

Basic Theory

Lepton
Universality
Massive
Neutrinos

Experiment

Geant4
Simulation
Digitizer
MWPC
mTPC
CsI

Precise Determination of the Pion Electronic Decay Branching Ratio

Charles Glaser

University of Virginia

PEN Collaboration



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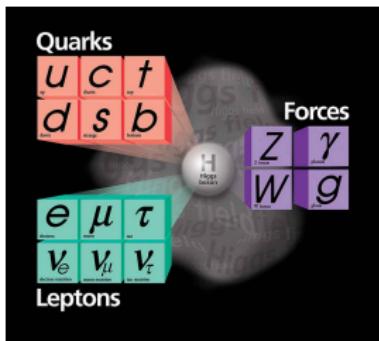
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- Basic Theory/PEN
- Motivations
 - Lepton Universality
 - Massive Neutrinos
- Experiment
- Geant4 Simulation
 - Waveform Digitizer
 - Multi-Wire Proportional Chamber
 - Mini-Time Projection Chamber
 - CsI EM Calorimeter
 - Putting it together



Standard Model



- expected particles of nature
- spontaneous symmetry breaking- mass
- local gauge invariance- gauge bosons (force mediators)

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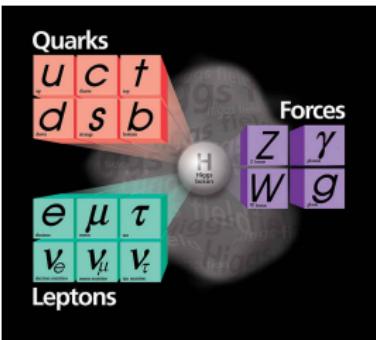
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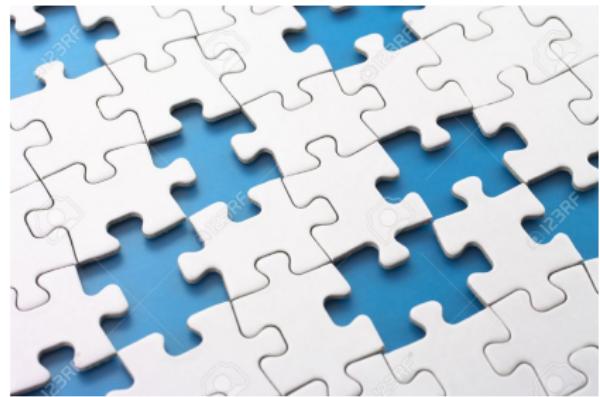
Standard Model



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Not complete:

- why 3 generations?
- dark matter?
- massive/sterile neutrinos?
- supersymmetry?



Theory/PEN

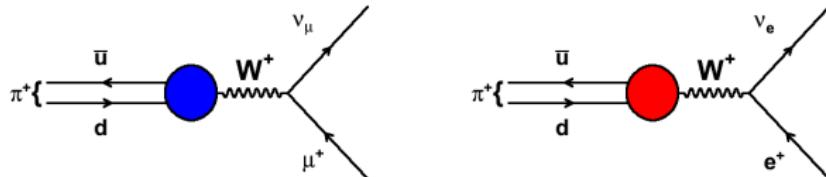
Explore the (V–A) interaction through a precision measurement

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$$\frac{\Gamma(\pi^+ \rightarrow e^+ \nu_e (\gamma))}{\Gamma(\pi^+ \rightarrow \mu^+ \nu_\mu (\gamma) \rightarrow e^+ \nu_e \bar{\nu}_\mu)} = \left(\frac{g_e}{g_\mu} \right)^2 \left(\frac{m_e}{m_\mu} \right)^2 \frac{\left(1 - \left(\frac{m_e}{m_\mu} \right)^2 \right)^2}{\left(1 - \left(\frac{m_\mu}{m_\pi} \right)^2 \right)^2} (1 + \delta_R)$$

Theoretical BR: $(1.2352 \pm 0.0001) \times 10^{-4}$

*

Experimental BR: $(1.230 \pm 0.004) \times 10^{-4}$

δ_R rad/loop corrections in SM, non V–A extensions

$$\left(\frac{g_e}{g_\mu} \right)^2 = 1.0021 \pm 0.0016 \text{ (experimental)}$$

Goal: relative uncertainty 5×10^{-4} or better

* D.Počanić et al J. Physics G 2014 41 11



Theory/PEN

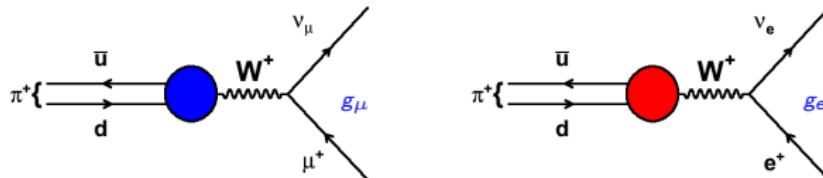
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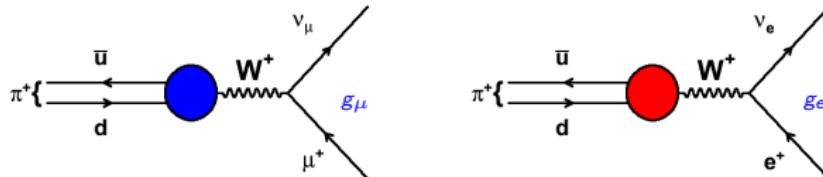
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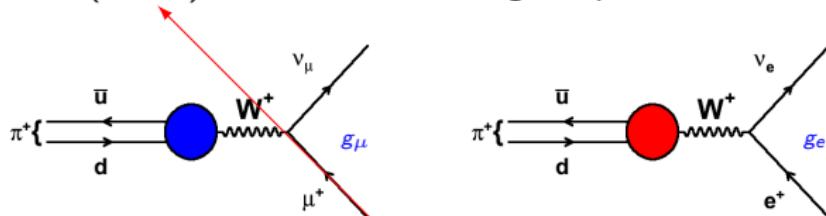
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Reach of π_{e2} decay beyond the SM (New Physics)

$$\begin{aligned}\mathcal{L}_{\text{NP}} = & \left[\pm \frac{\pi}{2\Lambda_V^2} \bar{u} \gamma_\alpha d \pm \frac{\pi}{2\Lambda_A^2} \bar{u} \gamma_\alpha \gamma_5 d \right] \bar{e} \gamma^\alpha (1 - \gamma_5) \nu \\ & + \left[\pm \frac{\pi}{2\Lambda_S^2} \bar{u} d \pm \frac{\pi}{2\Lambda_P^2} \bar{u} \gamma_5 d \right] \bar{e} (1 - \gamma_5) \nu, \quad (\Lambda_i \dots \text{scale of NP})\end{aligned}$$

CKM unitarity and superallowed Fermi nuclear decays currently limit:

$$\Lambda_V \geq 20 \text{ TeV}, \quad \text{and} \quad \Lambda_S \geq 10 \text{ TeV}.$$

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At $\Delta R_{e/\mu}^\pi / R_{e/\mu}^\pi = 10^{-3}$, π_{e2} decay is directly sensitive to:

$$\boxed{\Lambda_P \leq 1000 \text{ TeV}} \quad \text{and} \quad \boxed{\Lambda_A \leq 20 \text{ TeV}},$$

and indirectly, through loop effects to $\boxed{\Lambda_S \leq 60 \text{ TeV}}$.

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In general multi-Higgs models with charged-Higgs couplings

$\lambda_{e\nu} \approx \lambda_{\mu\nu} \approx \lambda_{\tau\nu}$, at 0.1% precision, $R_{e\mu}^\pi$ probes

$$\boxed{m_{H^\pm} \leq 400 \text{ GeV}}.$$



Lepton universality

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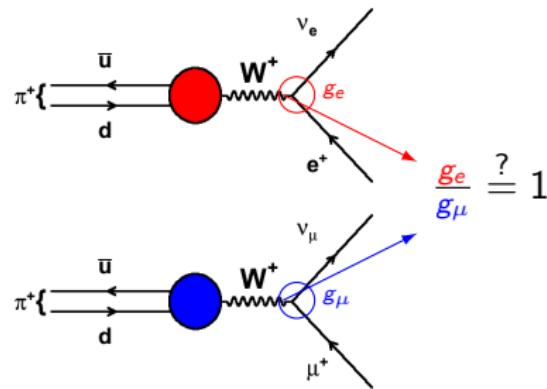
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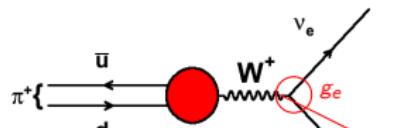
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In SM, e , μ , and τ differ by Higgs
couplings only



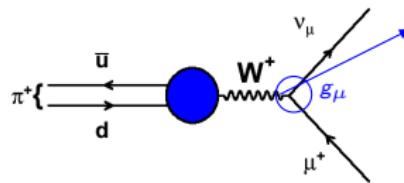
Lepton universality



Redefining $g_I \rightarrow g_I(1 - \frac{\epsilon_I}{2})$

$$\frac{g_i}{g_j} = 1 + \frac{\epsilon_j - \epsilon_i}{2}$$

$$\Delta_{ij} = \epsilon_i - \epsilon_j \quad *$$



Δ_{ij} is constrained by current experimental data

and can be further constrained.

