## Majorana materializes



Mourik et al., Science 2012


Jason Alicea (Caltech)

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Felix von Oppen (Berlin)
Conan Weeks (UBC)
Ruqian Wu (UCI)
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## Outline

- Majorana fermions: what they are \& why they're interesting
- The quest for Majorana in the solid state
- Getting the most out of Majorana fermions
- Experimental status \& closing remarks


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## Exchange statistics

Describes how wavefunctions transform when indistinguishable particles exchange positions
$\psi\left(\mathbf{r}_{1}, \ldots, \mathbf{r}_{\mathbf{N}}\right)$


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$$
\psi\left(\mathbf{r}_{1}, \ldots, \mathbf{r}_{\mathbf{N}}\right) \quad \longrightarrow \quad \psi^{\prime}\left(\mathbf{r}_{1}, \ldots, \mathbf{r}_{\mathbf{N}}\right)
$$



Extraordinarily fundamental!
Underlies most condensed matter phenomena.

## Role of dimensionality

$\mathbf{d}=3$
Only bosons \& fermions


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$\mathbf{d}=\mathbf{2}$
Anyons are now possible!


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$\mathbf{d}=\mathbf{2}$
Anyons are now possible!

$\mathbf{d}=\mathbf{I}$
Exchange not well defined...

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## Role of dimensionality

$\mathbf{d}=3$
Only bosons \& fermions

$d=\mathbf{2}$
Anyone are now possible!

$\mathbf{d}=\mathbf{I}$
Exchange not well defined...
...because particles inevitably "collide"

Non-Abelian anyons


## Non-Abelian anyons


"Rotates" wavefunction to a different quantum state!

$$
\psi_{a} \rightarrow U_{a b} \psi_{b}
$$

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$$
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$$

Urgently wanted for topological quantum computation

Kitaev; Freedman; Preskill; Frohlich, etc. Nayak, Simon, Stern, Freedman, \& Das Sarma, RMP 80, 1083 (2008)

Simplest source of non-Abelian statistics: Majorana fermions

## The "inventor" of Majorana fermions


> "There are many categories of scientists: people of second and third rank, who do their best, but do not go very far; there are also people of first-class rank, who make great discoveries, fundamental to the development of science. But then there are the geniuses, like Galileo and Newton. Well Ettore Majorana was one of them." -Enrico Fermi

Ettore Majorana (1906-1938?)

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"There are many categories of scientists: people of second and third rank, who do their best, but do not go very far; there are also people of first-class rank, who make great discoveries, fundamental to the development of science. But then there are the geniuses, like Galileo and Newton. Well Ettore Majorana was one of them." -Enrico Fermi
"Majorana had greater gifts than anyone else in the world. Unfortunately he lacked one quality which other men generally have: plain common sense." -Enrico Fermi

## The Search for Majorana fermions

## Majorana fermions are their own antiparticle <br> $$
\gamma=\gamma^{\dagger}
$$

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$$

Neutrinos?


## The Search for Majorana fermions

## Majorana fermions are their own antiparticle <br> $$
\gamma=\gamma^{\dagger}
$$



74\% Dark Energy

## The Search for Majorana fermions

## Majorana fermions

 are their own antiparticle $\gamma=\gamma^{\dagger}$

Observation would reveal something quite profound about nature.


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## Majorana fermions in condensed matter?

Typical metal or insulator

## Majorana fermions in condensed matter?


$c^{\dagger}|\psi\rangle \quad$ (Adds an electron)

## Majorana fermions in condensed matter?



$$
\begin{array}{cc}
c^{\dagger}|\psi\rangle & \text { (Adds an electron) } \\
c|\psi\rangle & \text { (Adds a hole) }
\end{array}
$$

## Majorana fermions in condensed matter?



Majorana appears only through emergent excitations

## Majorana fermions in condensed matter?



$$
\begin{gathered}
c^{\dagger}|\psi\rangle \quad \text { (Adds an electron) } \\
c|\psi\rangle \quad \text { (Adds a hole) } \\
C^{\dagger} \neq C
\end{gathered}
$$

