## Phys 531 Assignment 3

1. Consider a series of $m$ parallel planar interfaces, as shown. Starting from 0 , the index of refraction in the $i$ th layer is $n_{i}$, and the angle of incidence on the $i$ th interface is $\theta_{i-1}$. Find the output angle $\theta_{m}$ in terms of the input angle $\theta_{0}$.

2. Show that to someone looking straight down into a swimming pool, any object in the water will appear to be at about $3 / 4$ of its true depth.
3. A laser beam impinges on the top surface of a parallel glass plate of thickness $t$ and index of refraction $n$. In terms of the angle of incidence, $\theta_{i}$, determine the true length of the path through the glass, $d$, and the lateral displacement of the beam, $\delta$.

4. Show from the Fresnel equations that $R_{\|}+T_{\|}=1$ and $R_{\perp}+T_{\perp}=1$. Restrict yourself to the case where the index and transmission angle are real.
5. Calculate the reflectances $R_{\perp}$ and $R_{\|}$for the interface beween air and SF11 glass (index $n=1.7$ ) at incident angles of $0^{\circ}$ and $45^{\circ}$. What is Brewster's angle in this case?
6. You notice the reflection of the sun in the still waters of a pond. If the angle of incidence of the sunlight on the water is about $60^{\circ}$, what fraction of the incident light are you actually observing? Note that sunlight, like most natural light, is an equal mixture of both polarization states.
7. A beam of light is normally incident on a right angle prism, as shown. What is the minimum value of the index of refraction such that the beam is totally internally reflected from the back surfaces?