In SM, e , μ , and τ differ by Higgs couplings only

* Will Loinaz, et al. Nutev anomaly, lepton universality, and nonuniversal neutrino-gauge couplings. Phys.Rev. D, 70(11):113004, 2004



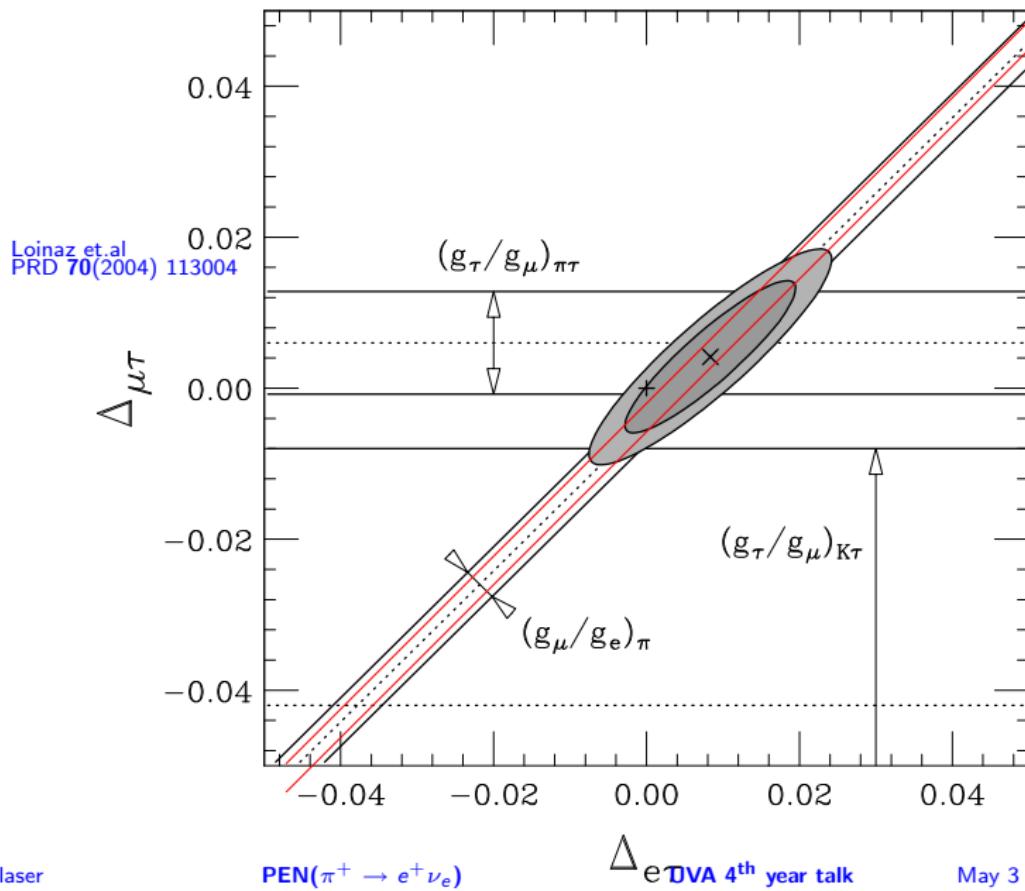
Lepton universality

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Massive Neutrinos

Suppose, $\nu: (\nu_e, \nu_\mu, \nu_\tau, \nu_1, \dots)$

- $\nu_\alpha = \sum U_{\alpha i} \nu_i$
- $\pi \rightarrow e\nu_e = \sum \pi \rightarrow e\nu_i$ (incoherent)
- normally, $\pi \rightarrow e\nu_e$ e has 70 MeV
- with $\pi \rightarrow e\nu_x$ e has < 70 MeV-monoenergetic
- isolated signal below normal peak

relaxes helicity suppression of $\pi \rightarrow e\nu$

$$V - A \sim \frac{\left(1 - \frac{v_e}{c}\right)}{\left(1 - \frac{v_\mu}{c}\right)} \sim \frac{m_e^2}{m_\mu^2}$$



Experiment

Paul Scherrer Institute (PSI) 2008-2010

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Charlie Glaser

PEN($\pi^+ \rightarrow e^+ \nu_e$)

UVA 4th year talk

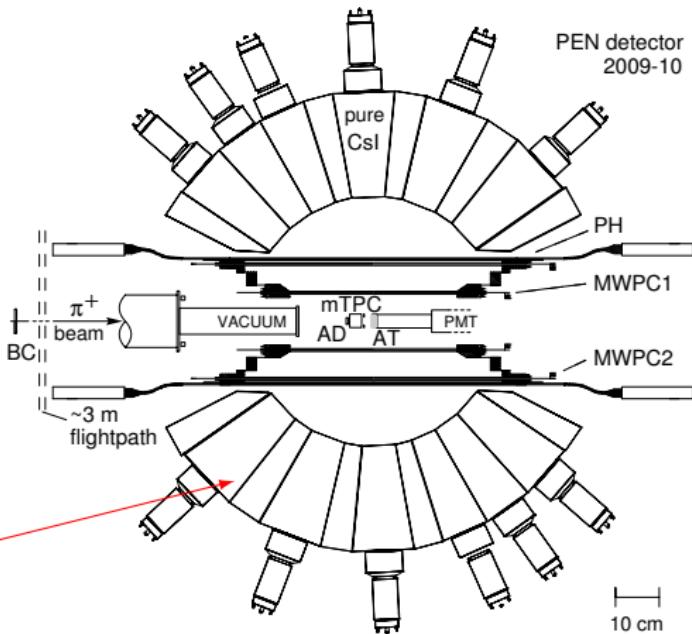
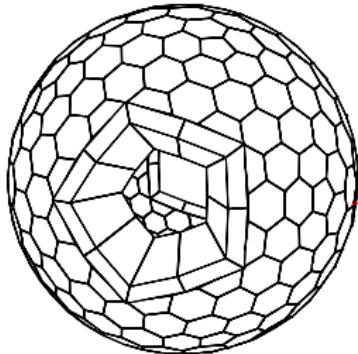
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Detector Setup

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- π^- beamline at PSI
- stopped π^+ beam
- active target counter
- 240 spherical pure CsI calorimeter
- central tracking
- beam tracking
- digitized waveforms



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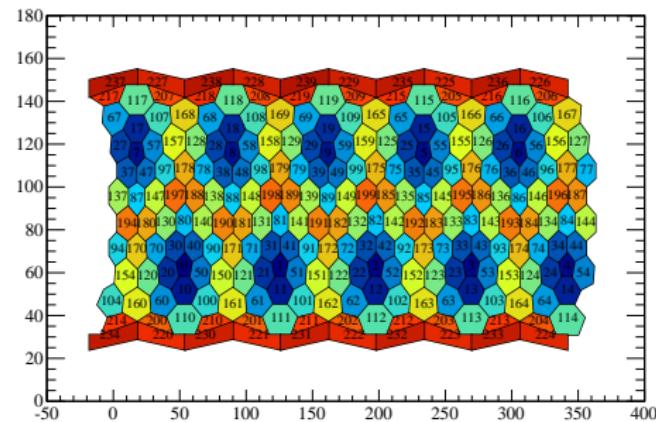
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Mercator Projection of CsI Crystals



Triggers

2 Process for final e:

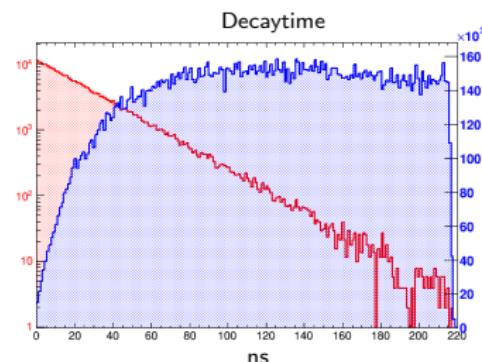
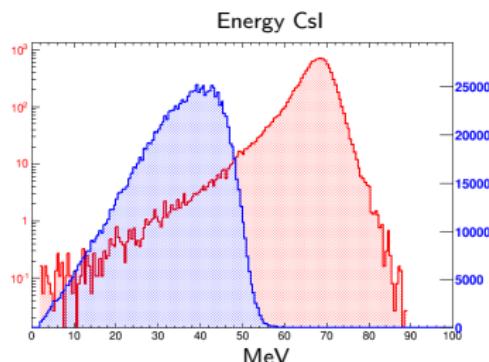
$$\mu \rightarrow e\nu\bar{\nu}$$

$$\pi \rightarrow e\nu$$

$$\tau_\mu = 2.2 \mu s$$

$$\tau_\pi = 26.03 \text{ ns}$$

$$E_{e \text{ max}} = \frac{1}{2} m_\mu = 52.5 \text{ MeV} \quad E_{e \text{ max}} = \frac{1}{2} m_\pi = 69.5 \text{ MeV}$$



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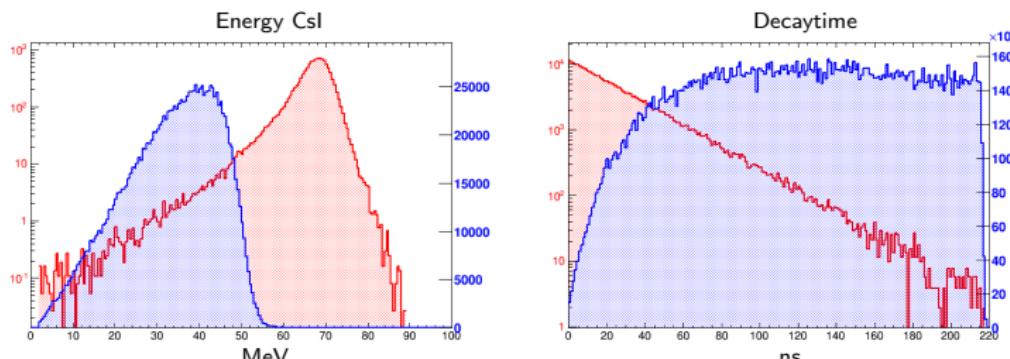
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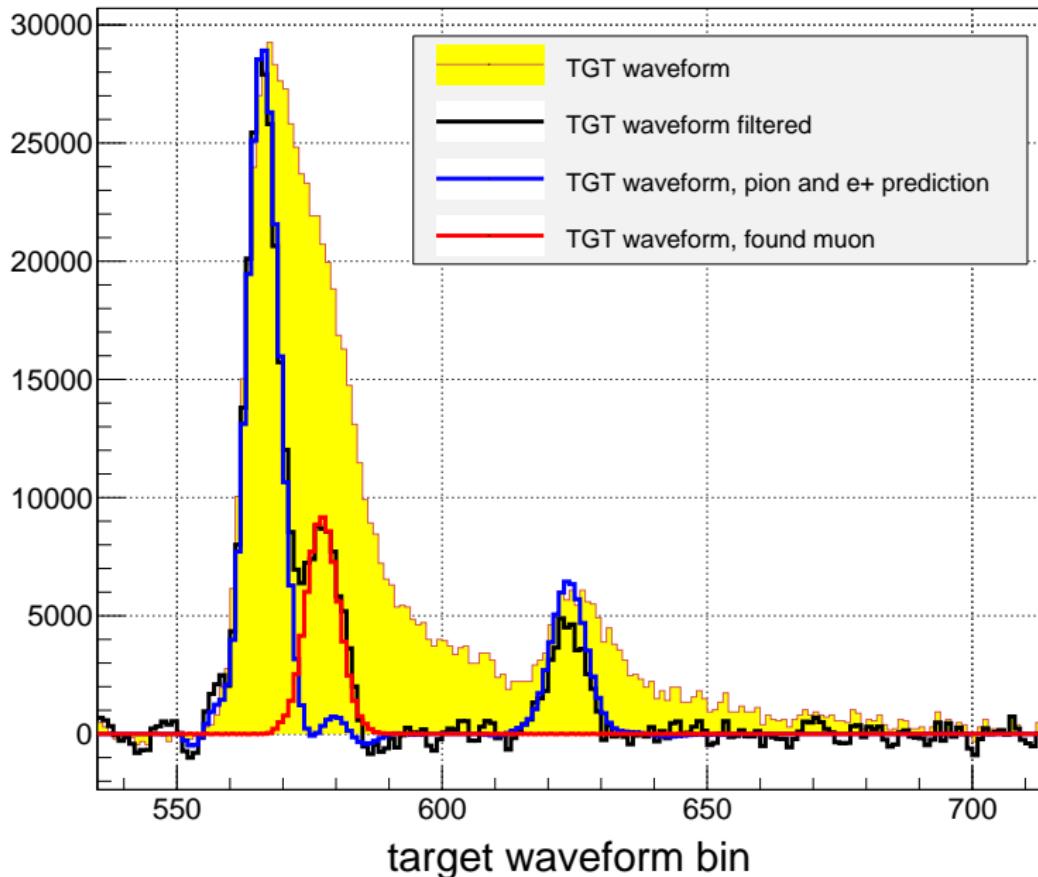
e^+ within 250 ns of the stopping time
anything above 48 MeV is recorded
if below 48 MeV, prescaled by 64



