## *LHCb results, 0.37/fb*

Phys. Rev. Lett. 108, 101803 (2012), [arXiv:1112.3183v3](https://arxiv.org/abs/1112.3183v3)

TABLE I. Fit results for the solution with  $\Delta\Gamma_s > 0$  with statistical and systematic uncertainties.

parameter	value	$\sigma_{\text{stat.}}$	$\sigma_{\text{syst.}}$
$\Gamma_s$ [ps <sup>-1</sup> ]	0.657	0.009	0.008
$\Delta\Gamma_s$ [ps <sup>-1</sup> ]	0.123	0.029	0.011
$ A_{\perp}(0) ^2$	0.237	0.015	0.012
$ A_0(0) ^2$	0.497	0.013	0.030
$ A_S(0) ^2$	0.042	0.015	0.018
$\delta_{\perp}$ [rad]	2.95	0.37	0.12
$\delta_S$ [rad]	2.98	0.36	0.12
$\phi_s$ [rad]	0.15	0.18	0.06

## *D0 results, 8/fb*

Phys. Rev. D **85**, 032006 (2012), [arXiv:1109.3166](https://arxiv.org/abs/1109.3166)

$$\overline{\tau}_s = 1.426^{+0.035}_{-0.032} \text{ ps},$$

$$\Delta\Gamma_s = 0.129^{+0.076}_{-0.053} \text{ ps}^{-1}$$

$$\phi_s^{J/\psi\phi} = -0.49^{+0.48}_{-0.40},$$

$$|A_0|^2 = 0.552^{+0.016}_{-0.017},$$

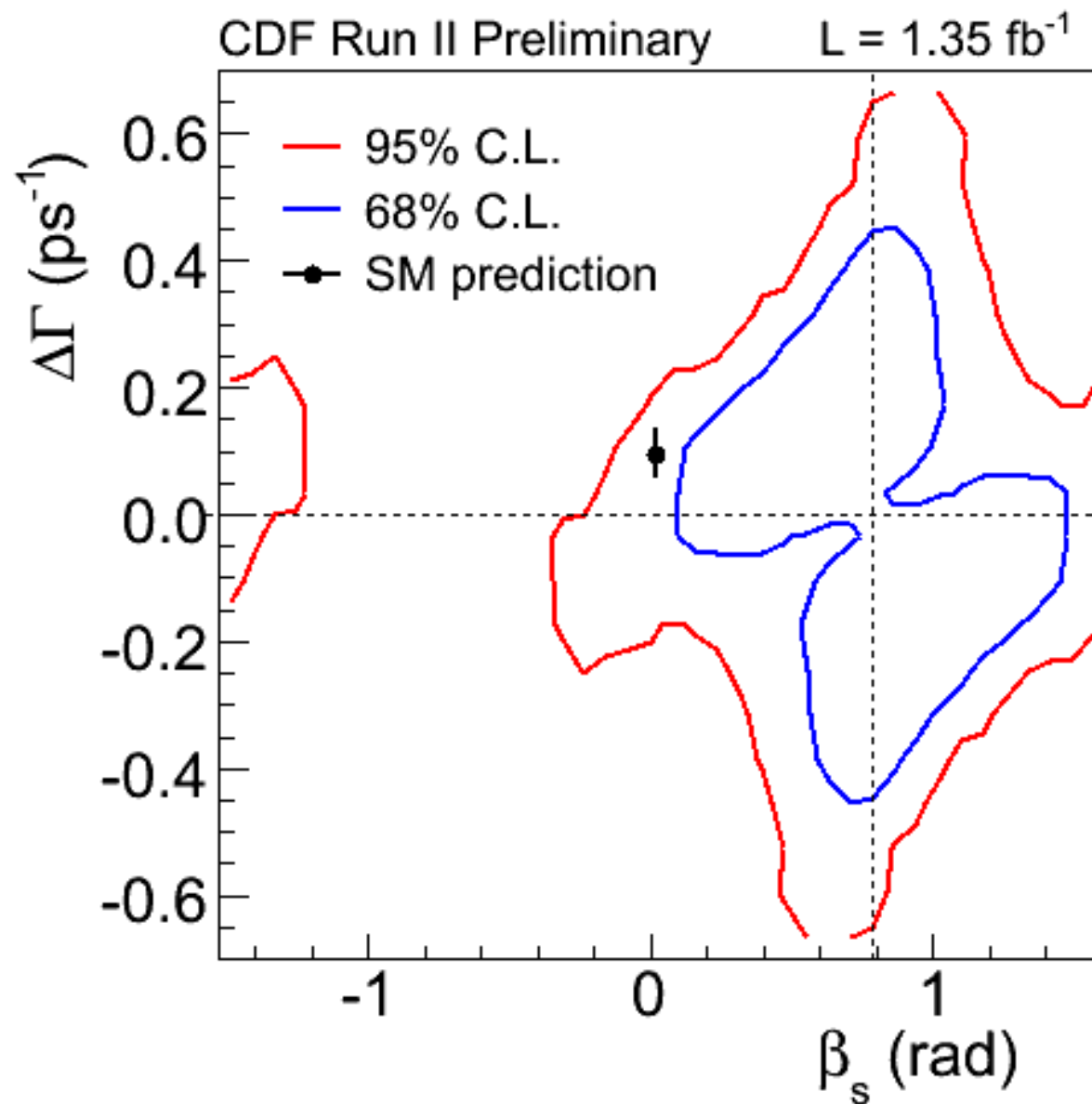
$$|A_{\parallel}|^2 = 0.219^{+0.020}_{-0.021},$$

