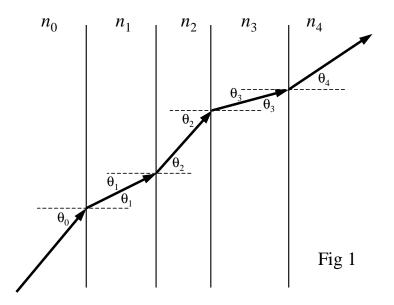
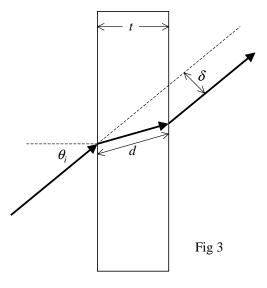
## Phys 531 Assignment 3

1. Consider a series of m parallel planar interfaces, as shown. Starting from 0, the index of refraction in the *i*th layer is  $n_i$ , and the angle of incidence on the *i*th interface is  $\theta_{i-1}$ . Find the output angle  $\theta_m$  in terms of the input angle  $\theta_0$ .



2. Show that to someone looking straight down into a swimming pool, any object in the water will appear to be at about 3/4 of its true depth.

3. A laser beam impinges on the top surface of a parallel glass plate of thickness t and index of refraction n. In terms of the angle of incidence,  $\theta_i$ , determine the true length of the path through the glass, d, and the lateral displacement of the beam,  $\delta$ .



4. Show from the Fresnel equations that  $R_{\parallel} + T_{\parallel} = 1$  and  $R_{\perp} + T_{\perp} = 1$ . Restrict yourself to the case where the index and transmission angle are real.

5. Calculate the reflectances  $R_{\perp}$  and  $R_{\parallel}$  for the interface between air and SF11 glass (index n = 1.7) at incident angles of 0° and 45°. What is Brewster's angle in this case?

6. You notice the reflection of the sun in the still waters of a pond. If the angle of incidence of the sunlight on the water is about 60°, what fraction of the incident light are you actually observing? Note that sunlight, like most natural light, is an equal mixture of both polarization states.

7. A beam of light is normally incident on a right angle prism, as shown. What is the minimum value of the index of refraction such that the beam is totally internally reflected from the back surfaces?