A closer look at waveforms

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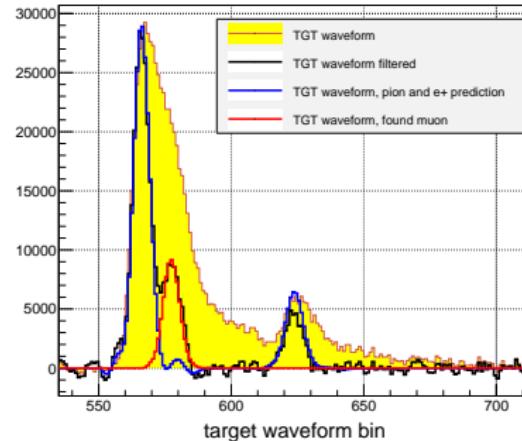
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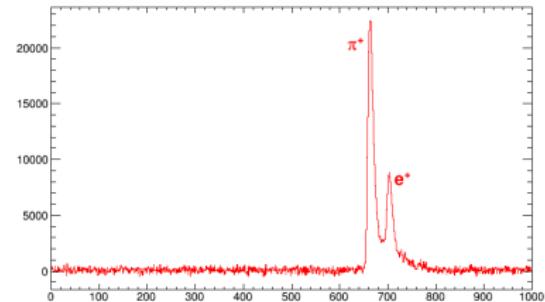
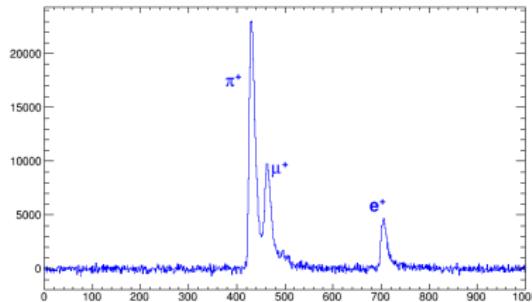
2 GS/s digitized waveforms
predicted π energy and time



MWPC 250 Ms/s TPC digitizer
PH predict e^+ energy and time

μ found

no μ found



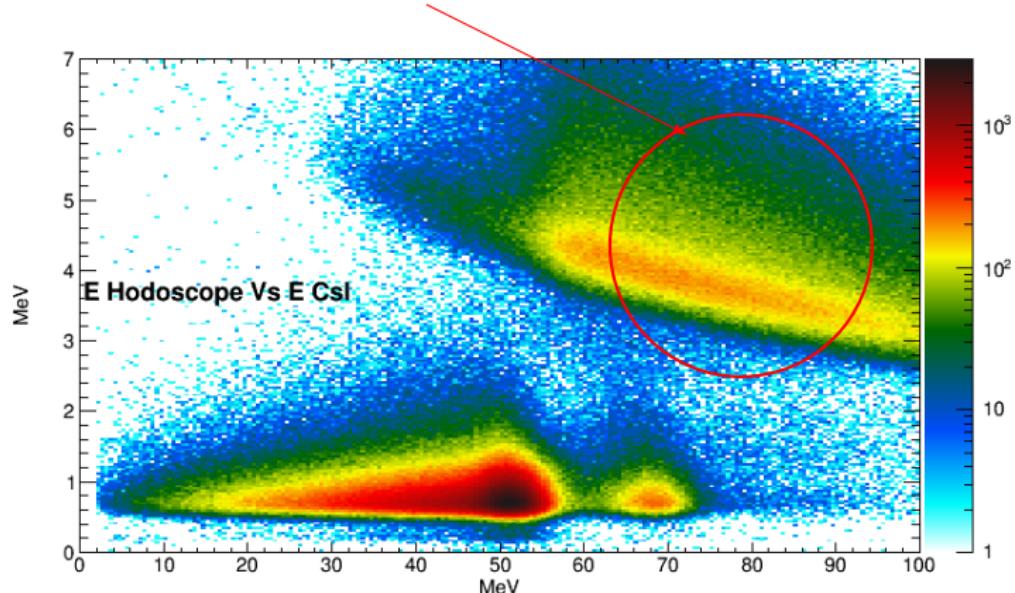
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π absorption produces **protons** through hadronic interactions



Experimental Branching Ratio

Branching ratio =

$$\frac{\text{Number of } \pi \rightarrow e\nu \text{ Events}}{\text{Number of } \pi \rightarrow \mu\nu \text{ Events}}$$

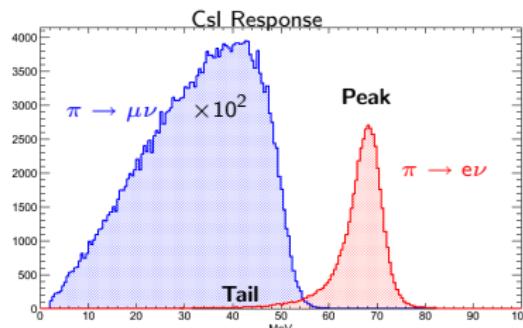
Rate($\pi^+ \rightarrow e^+ \nu_e$) =

$$\frac{N_{\text{Tail}} + N_{\text{Peak}}}{A_e N_\pi}$$

Rate($\pi^+ \rightarrow \mu^+ \nu_\mu \rightarrow e^+ \nu_e \bar{\nu}_\mu$) =

$$\frac{N_\mu}{A_\mu N_\pi}$$

$$\frac{\text{Rate}(\pi^+ \rightarrow e^+ \nu_e)}{\text{Rate}(\pi^+ \rightarrow \mu^+ \nu_\mu \rightarrow e^+ \nu_e \bar{\nu}_\mu)} = \frac{N_{\text{Peak}} \left(1 + \frac{N_{\text{Tail}}}{N_{\text{Peak}}} \right) A_\mu}{N_\mu A_e}$$



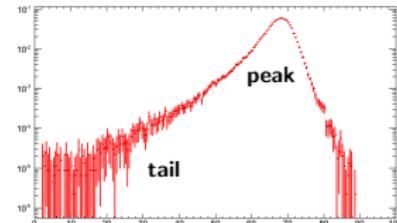
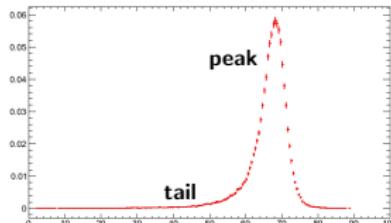
A = Acceptances



Geant4 Monte Carlo Simulation

- particle tracking
- energy deposition
- decaying particles
- acceptances by studying **pure processes**

CsI Response $\pi \rightarrow e\nu$



Will give us $\frac{N_{\text{tail}}}{N_{\text{peak}}}$



Problems

Geant gives energies and timings and positions
does not simulate full detector response

In the Experiment:

- digitized energies and timings
- signals/waveforms
- photoelectron statistics smear signal

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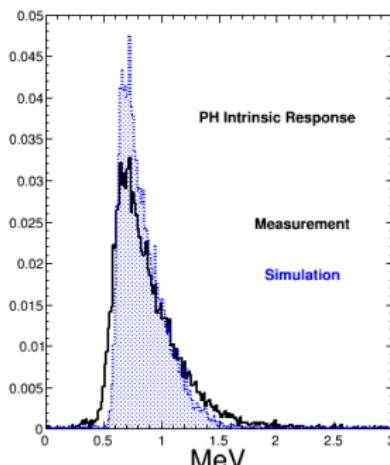


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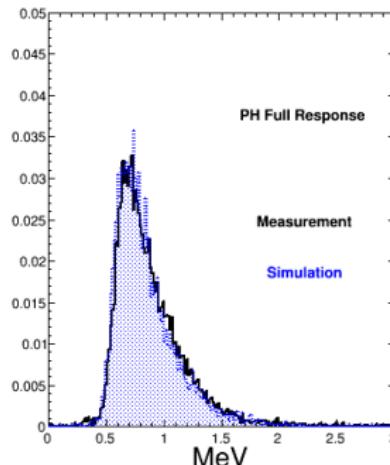
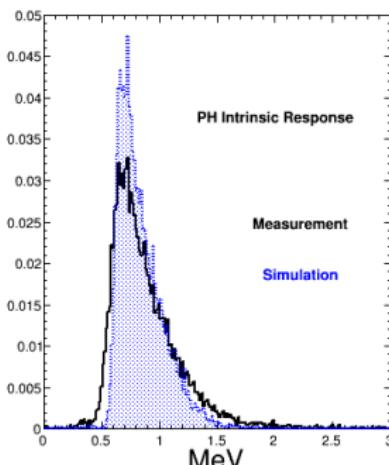


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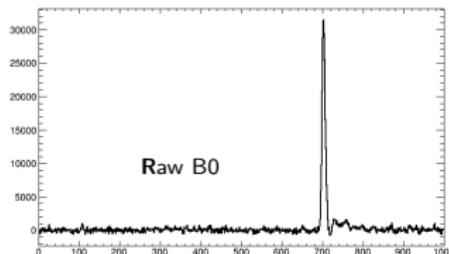
Full detector responses that are simulated :