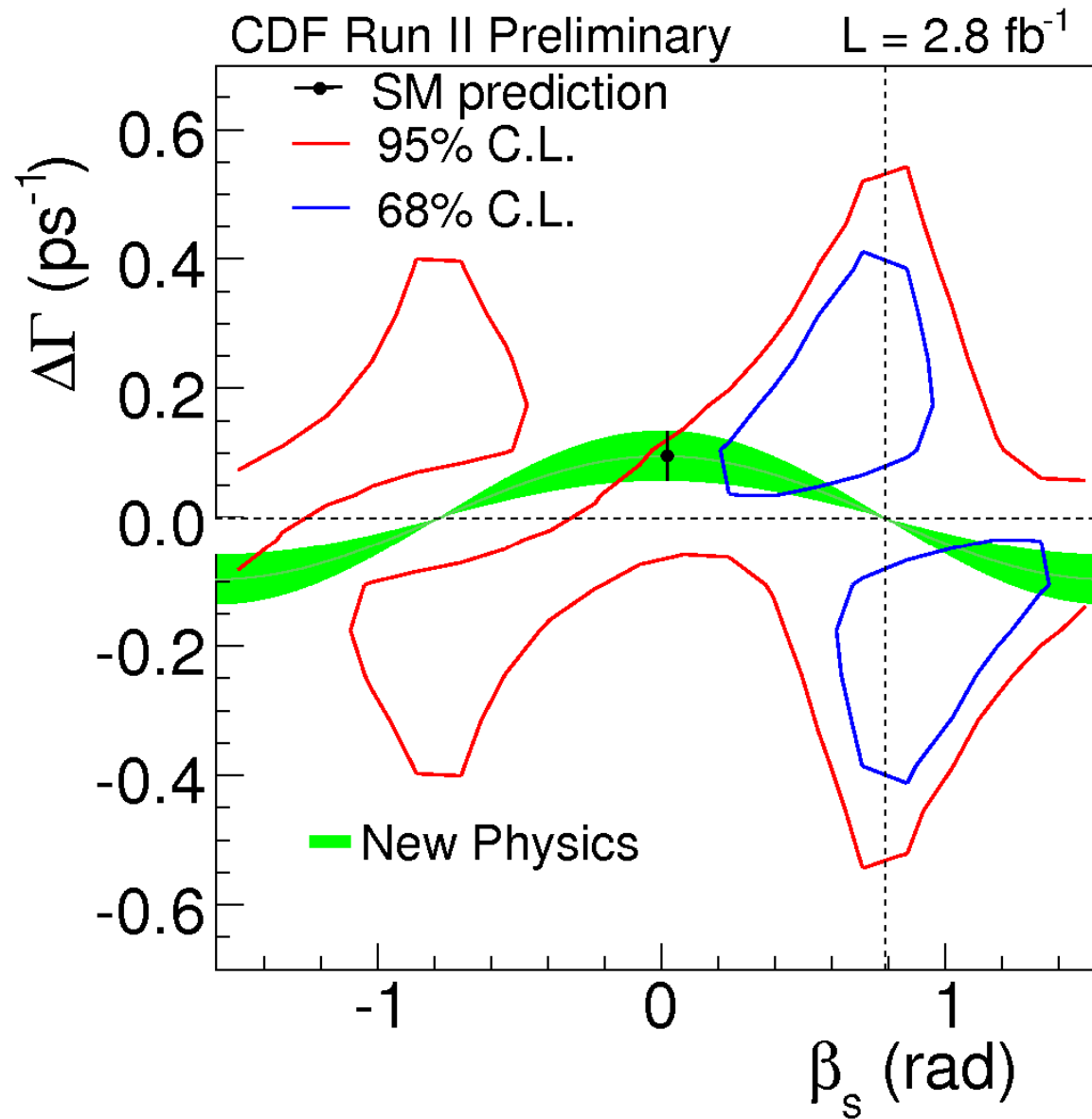
$$\delta_{\parallel} = 3.15 \pm 0.27,$$

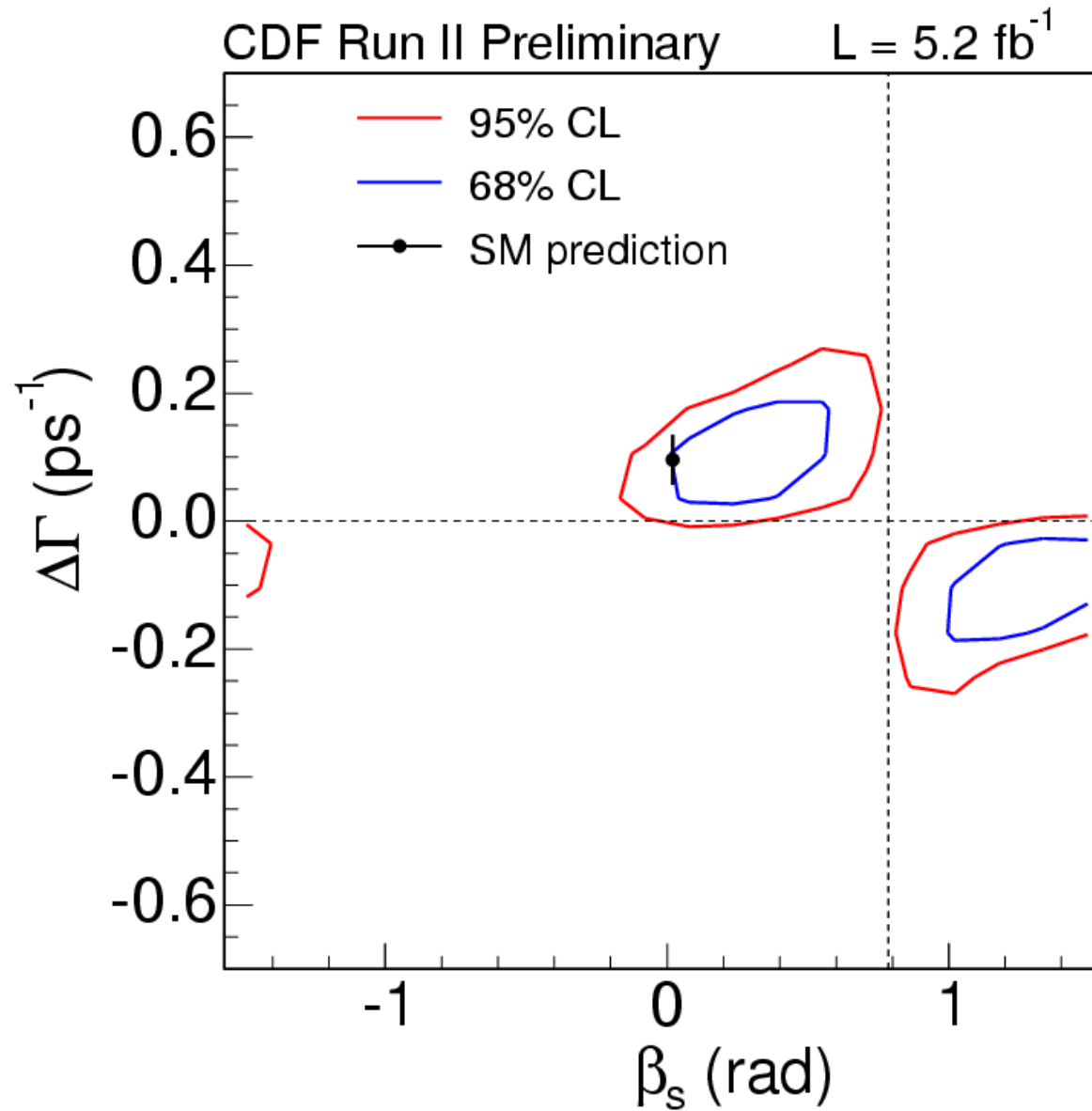
$$\cos(\delta_{\perp} - \delta_s) = -0.06 \pm 0.24,$$

$$F_S(\text{eff}) = 0.146 \pm 0.035.$$

CDF 2007 initial result , arXiv:0712.2397, PRL 100,161802 (2008) , 1.4/fb, ~2000 signal events







CDF 2012 update, 5.6/fb, ~11000 signal events