Majorana appears only through emergent excitations


-     - 


## Superconductors <br> are natural platforms <br> $f^{\dagger} \sim u c^{\dagger}+v c$

## Majorana via topological superconductivity

## "Spinless" 2D superconductor



## Majorana via topological superconductivity

## "Spinless" 2D superconductor



## Majorana via topological superconductivity

## "Spinless" 2D superconductor

Vortices bind Majorana zeromodes


One Majorana = "half" a usual fermion
Ground-state degeneracy + non-locality

$$
\begin{aligned}
& f_{A}=\gamma_{1}+i \gamma_{2} \\
& f_{B}=\gamma_{3}+i \gamma_{4}
\end{aligned}
$$

Vortices exhibit non-Abelian statistics

## Majorana via topological superconductivity

## "Spinless" 2D superconductor

Vortices bind Majorana zeromodes


## "Spinless" ID <br> superconductor



Majorana zero-modes localize at the ends of the system...
...but are they interesting \& useful? YES!

## The basic challenge

"Spinless" ID, 2D superconductivity is hard to find
I.We live in 3D


## The basic challenge

"Spinless" ID, 2D superconductivity is hard to find
I.We live in 3D

2. Electrons carry spin


## The basic challenge

## "Spinless" ID, 2D superconductivity is hard to find

I. We live in 3D

2. Electrons carry spin

3. Vast majority of superconductors form spin-singlet Cooper pairs


## Two ways forward

I. Search for new compounds w/exotic superconductivity

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Matthias's 6th rule: Stay away from theorists!

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I. Search for new compounds w/exotic superconductivity

Matthias's 6th rule: Stay away from theorists!
2."Engineer" topological superconductivity from available materials

Theorists can be useful, particularly if methods involve weakly interacting electrons

## Many roads to Majorana fermions in 2D

## "Intrinsic"



Willet, Eisenstein, et al. (1987)
Moore \& Read (1991)
Bonderson, Kitaev, Shtengel (2006)
Stern \& Haperin (2006)

## "Engineered"



Fu \& Kane (2008)


Sau, Tewari, Lutchyn, Das Sarma (2010)

...lots of
others

## ID "spinless" superconductivity via edge states




## I. By construction ID \& "spinless" <br> II. Easy to make superconducting

## ID "spinless" superconductivity via edge states





# I. By construction ID \& "spinless" 

II. Easy to make superconducting

Fu \& Kane 2009

## ID "spinless" superconductivity via edge states

## Ordinary Superconductor



## Small number of 2D topological insulators


I. By construction ID \& "spinless"
II. Easy to make superconducting

## Aside:Topological insulator in graphene?



Ist proposed topological
insulator, but gap is tiny:
$<0.01 \mathrm{meV}$

Kane \& Mele, PRL (2005)
Weeks, Hu, Alicea, Franz, Wu, PRX (20I I); Hu et al., arXiv:I206.4320

## Aside:Topological insulator in graphene?



## Ist proposed topological insulator, but gap is tiny: $<0.01 \mathrm{meV}$

Osmium


Experiments underway...

## Majorana fermions in ID wires

ID spin-orbit-coupled wire (e.g. $\operatorname{lnSb}$ )


## Majorana fermions in ID wires

ID spin-orbit-coupled wire (e.g. $\operatorname{lnSb}$ )


## Majorana fermions in ID wires



## Generates aID 'spinless' superconductor with Majorana fermions!

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## Harnessing non-Abelian statistics



Alicea, Oreg, Refael, von Oppen, Fisher, Nature Phys. 2010 Clarke, Sau, Tewari, PRB 2010
Halperin, Oreg, Stern, Refael, Alicea, von Oppen, PRB 201 I

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## Non-Abelian statistics possible using ID wires!

## Harnessing non-Abelian statistics



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Non-Abelian statistics possible using ID wires!

## Blueprints for quantum computers

Need to supplement braiding with additional operations...