- waveform digitizer with beam counters (B0, DEG, TGT)
- mini-time projection chamber (mTPC)
- multi-wire proportional chamber (MWPC)
- plastic hodoscope (PH)
- CsI calorimeter



Waveform digitizer

- beam counter, degrader, target



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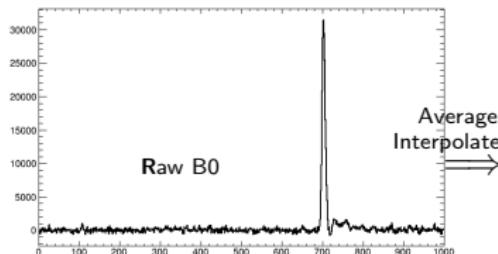
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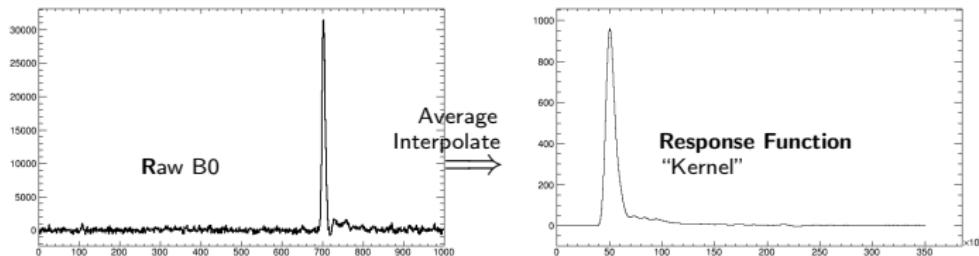
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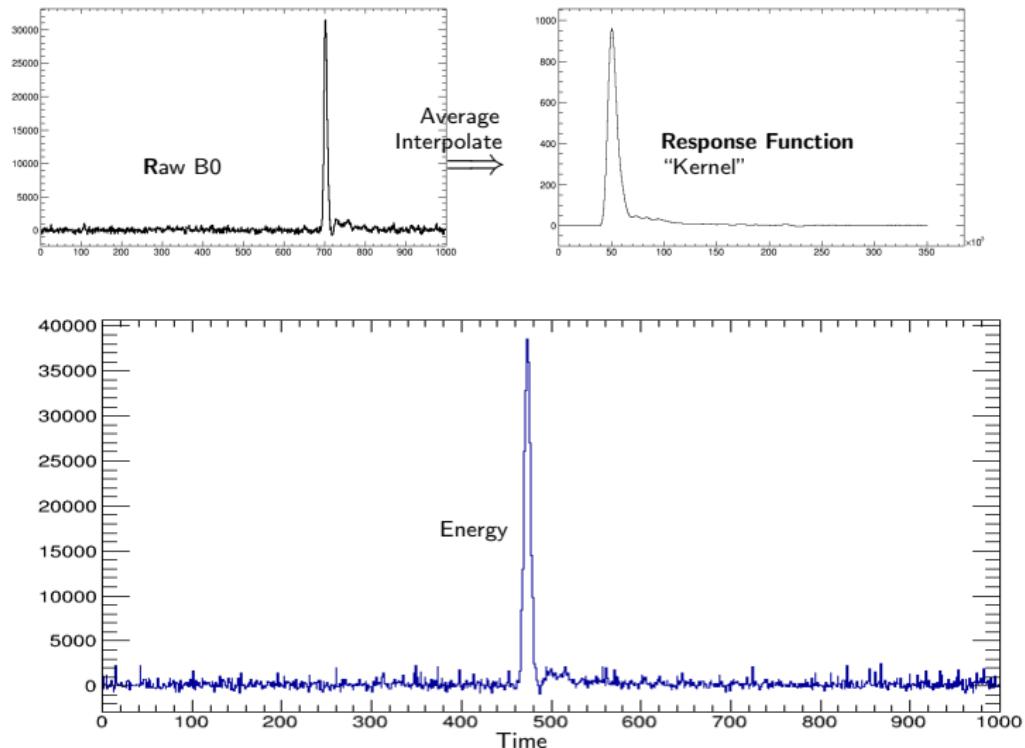
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Not that simple!

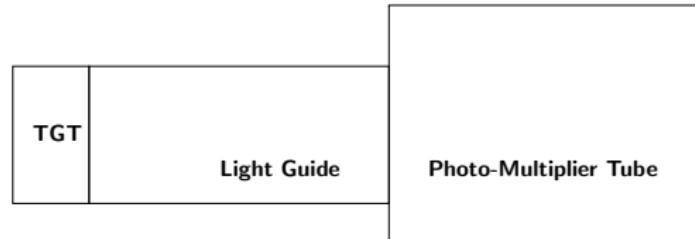
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The “energy” - deduced from number of photoelectrons



Not that simple!

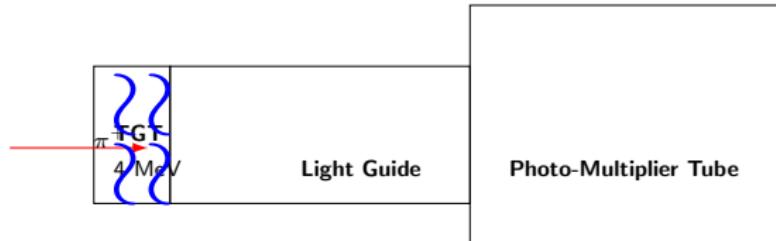
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CsI

The “energy” - deduced from number of photoelectrons



Not that simple!

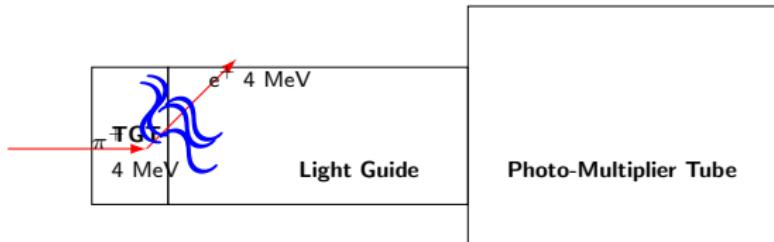
Basic Theory

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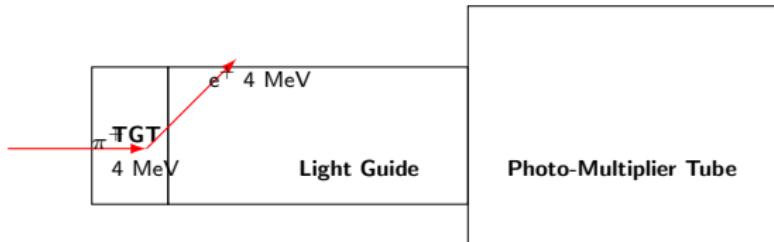
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Is the light output the same?



Not that simple!

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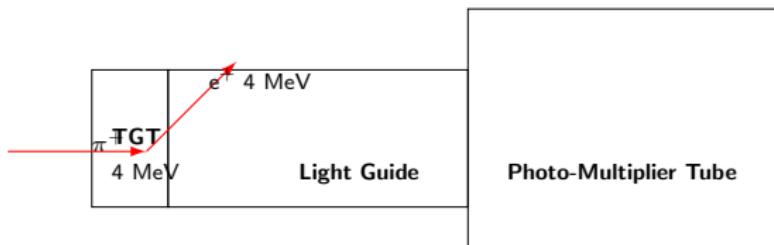
Digitizer

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The “energy” - deduced from number of photoelectrons



Is the light output the same?

NO!



To the Literature!

The light intensity $\propto E_{\text{deposited}}$ for $E_e > 100$ keV
heavy particles- nonlinear response! ie $\not\propto E$

$$\alpha = 0.025 \pm 0.002 \text{ g cm}^{-2} \text{MeV}^{-1} *$$

$$E_{ee} = \frac{(dE/dx)_{\min}}{\ln [1 + \alpha(dE/dx)_{\min}]} \int_0^L \ln [1 + \alpha(dE/dx)_p] dx$$

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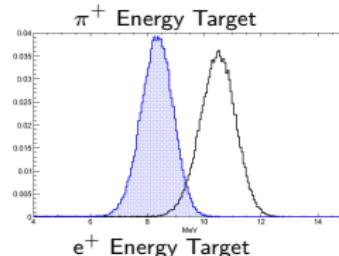
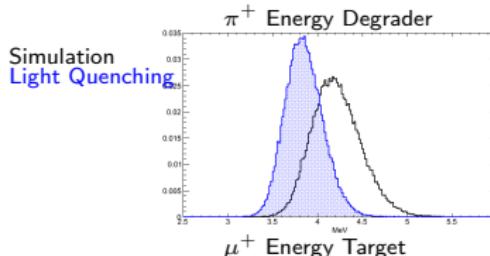


To the Literature!

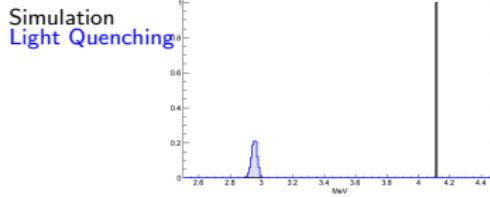
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Simulation Light Quenching



Simulation Light Quenching

* G. V. O'Reilly, N.R. Kolb, R.E. Pywell, NIM A (1996)

PEN($\pi^+ \rightarrow e^+ \nu_e$)



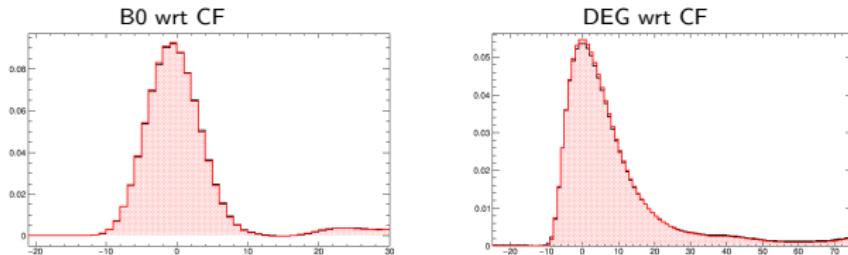
Beam counters

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measurement
simulation



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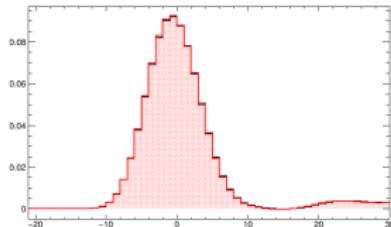
Digitizer

MWPC

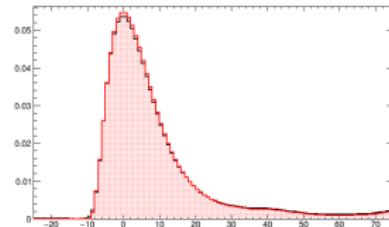
mTPC

CsI

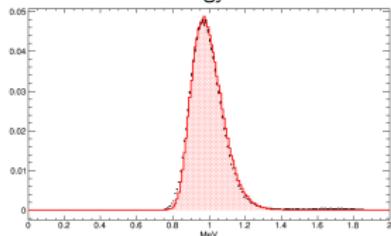
B0 wrt CF



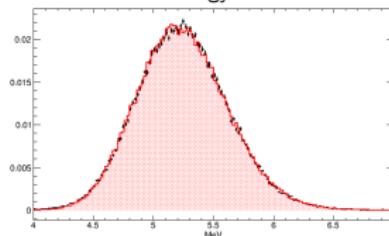
DEG wrt CF



π^+ energy in B0



π^+ energy in DEG



measurement
simulation



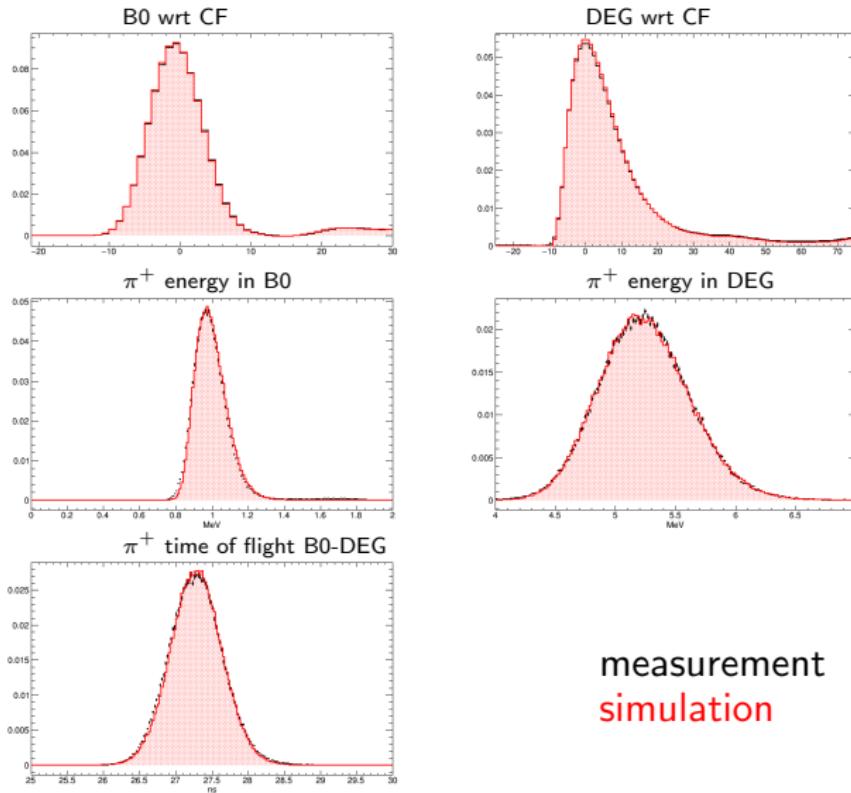
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measurement
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Raw tgt response:

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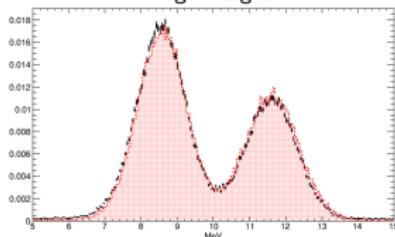
MWPC

mTPC

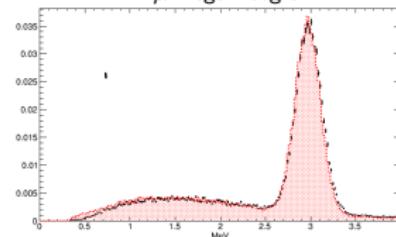
CsI

measurement
simulation

π^+ tgt integral

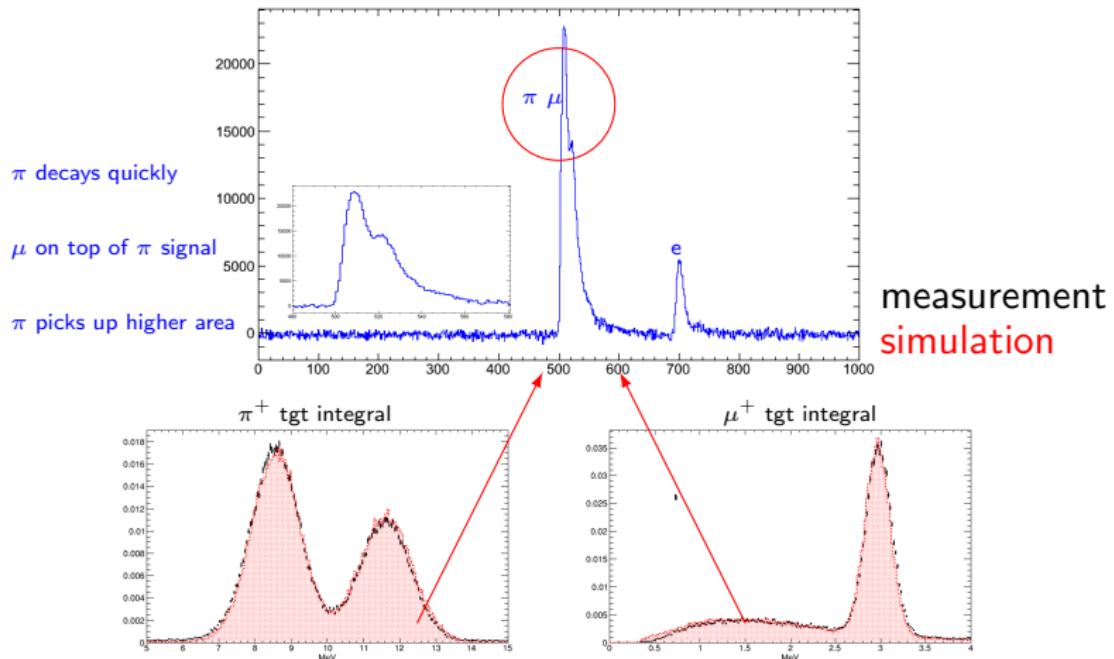


μ^+ tgt integral



Raw tgt response:

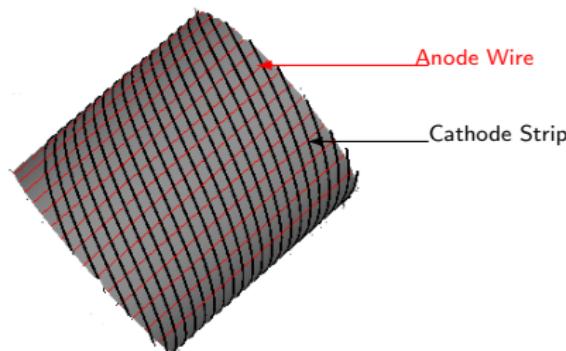
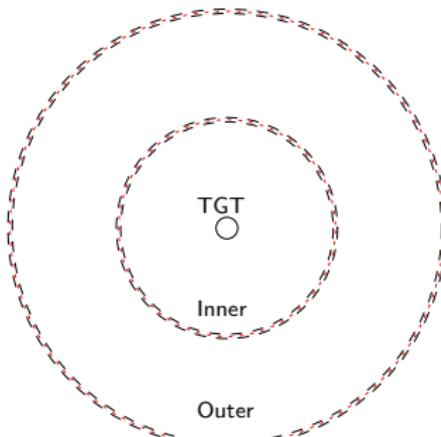
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Multi-Wire Proportional Chamber (MWPC)

Decay Particle Tracking

- Inner Chamber
 - 192 Anode Wires
 - 256 Cathode Strips
- Outer Chamber
 - 384 Anode Wires
 - 384 Cathode Strips



$$\text{PEN}(\pi^+ \rightarrow e^+ \nu_e)$$



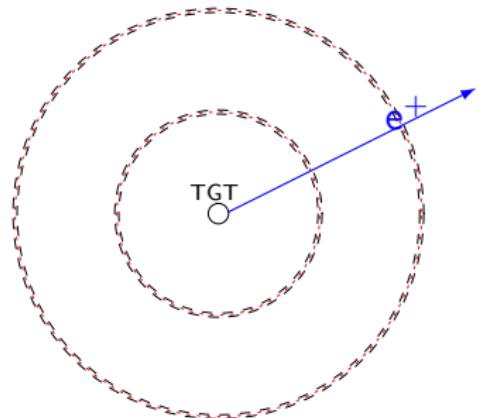
Multi-Wire Proportional Chamber (MWPC)

e^+ approaches chamber

ion pairs are formed

drawn toward the anode

induced charge on neighboring
cathodes



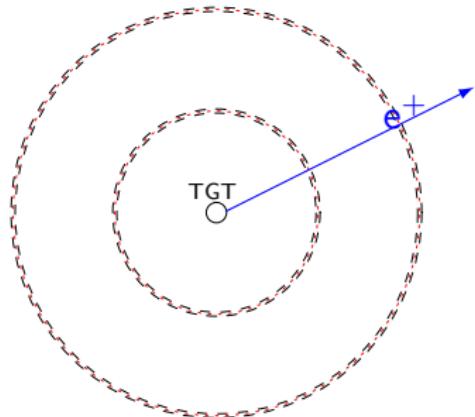
Multi-Wire Proportional Chamber (MWPC)

e^+ approaches chamber

ion pairs are formed

drawn toward the anode

induced charge on neighboring
cathodes



the wire fired gives us ϕ ie (x,y)

the strips fired gives us z

Problem: How much charge is induced on cathode strips?