Hassler, Akhmerov, Hou, Beenakker (2010)


Hassler, Akhmerov, Beenakker (201I)


Sau, Tewari, Das Sarma (20I0)



Bonderson and Lutchyn (2010)

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J. R. Williams, ${ }^{1}$ A. J. Bestwick, ${ }^{1}$ P. Gallagher, ${ }^{1}$ Seung Sae Hong, ${ }^{2}$ Y. Cui, ${ }^{3,4}$ Andrew S. Bleich, ${ }^{5}$ J. G. Analytis, ${ }^{2,4}$ I. R. Fisher,,${ }^{2,4}$ and D. Goldhaber-Gordon ${ }^{1}$

## Signatures of Majorana Fermions in Hybrid Superconductor-Semiconductor Nanowire Devices

V. Mourik, ${ }^{1 *}$ K. Zuo, ${ }^{1 *}$ S. M. Frolov, ${ }^{1}$ S. R. Plissard, ${ }^{2}$ E. P. A. M. Bakkers, ${ }^{1,2}$ L. P. Kouwenhoven ${ }^{1} \dagger$

Evidence of Majorana fermions in an Al - InAs nanowire topological superconductor Anindya Das*, Yuval Ronen*, Yonatan Most, Yuval Oreg, Moty Heiblum\#, and Hadas Shtrikman

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Observation of the fractional ac Josephson effect: the signature of Majorana particles

Leonid P. Rokhinson, ${ }^{1,2, *}$ Xinyu Liu, ${ }^{3}$ and Jacek K. Furdyna ${ }^{3}$
A. D. K. Finck, D. J. Van Harlingen, P. K. Mohseni, K. Jung, and X. Li Phys. Rev. Lett. 110, 126406 (2013)

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Superconductor-Nanowire Devices from Tunneling to the Multichannel Regime:
Zero-Bias Oscillations and Magnetoconductance Crossover
H. O. H. Churchill, ${ }^{1,2}$ V. Fatemi, ${ }^{2}$ K. Grove-Rasmussen, ${ }^{3}$ M. T. Deng, ${ }^{4}$ P. Caroff, ${ }^{4}$ H. Q. Xu, ${ }^{4,5}$ and C. M. Marcus

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## Detection via transport

## Normal reflection

## Insulator

# Conventional <br> Superconductor 

## Detection via transport

## Andreev reflection

## Insulator

# Conventional <br> Superconductor 

## Detection via transport

No Majoranas $\quad$ Perfect normal reflection $\quad \square G=0$


Sengupta et al. (200 I); Bolech, Demler (2007); Law, Lee, Ng (2009); Fidkowski, Alicea, Lindner, Lutchyn, Fisher (20I2)

## Experimental results



Mourik et al., Science 2012

$\underline{B \neq 0}$


## Experimental results



$$
\underline{B}=0
$$

$\underline{B \neq 0}$

Mourik et al., Science 2012


## Braiding on the horizon?




Mourik et al., Science 2012

## "More is different"...

## ...even at the macroscale

Topological insulators
Non-Abelian anyons
Majorana fermions
Parafermions
Fibonacci
can be "engineered" by combining simple ingredients


Mong, Clarke, JA, Lindner, Fendley, Nayak, Oreg, Stern, Berg, Shtengel, Fisher, arXiv: I 307.4403

## Thanks for your attention!

I. Beenakker, Annual Review of

Recent reviews:

Condensed Matter Physics 4,
II3 (2013)
2. Alicea, Reports on Progress in Physics 75, 07650 ( 2012 )

## Confirming non-Abelian statistics


I. Nucleate Majoranas from the vacuum
2. Check that fusing pairs you created returns the ground state
3. Exchange Majoranas

## Confirming non-Abelian statistics


5. Can detect excitation using Josephson measurements
I. Nucleate Majoranas from the vacuum
2. Check that fusing pairs you created returns the ground state
3. Exchange Majoranas
4. Fusing pairs in same way as in 2 should now yield excited state with 50\% probability