Multi-Wire Proportional Chamber (MWPC)

It has been shown E. Mathieson NIM 270 (1988)

$$\frac{\rho(\lambda)}{q_a} = K_1 \frac{1 - \tanh^2(K_2 \lambda)}{1 + K_3 \tanh^2(K_2 \lambda)} \quad \text{where } K_1 = \frac{K_2 \sqrt{K_3}}{4 \arctan(\sqrt{K_3})}$$
$$\text{and } K_2 = \frac{\pi}{2} \left(1 - \frac{\sqrt{K_3}}{2} \right)$$

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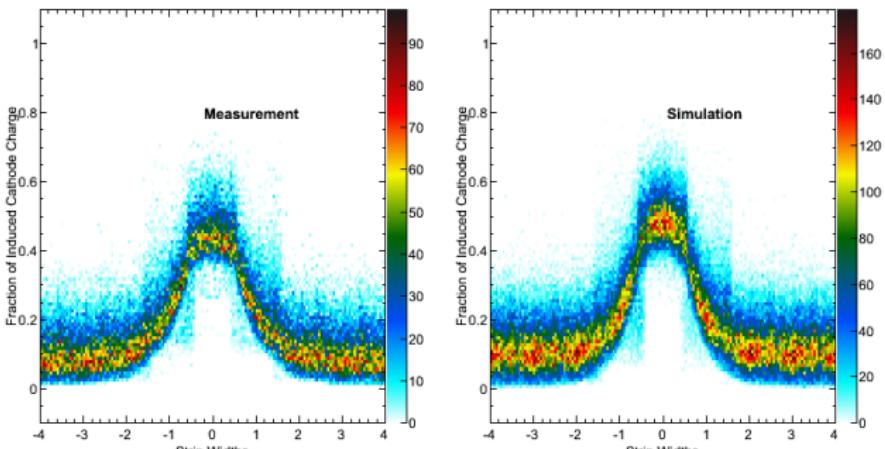
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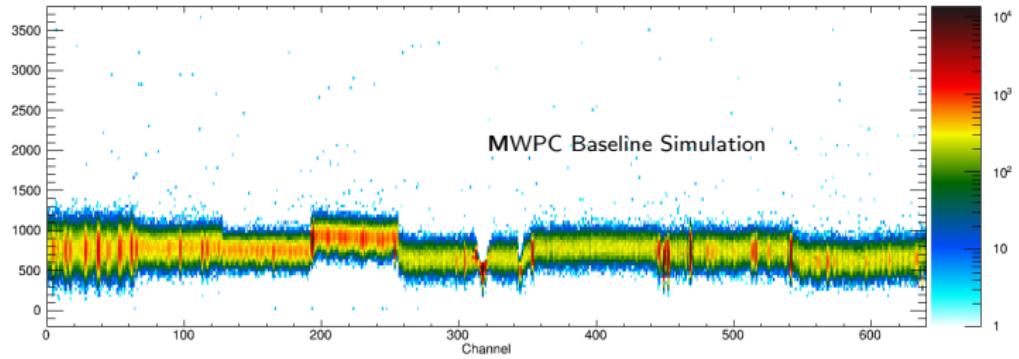
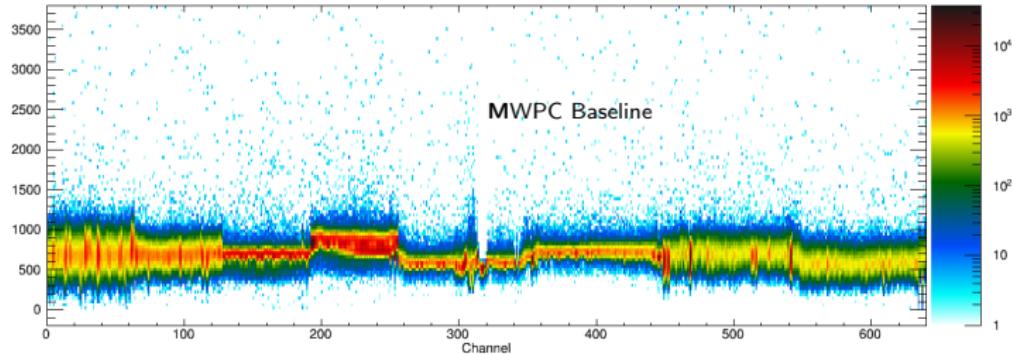
Anode-Cathode separation $\frac{z}{\text{Anode Charge}}$

$$\text{and } K_2 = \frac{\pi}{2} \left(1 - \frac{\sqrt{K_3}}{2} \right)$$



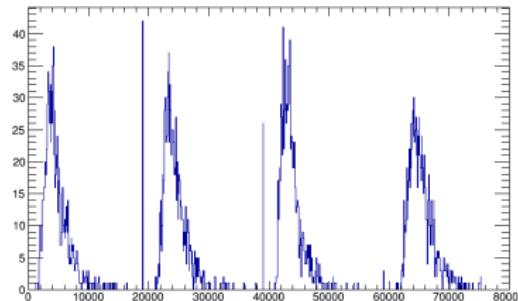
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Wire Chamber + Drift Chamber

- beam tracking
- π produces ion pairs
- charges drawn to wires
- charge collected related to energy deposited
- relative charge on each pair of wires determines 1 coordinate
- drift time determines the other coordinate
- output is digitized signal

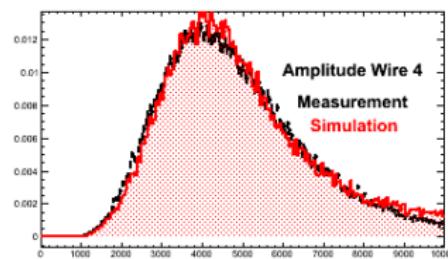
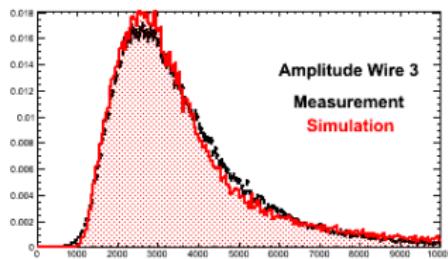
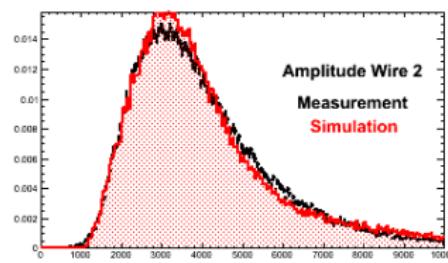
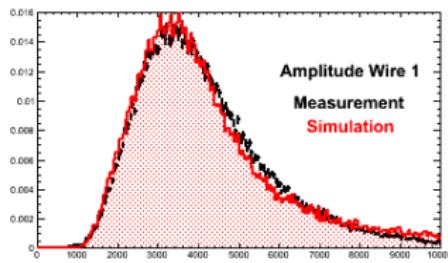


- response function
- place according to drift time (y-coordinate)
- scale according to energy and x-coordinate

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Top: Known x (geant) vs reconstructed x (waveforms)
Bottom: Known y (geant) vs reconstructed y (waveforms)

Basic Theory

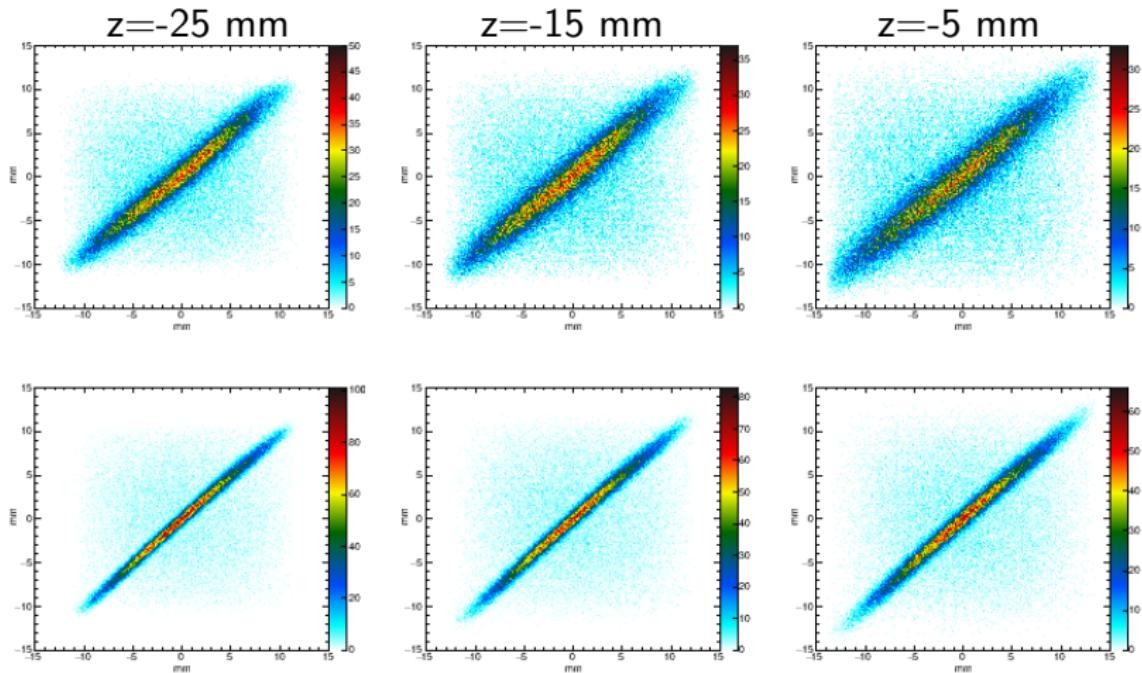
Lepton Universality

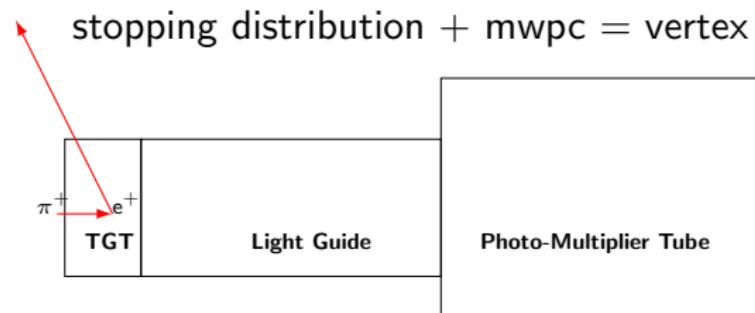
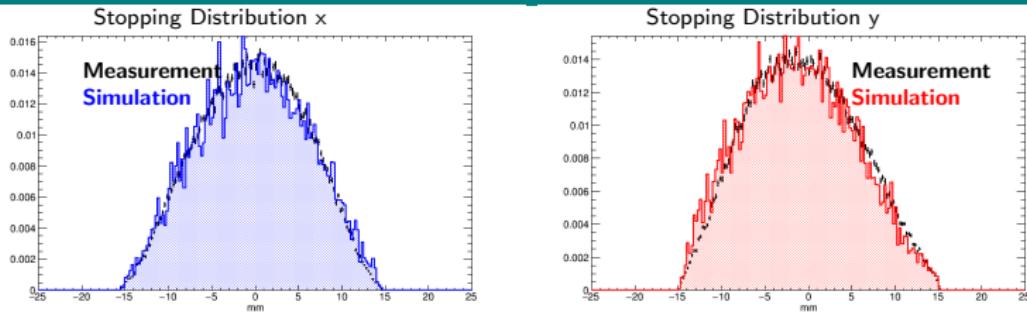
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Vertex allows for predicted e^+ energy \Rightarrow
Prediction in TGT waveform



CsI EM Calorimeter

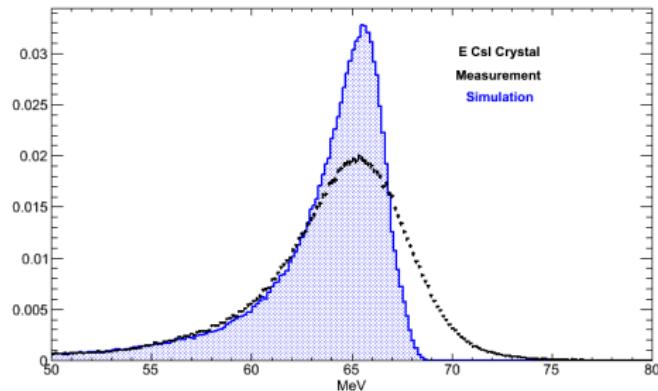
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Consider $\pi \rightarrow e\nu$



CsI EM Calorimeter

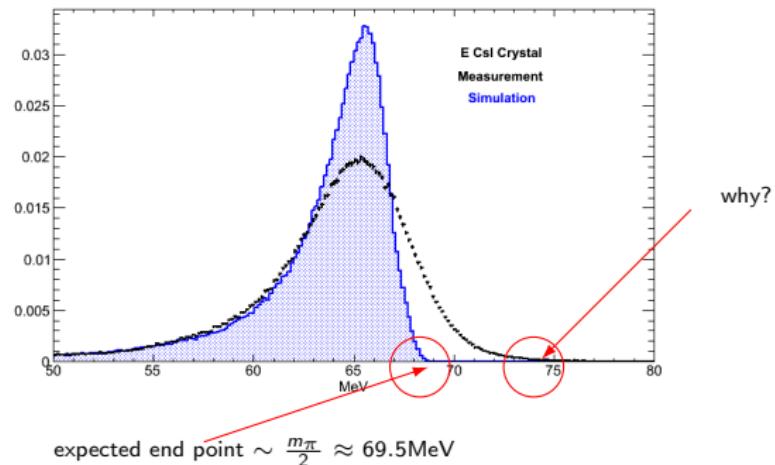
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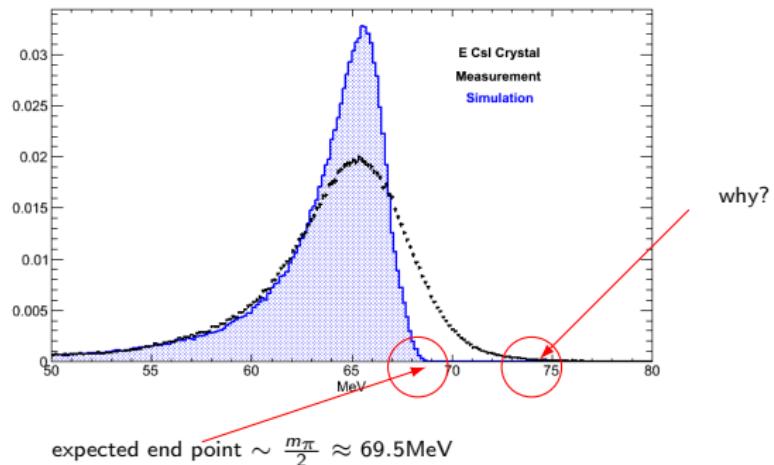
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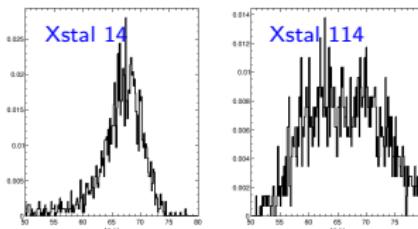
CsI EM Calorimeter

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Consider $\pi \rightarrow e\nu$



1. Crystals are not all the same



$$\text{PEN}(\pi^+ \rightarrow e^+ \nu_e)$$

UVA 4th year talk

May 3 2016 32 / 42



Charlie Glaser

CsI EM Calorimeter

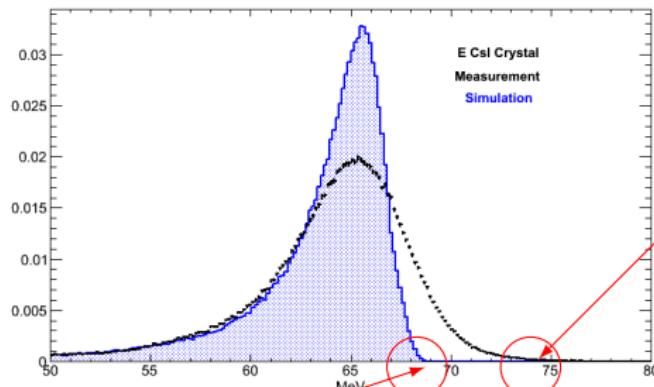
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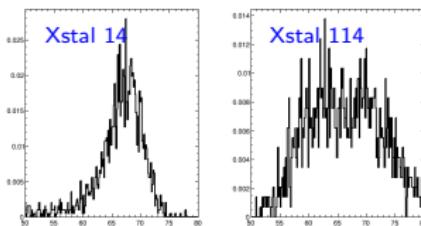
Consider $\pi \rightarrow e\nu$



why?

$$\text{expected end point} \sim \frac{m_\pi}{2} \approx 69.5 \text{ MeV}$$

1. Crystals are not all the same



$$\text{PEN}(\pi^+ \rightarrow e^+ \nu_e)$$

2. Photoelectron statistics

- shower \rightarrow photons
- photons \rightarrow PMT
- PMT \rightarrow photoelectrons
- photoelectrons \rightarrow signal



Photoelectron Statistics?

It has been shown that the number of photoelectrons produced is a Poisson distribution assuming: *

1. $P(1, t, dt + t) \propto \gamma I(t)$
2. dt can be chosen very small
3. P does not change based off previous events occurring.

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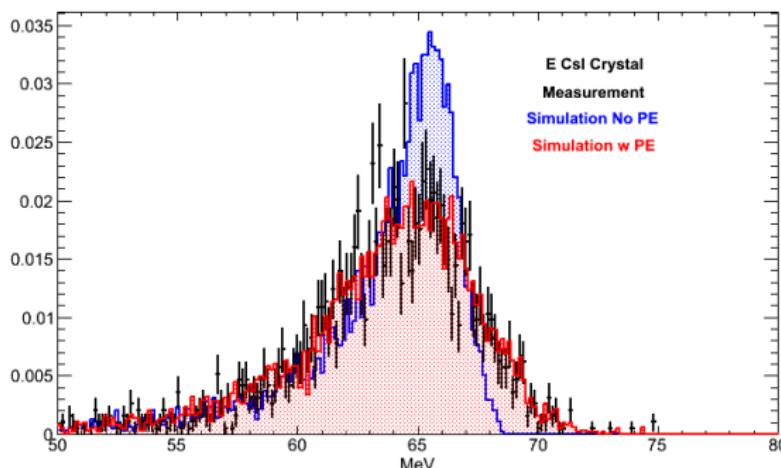
CsI



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* L. Mandel, Procs. Phys. Soc. (London) **74** 233 (1959)



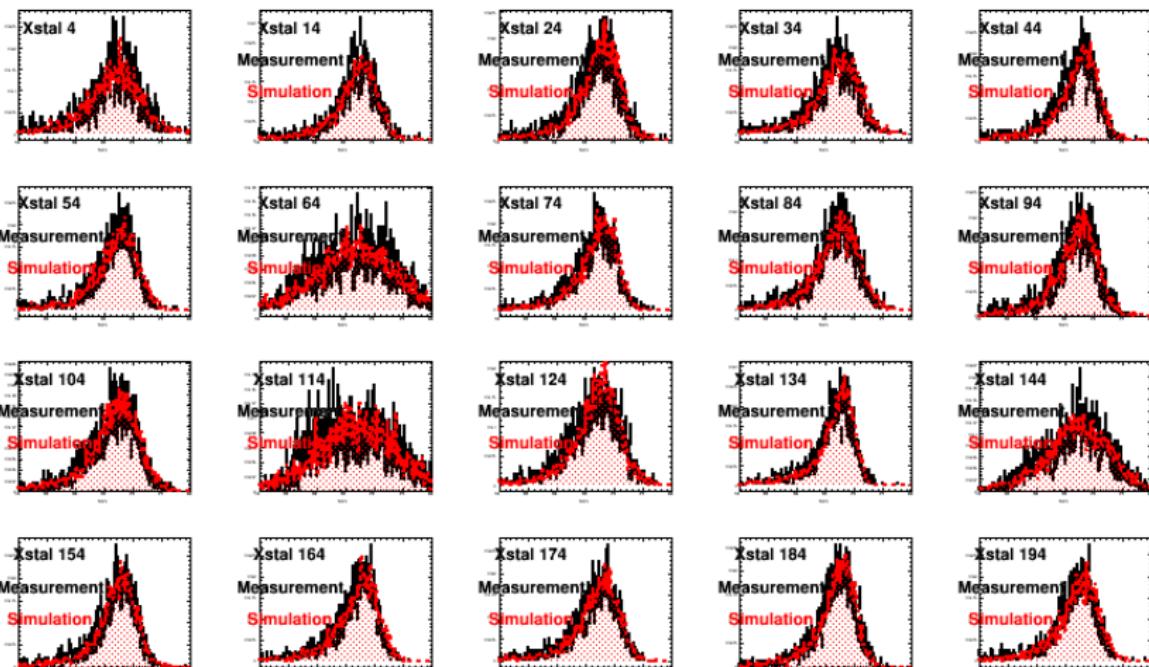
Do this to all 240 Crystals

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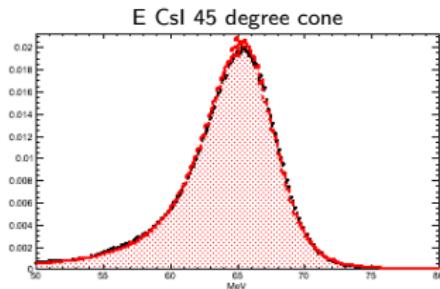
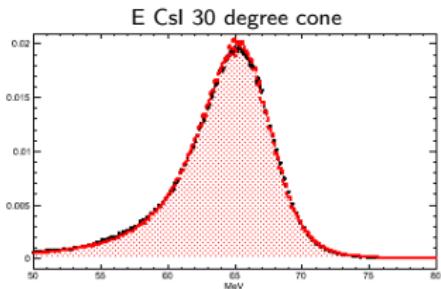
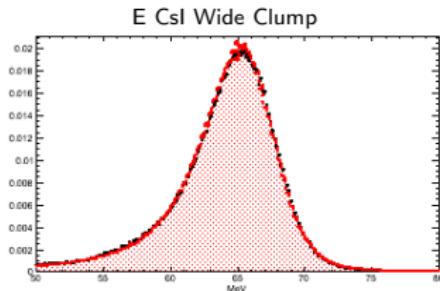
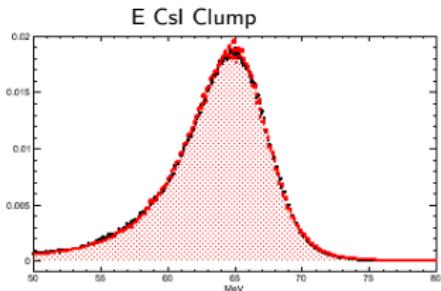
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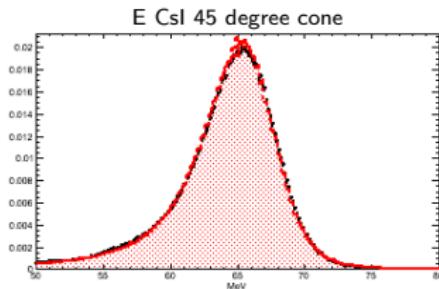
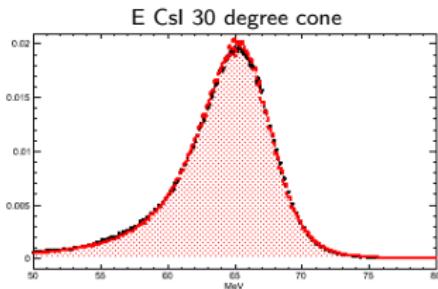
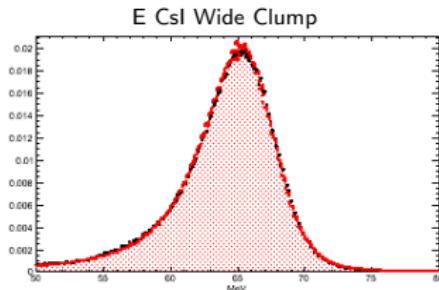
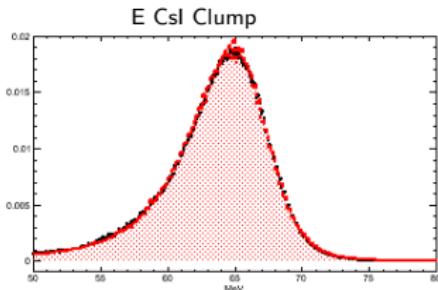
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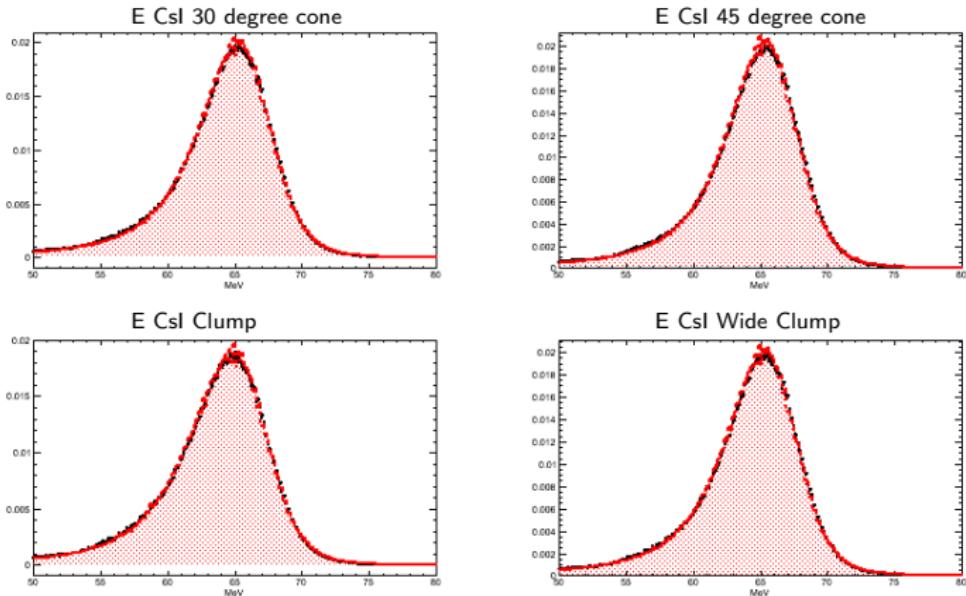
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If all is good above 50 MeV, the tail should follow:



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If all is good above 50 MeV, the **tail** should follow:

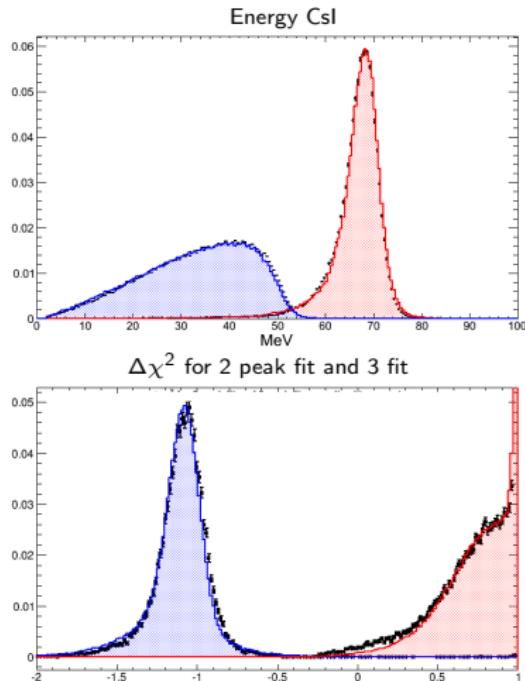
tail-to-peak ratio may be obtained



When all is said and done

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Measurement
 $\pi \rightarrow e\nu$ Simulation
 $\pi \rightarrow \mu\nu$ Simulation



If All this Works...

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Then

- get acceptances
- study false positive signals
- get tail-to-peak ratio
- get branching ratio
- put limits on beyond Standard Model physics



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- obtaining tail-to-peak ratio
 - Issue: Giant Dipole Resonances of ^{127}I
- mwpc efficiencies
 - Issue: Based on “seen” energy
- positron lineshape
 - aids in search of massive ν 's



Current and former PIBETA and PEN collaborators

L. P. Alonzi **K. Assamagan**, V. A. Baranov , W. Bertl ,
C. Broennimann , **S. Bruch** , M. Bychkov , Yu.M. Bystritsky ,
M. Daum , T. Fl "ugel , E. Frlež , C. Glaser, **R. Frosch**, **K. Keeter**,
V.A. Kalinnikov , N.V. Khomutov , **J. Koglin** , A.S. Korenchenko ,
S.M. Korenchenko , M. Korolija , T. Kozlowski, N.P. Kravchuk ,
N.A. Kuchinsky, D. Lawrence , M. Lehman, **W. Li** , **J. S. McCarthy** ,
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P. L. Slocum , **L. C. Smith** , **N. Soić RB**, U. Straumann , I. Supek ,
P. Truöl , Z. Tsamalaidze , A. van der Schaaf *, E.P. Velicheva , M.
Vitz, V.P. Volnykh, **Y. Wang** , **C. Wigger** , **H.-P. Wirtz** , **K. Ziock** .

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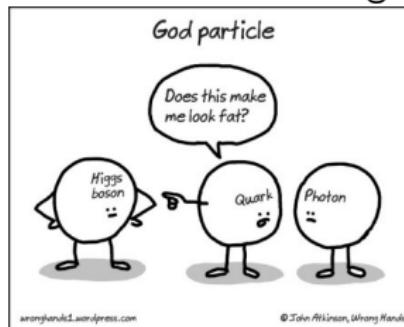
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Thanks For Listening!



References

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3. G. V. O'Reilly, N.R. Kolb, R.E. Pywell, Nucl. Instr. and Meth. in Res. A 368(1996)745-749
4. L. Mandel, "Fluctuations of photon beams: the distribution of photo-electrons", Procs. Phys. Soc. (London) **74** 233 243 (1959)



Minimal Supersymmetric Standard Model

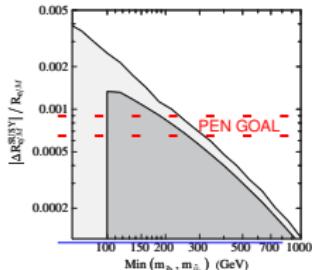
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Lepton Universality
Massive Neutrinos

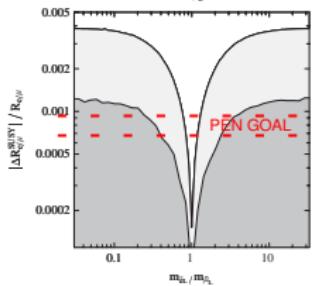
Experiment

Geant4
Simulation
Digitizer
MWPC
mTPC
CsI

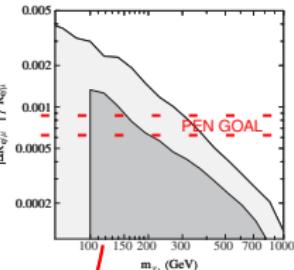
minimal
selec-
tron,
smuon
masses:



slepton
mass
degen-
eracy:



lowest
mass
chargino:



Higgsino
mass
param.s.
 μ , $m_{\tilde{t}_L}$:

