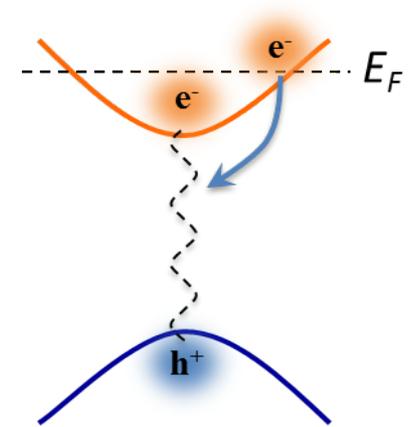
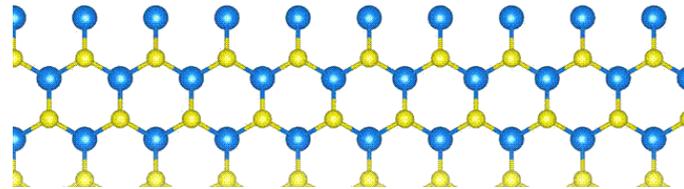
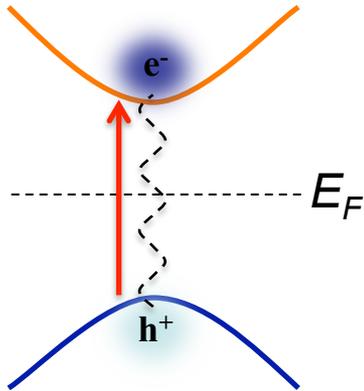
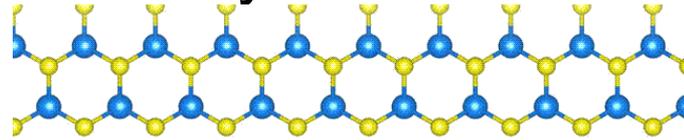


# Tailoring properties of 2D transition metal dichalcogenides: looking beyond graphene

Talat S Rahman,  
University of Central Florida



Physics Colloquium, University of Virginia, February 12, 2016



# PHYSICS

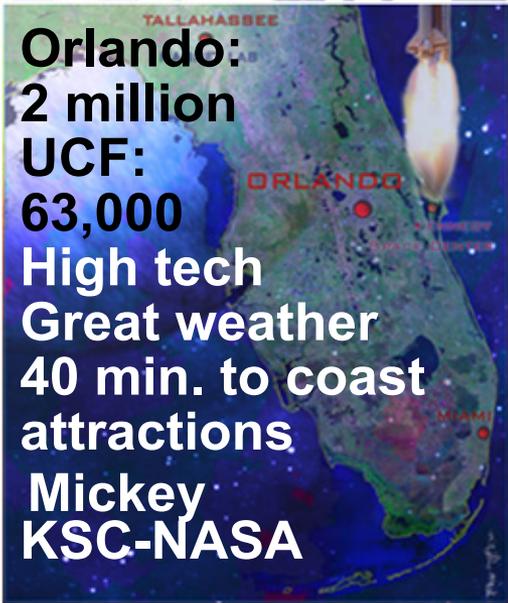
ORLANDO - FLORIDA

UCF

**45 Faculty and 20 affiliated faculty**  
**~100 Graduate Students**  
**~200 Physics Majors**

## UCF-LIFE

**Orlando:**  
**2 million**  
**UCF:**  
**63,000**  
**High tech**  
**Great weather**  
**40 min. to coast**  
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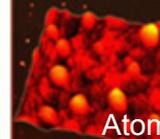
**Prof. Helge Heinrich**  
**physics@ucf.edu**

## RESEARCH

### ASTRONOMY

Planetary Science  
How do other planets form?  
**Comet impact**  
Are we alone?

### CONDENSED MATTER



Semiconductors  
Quantum computation  
**Surface science**  
Nanomagnetism  
Atomic vibrational dynamics

### BIOPHYSICS

Self-organized polymers  
**Biomolecular Fluorescence**  
Nanoparticle Drug Delivery  
Protein folding  
Microraman spectroscopy

### NANOSCIENCE

Quantum dots  
**Single-electron transistors**  
Nanocatalysis/fuel cells  
Single-molecule magnets  
Graphene and CNTs

### OTHER AREAS

AMO physics  
Physics education  
High energy physics  
Mathematical physics  
**materials science**



# Two other programs of interest

- Comprehensive PhysTEC Site
- APS Bridge Program Site

Both are funded by the American Physical Society and UCF

# Acknowledgements



**Duy The Le**  
**Alfredo Ramirez**  
**Volodymyr Turkowski**  
**Maral Aminpour**  
**Marisol Alcantara Ortigoza**  
**Sampyo Hong**

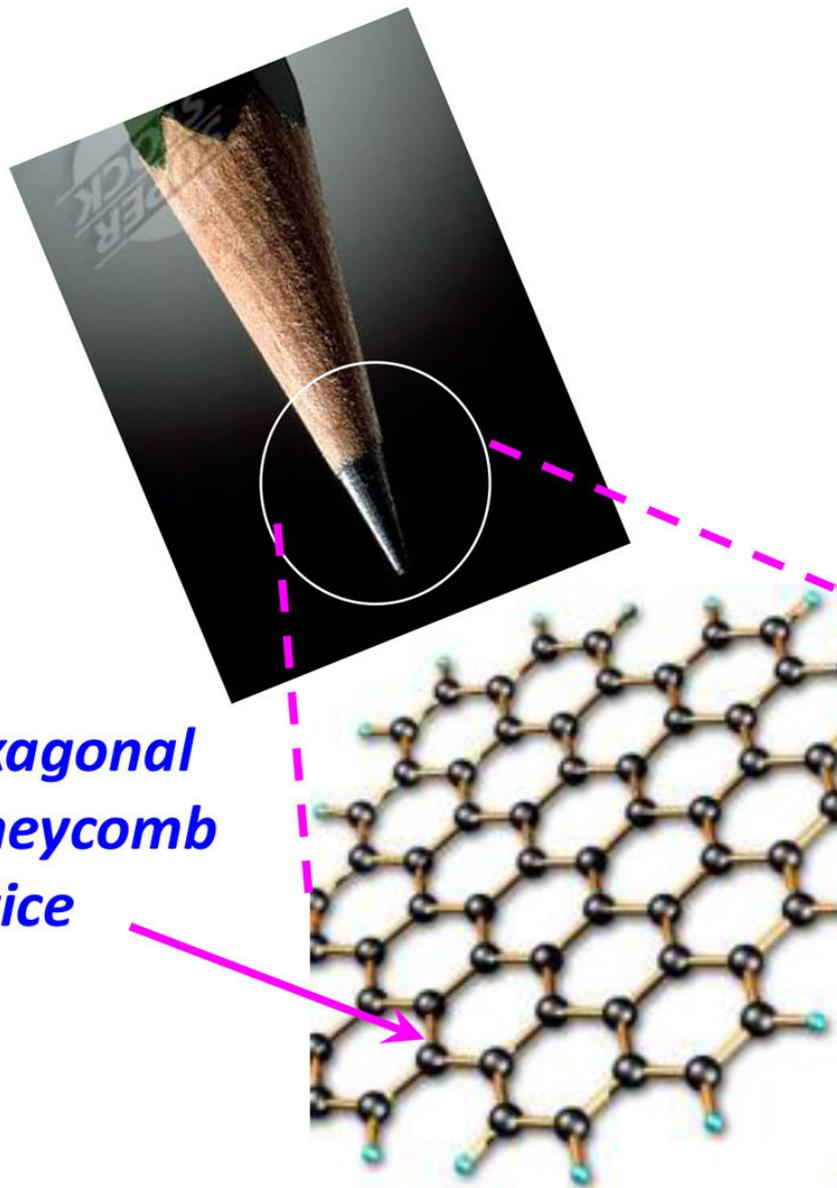
**DOE**  
**NSF**  
**UCF**

**Alamgir Kabir**  
**Islamuddin Shah**  
**Takat Rawal**  
**Neha Nayyar**  
**Ghazal Shafai**  
**Shree Ram Acharya**

**Ludwig Bartels**  
**Tony Heinz**  
**Donna Chen**  
**Pavel Jelinek**  
**Peter Dowben**



# Could a pencil revolutionize science?



*Hexagonal  
honeycomb  
lattice*

# Lots of atomically thin materials

Group →	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
↓ Period																		
1	1 H																	2 He
2	3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne
3	11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
4	19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
5	37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
6	55 Cs	56 Ba		72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
7	87 Fr	88 Ra		104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Uut	114 Uuq	115 Uup	116 Uuh	117 Uus	118 Uuo
Lanthanides	57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu			
Actinides	89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr			

Transition-metal chalcogenides

- Topological insulators
- Semiconductors
- Anomalous semiconductors
- Semimetals (CDW)
- Bismuth selenide telluride
- Metals (CDW, superconductivity)

# Outline

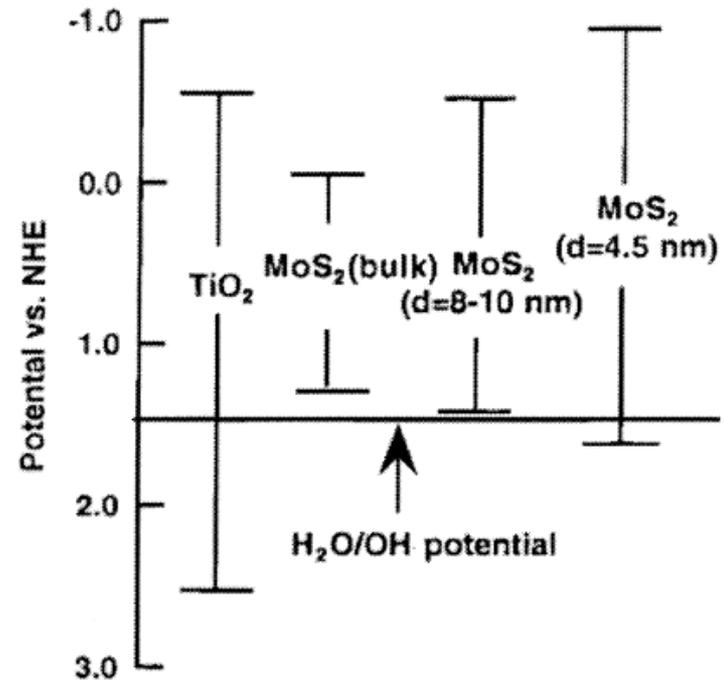
- Motivation
- **Growth** of single-layer MoS<sub>2</sub> is nontrivial  
Moiré Patterns on fcc(111)
- **Joint edges** of SL MoS<sub>2</sub>: 1-D magnetism?
- Controlling properties through **defects**  
**Band gap engineering**: vacancy, doping
- **Manipulation** of chemical properties  
defect-laden MoS<sub>2</sub>, on Cu(111),  
MoS<sub>2</sub>- supported Ag/Cu/Au Nanoparticles
- Enhanced Coulomb interaction  
**Excitons & Trions**
- Concluding Remarks

# Bulk MoS<sub>2</sub>: already in much use

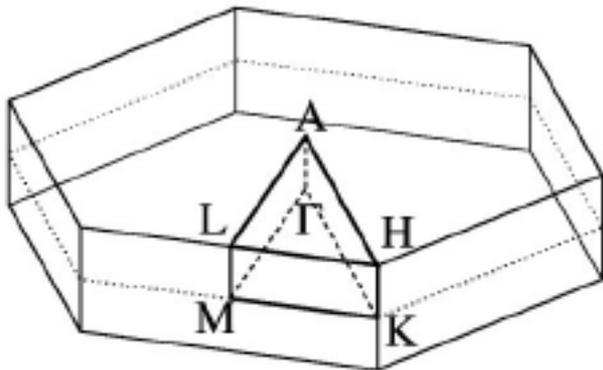
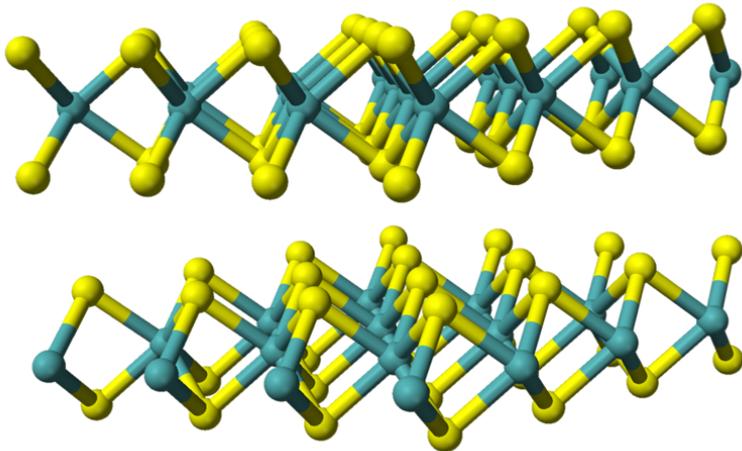
## Lubricants



## Catalysis/photocatalysis

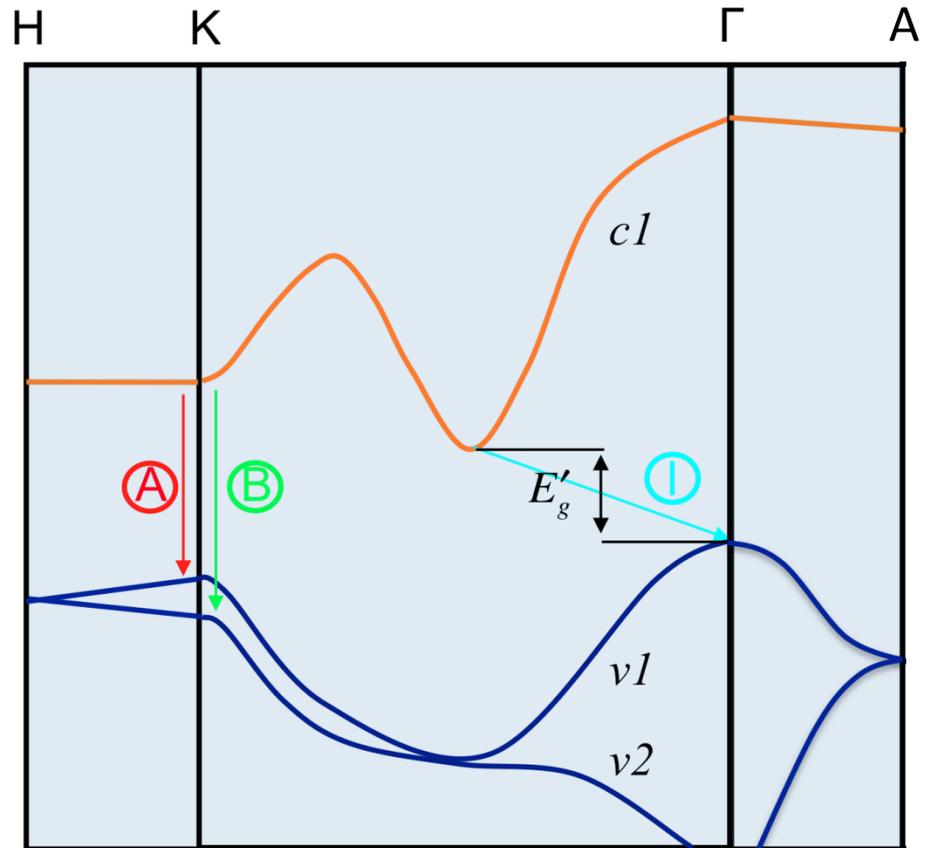


# Bulk MoS<sub>2</sub>: band structure

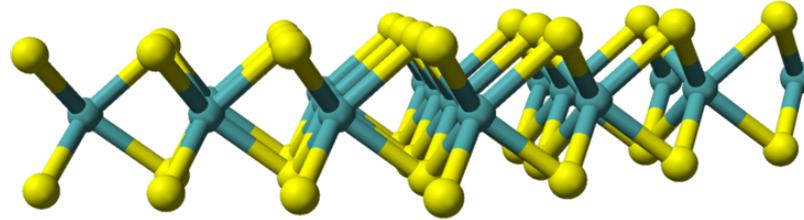


Indirect gap semiconductor

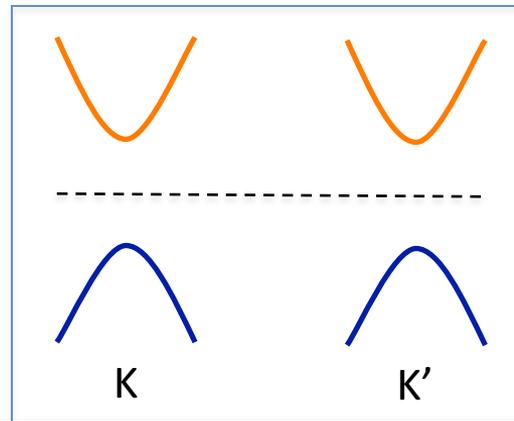
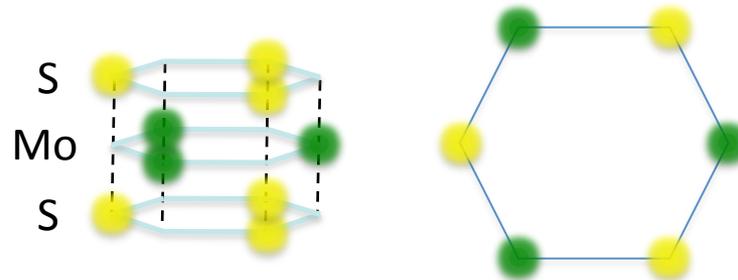
Negligible PL quantum yield



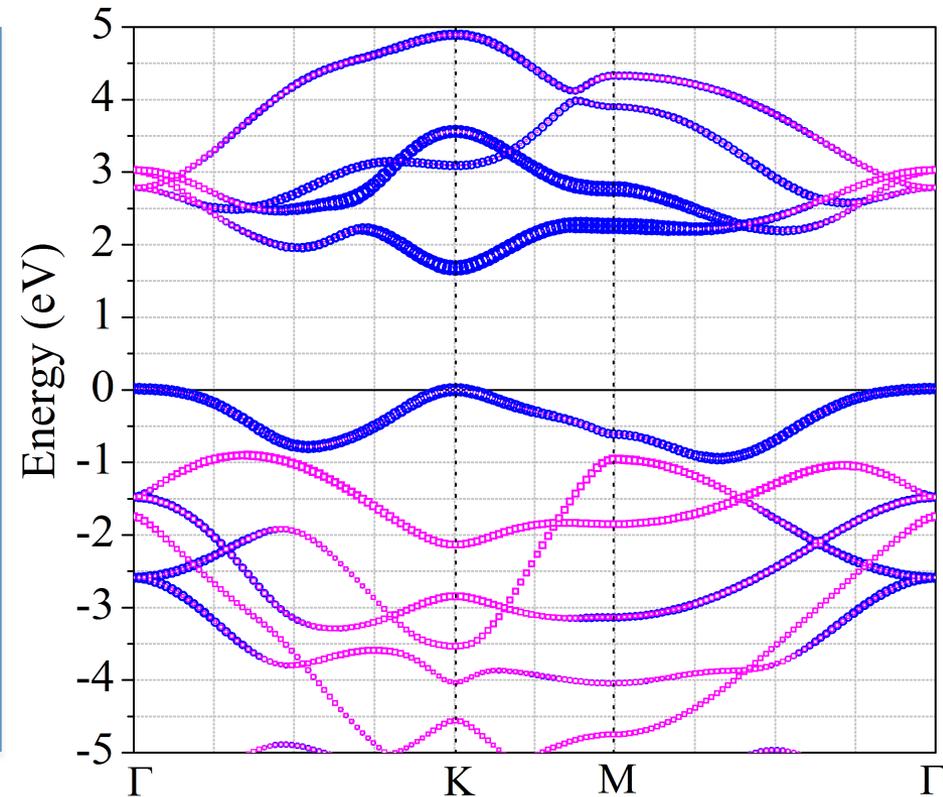
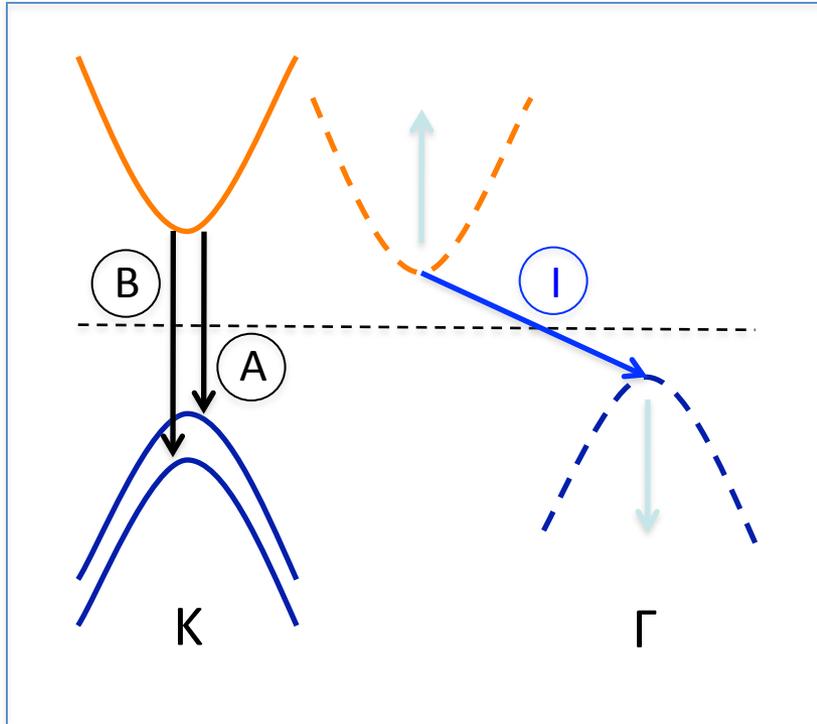
# Single layer MoS<sub>2</sub>



Honeycomb lattice with  
broken sublattice symmetry

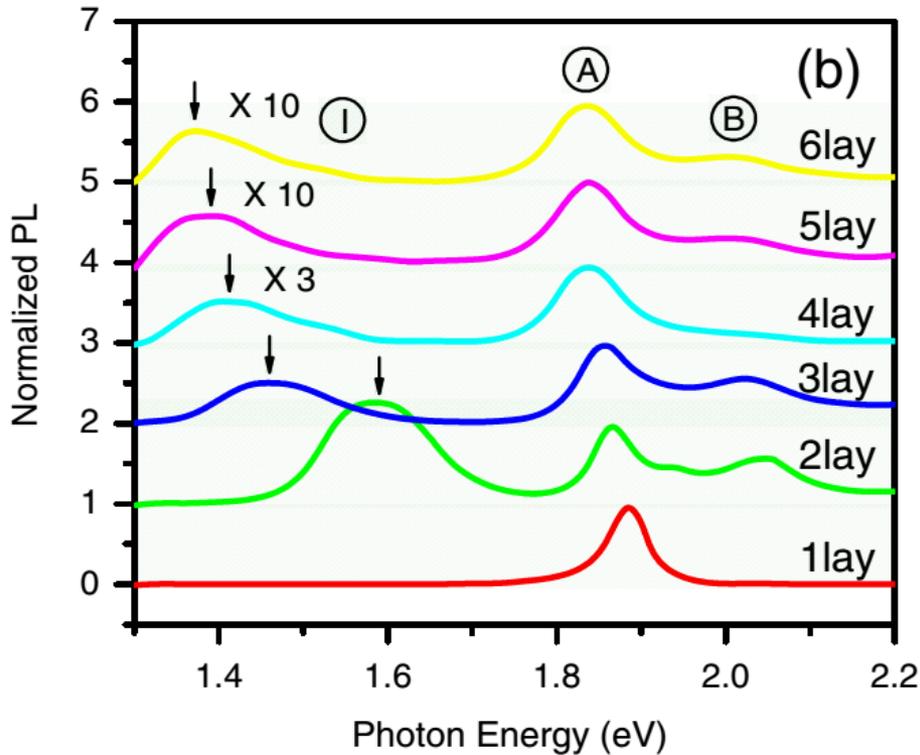


# Indirect-Direct Band Gap Transition

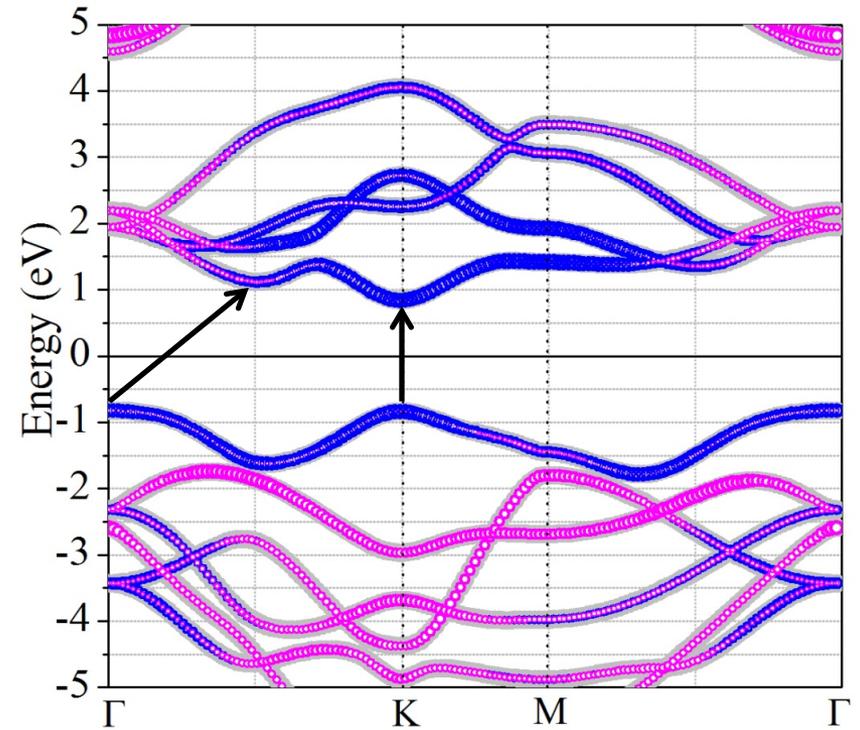


Blue: Mo orbitals  
Magenta: S orbitals  
(Le et al, 2012)

# Band-gap transition

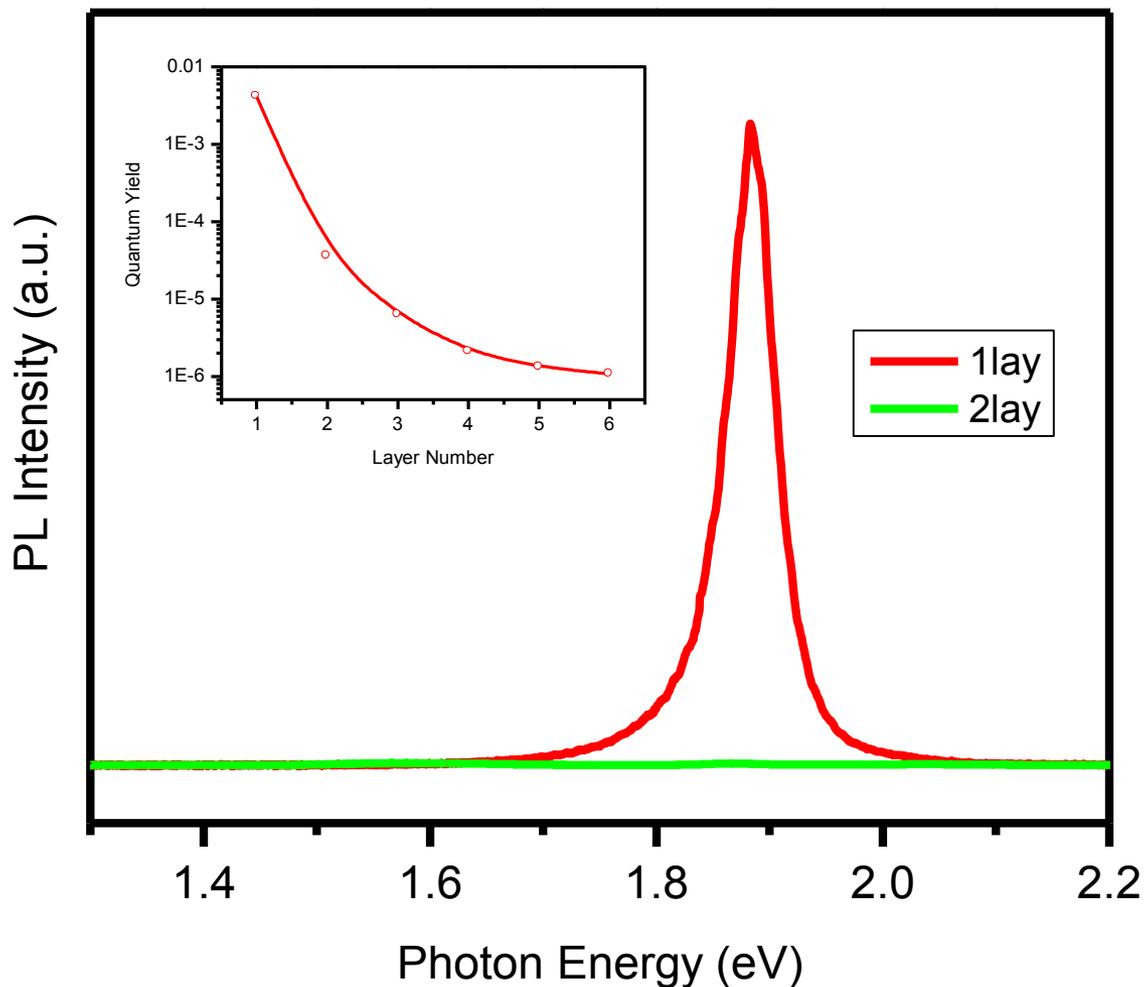


Mak et al., PRL (2010)



- Positions of indirect transitions are strongly affected by number of layers, while that of direct transitions are not.
- Can be explained by theoretical color-coded band structure: at K, states are d-like, localized at Mo atoms (blue) while at indirect transition points the states are affected by S states (magenta).

# Photoluminescence from Atomically Thin MoS<sub>2</sub> Layers

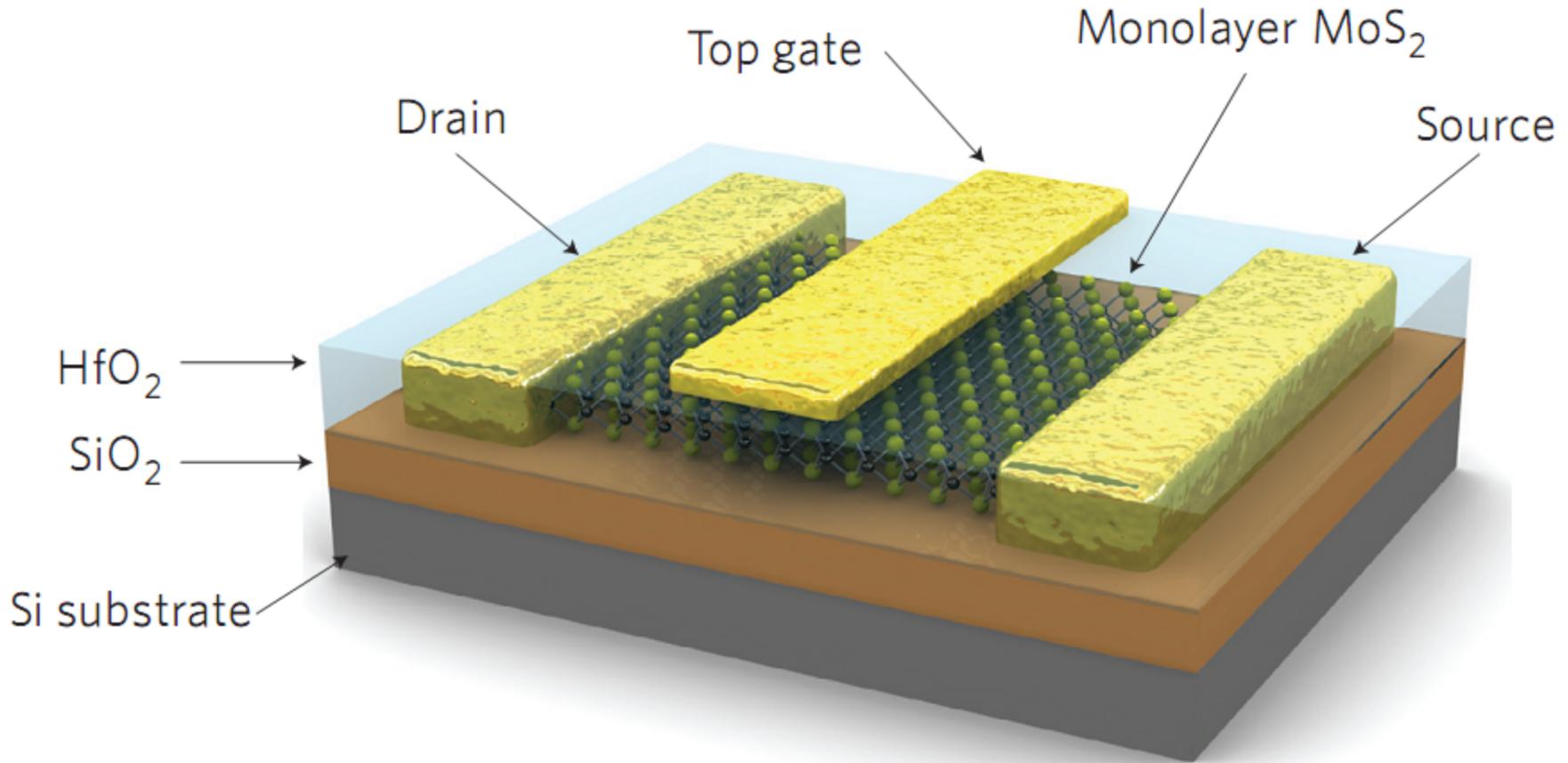


Significant enhancement of PL in *thinner* layers

Nearly 10<sup>4</sup> compared to bulk

Mak et al. PRL (2010)

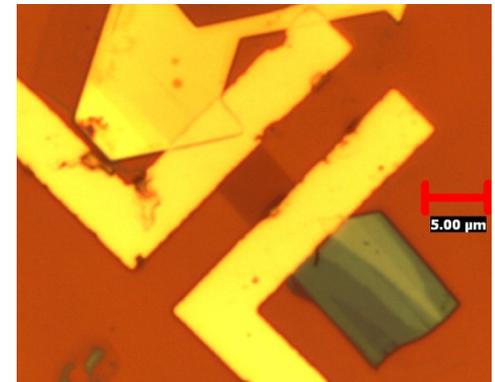
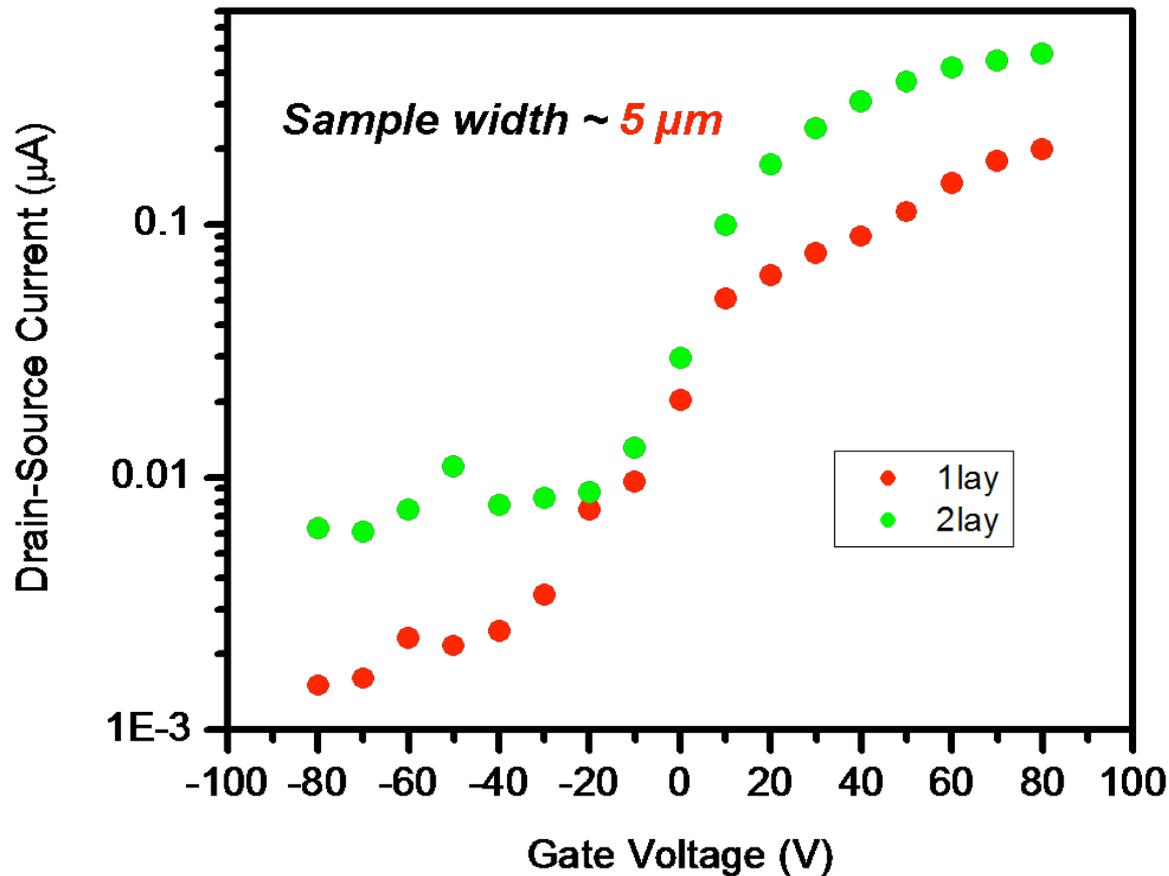
# Electronic Application: Field Effect Transistor



Used hafnium oxide gate dielectric to demonstrate a room-temperature single-layer MoS<sub>2</sub> mobility of at least  $200 \text{ cm}^2\text{V}^{-1}\text{s}^{-1}$ , similar to that of graphene nanoribbons, and produce transistors with room-temperature current on/off ratios of  $1 \times 10^8$  and ultralow standby power dissipation.

Radisavljevic et al., *Nature nanotechnology* (2011).

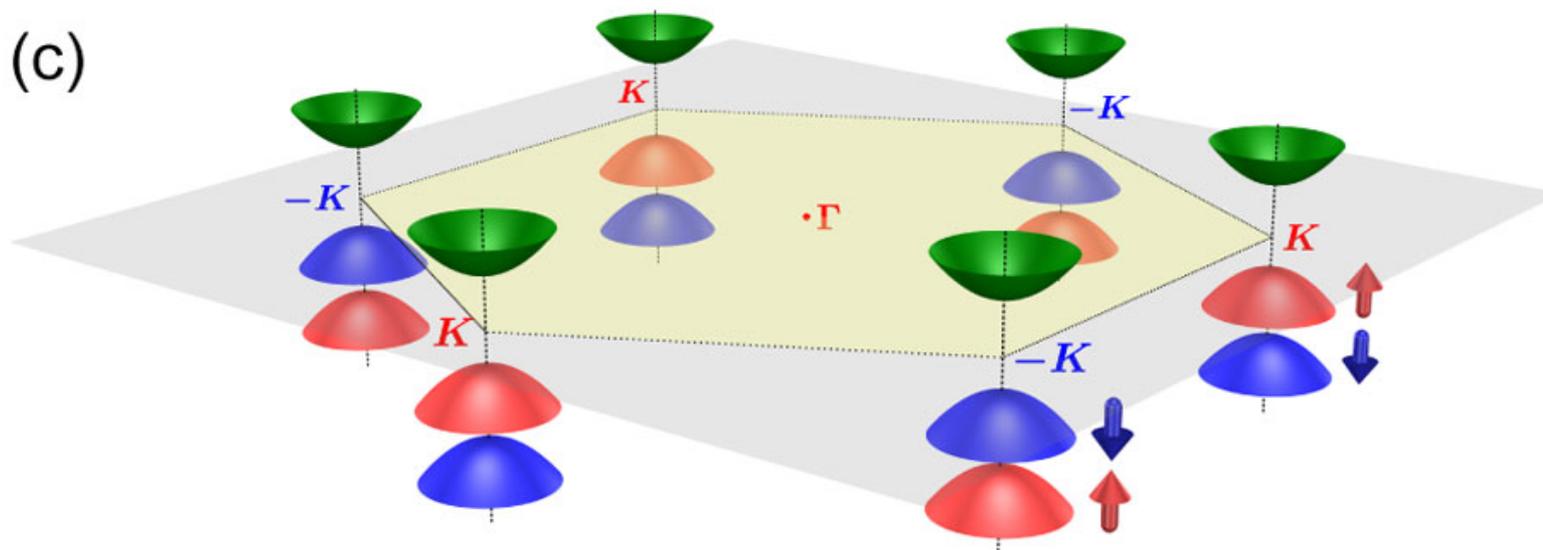
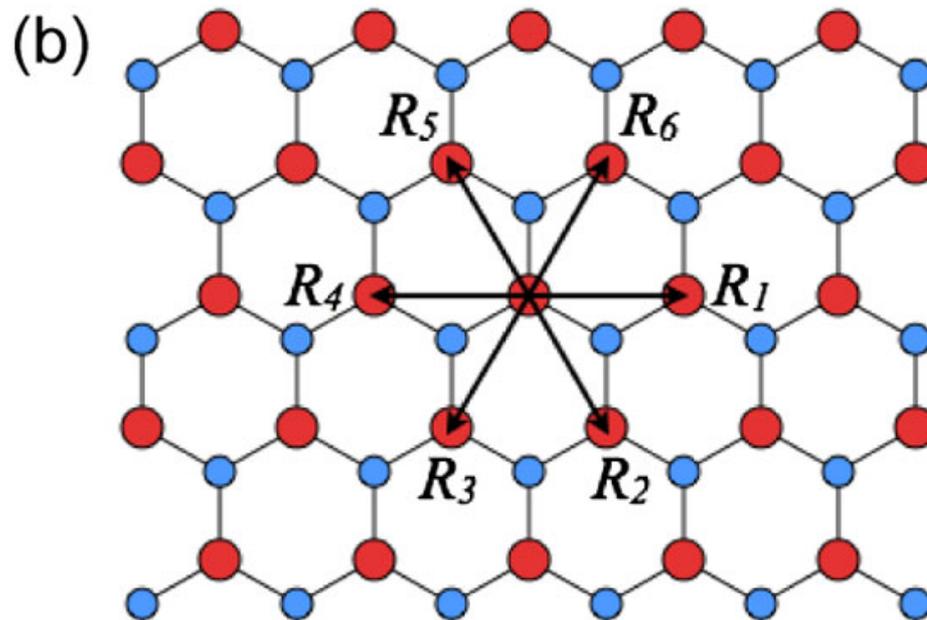
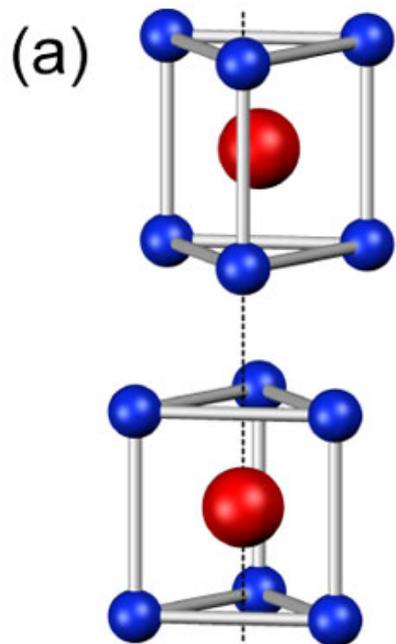
# Single Layer MoS<sub>2</sub> Field-Effect Transistors



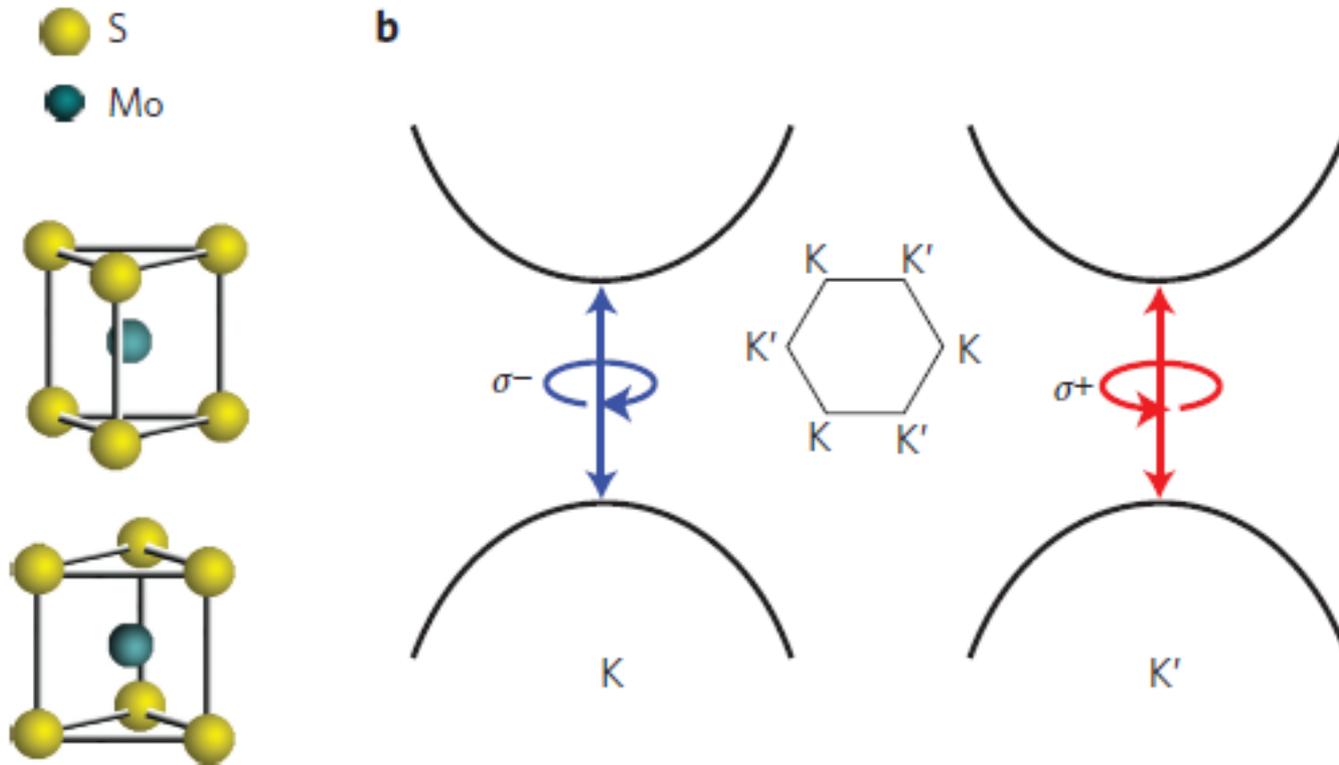
Mak et al. PRL (2010)

A. Kis et al. Nature Nano (2011).

# Reminescent of Graphene & Beyond

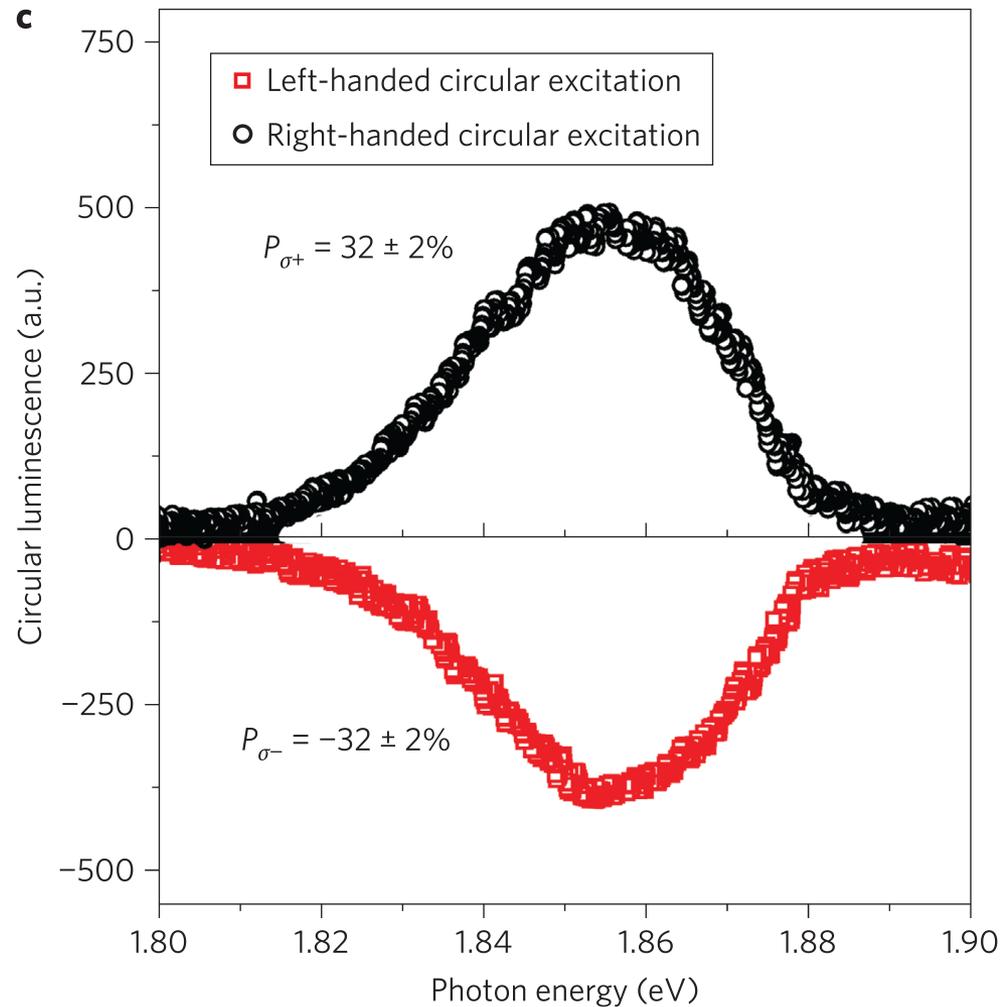


# Valley-dependent selection rules at K and K' points



left (right)-handed circularly polarized light  $\sigma^+$  ( $\sigma^-$ ) only couples to the band-edge transition at K (K') points for the sake of angular momentum conservation and time reversal symmetry  
Figure from H. Zeng et al., Nature Nanotech. 7 409 2012)

# Luminescence polarization in MoS<sub>2</sub>



H. Zeng et al., Nature Nanotech. 7 409 2012

➤ Transition Metal Dichalcogenides (TMDCs) are among the most studied layered compounds that have been isolated in **monolayer form**.

	-S <sub>2</sub>	-Se <sub>2</sub>	-Te <sub>2</sub>
Mo-	Semiconducting Optical gap: 1.9 eV	Semiconducting Optical gap: 1.5 eV	Semiconducting Optical gap: 1.1 eV
W-	Semiconducting Optical gap: 2.1 eV	Semiconducting Optical gap: 1.7 eV	Semiconducting Optical gap: 1.1 eV
Ta-	Metal Superconducting Charge Density Wave	Metal Superconducting Charge Density Wave	Metal
Nb-	Metal Superconducting Charge Density Wave	Metal Superconducting Charge Density Wave	Metal

This table was reproduced from Q. H. Wang *et al.*, Nat. Nanotechnol. 7, 699 (2012).

➤ Mo- and W-based TMDCs are the most studied because of their availability and possibility of isolation in single layer form

# But how do you get 1L TMDC

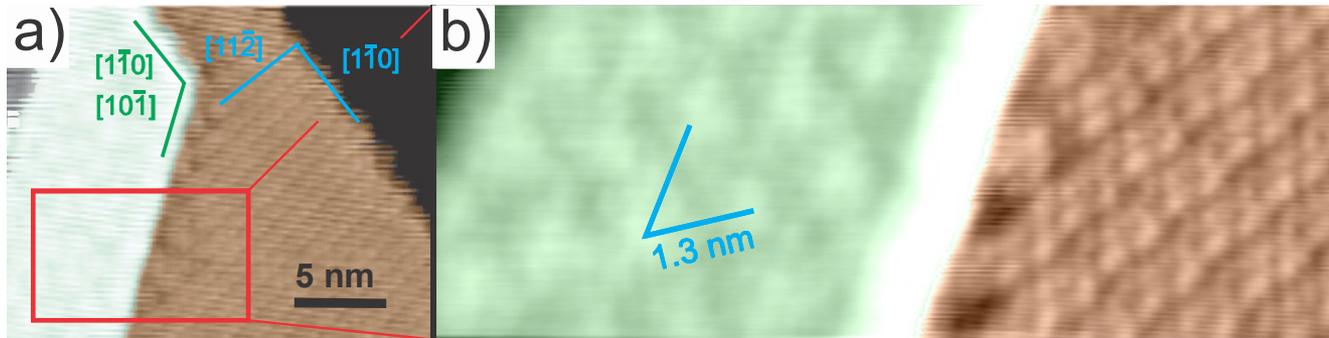
- Exfoliation
- Chemical Vapor Deposition
- Wet chemistry
- Others?

# Growth of Single Layer MoS<sub>2</sub> on close-packed metal surfaces

on close-packed metal surfaces

- D. Kim, D. Sun, W. Lu, Z. Cheng, Y. Zhu, D. Le, TSR, and L. Bartels “[Toward the Growth of an Aligned Single-Layer MoS<sub>2</sub> Film](#),” Langmuir 27, 11650 (2011).
- D. Le, L. Bartels, and TSR and, “[Single layer MoS<sub>2</sub> on the Cu\(111\) surface: First-principles electronic structure calculations](#),” Phys. Rev. B 85, 075429 (2012).

➤ Recently, large single layer patches of MoS<sub>2</sub> were grown on Cu(111) which shows a regular Moiré pattern of about 1.3 nm.



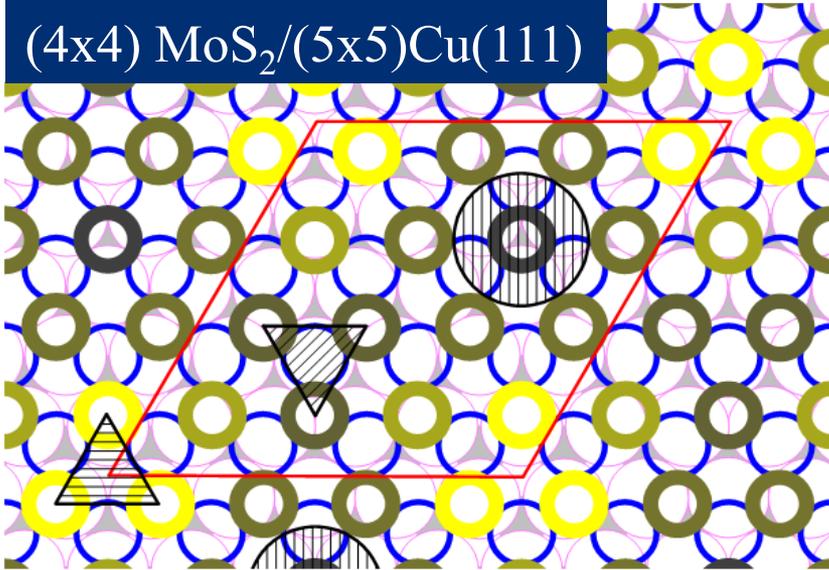
(a) portion of a MoS<sub>2</sub> layer (left, green) on a sulfur terminated Cu(111) terrace with a dislocation step indicating substrate crystallographic axes. (b) Enlarged portion near the MoS<sub>2</sub> edge showing angular registry between MoS<sub>2</sub> Moiré pattern and straight edge. Image Parameters: Bias: -560 mV, Current: 140 pA [D. Kim *et al*, Langmuir (2011)]

➤ Using DFT with vdW-DF) we have:

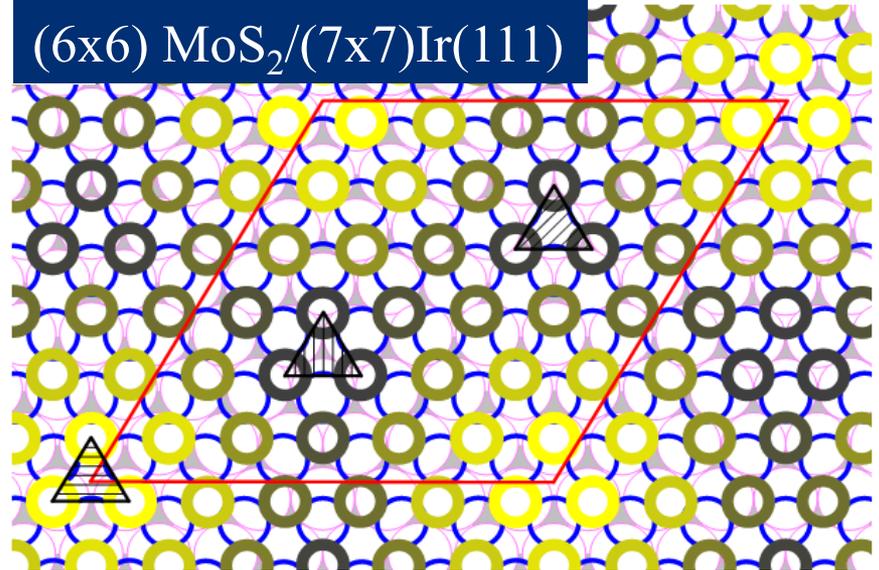
- Confirmed the observed Moiré pattern periodicity on Cu(111)
- Investigated geometry of MoS<sub>2</sub> layer and Cu(111).
- Found the nature of bonding between MoS<sub>2</sub> layer & Cu(111)
- Predicted Moiré patterns on other metal surfaces.

# Moiré patterns on metal surfaces

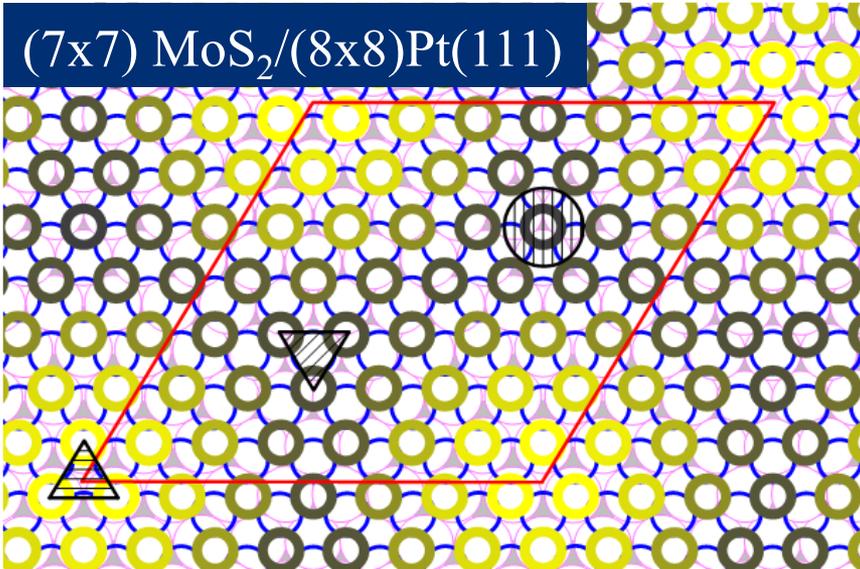
(4x4) MoS<sub>2</sub>/(5x5)Cu(111)



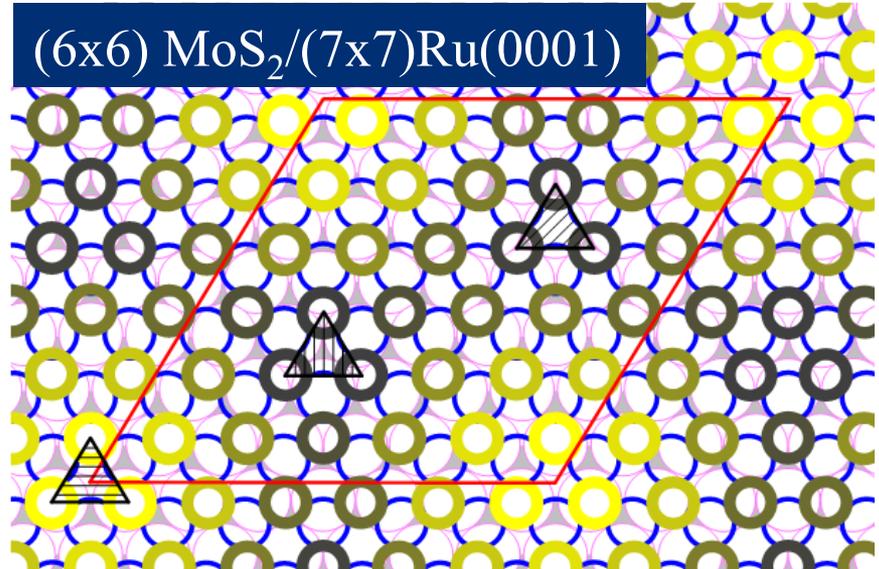
(6x6) MoS<sub>2</sub>/(7x7)Ir(111)



(7x7) MoS<sub>2</sub>/(8x8)Pt(111)



(6x6) MoS<sub>2</sub>/(7x7)Ru(0001)



# Moiré pattern periodicities

- Moiré pattern is formed if a MoS<sub>2</sub> layer can be grown on close packed metal surfaces.
- It is because of the mismatch between MoS<sub>2</sub> lattice (3.16 Å) and the distance between two three-fold hollow sites.

➤ If the unit cell of Moiré pattern consists of a ( $n_1 \times n_1$ ) MoS<sub>2</sub> and ( $n_2 \times n_2$ ) Metal surfaces, the mismatch  $m$  has to be small:

$$m = \frac{n_1 d_S}{n_2 d_M} - 1$$

$d_S$ : S-S distance

$d_M$ : Metal-Metal distance

TABLE I. Predicted sizes of MoS<sub>2</sub> Moiré unit cell on several close packed metal surfaces. ( $n_2 \leq 20$ )

Surfaces	$d_M$ (Å) <sup>a</sup>	$n_1$	$n_2$	$m$ (%)
Ag(111)	2.89	10	11	-0.7
Cu(111)	2.55	4	5	-1.0
Ni(111)	2.49	4	4	-0.2
Pt(111)	2.77	4	4	0.2
Rh(111)	2.69	4	4	-0.2
		4	4	0.8
		4	4	-0.5
		17	20	0.0
Ir(111)	2.72	6	7	-0.2
Re(0001)	2.76	7	8	0.2
Ru(0001)	2.71	6	7	-0.1

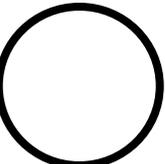
**Agree with experimental observation**

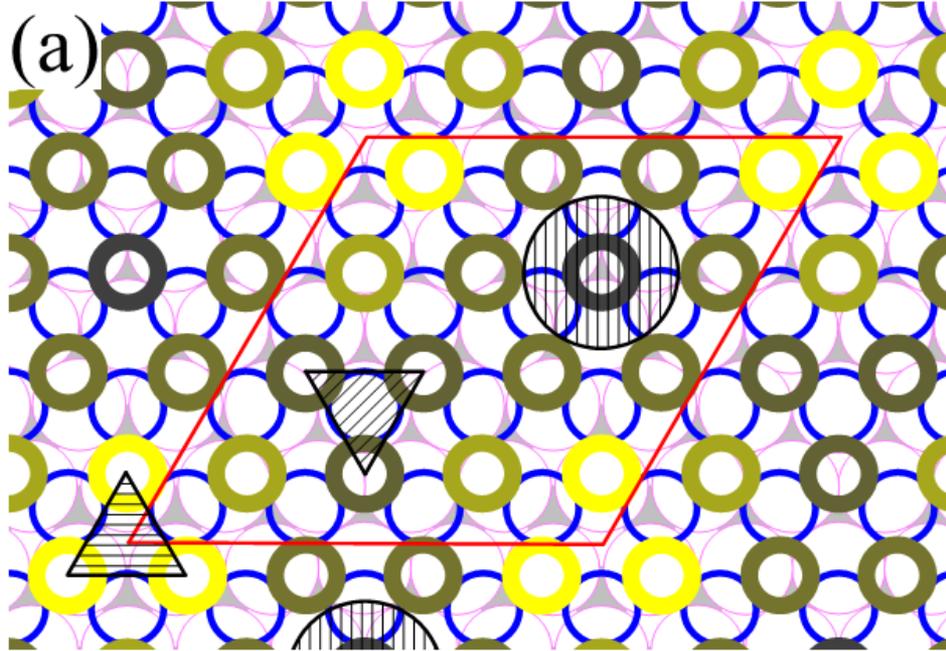
<sup>a</sup> Calculated from experimental lattice parameters

# Geometry of MoS<sub>2</sub> on Cu(111) - Registry

 Connect 3 equivalent S without Mo at center

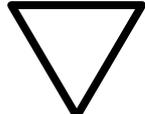
 Connect 3 equivalent S with Mo at center

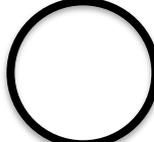
 Centered at S atom that is in registry with high symmetry site



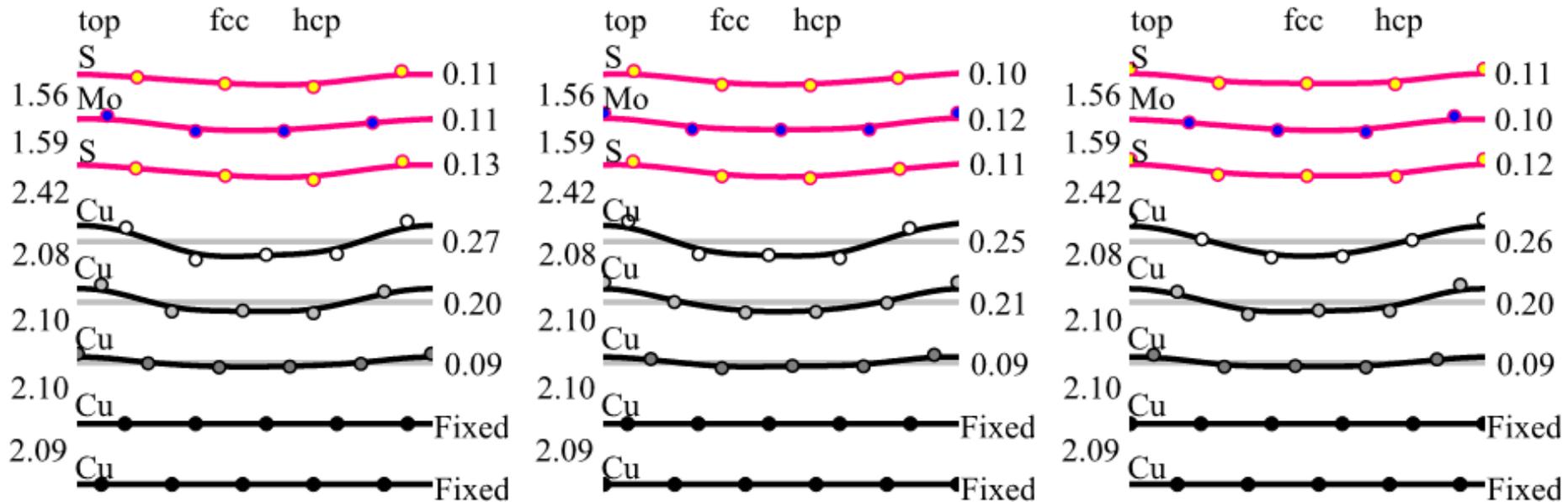
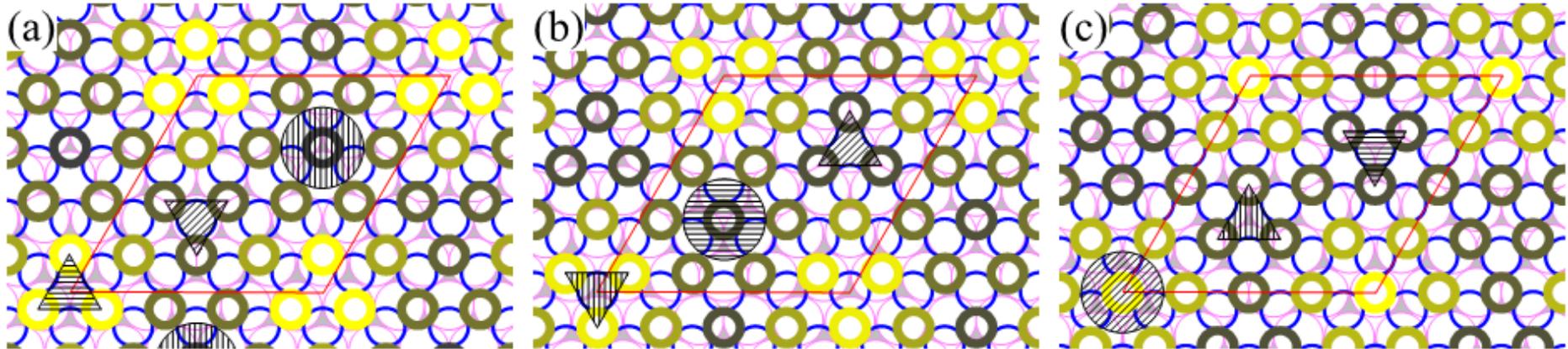
**$\alpha$  stacking**

Centers of  are in registry with fcc sites

Centers of  are in registry with top sites

Centers of  are in registry with hcp sites

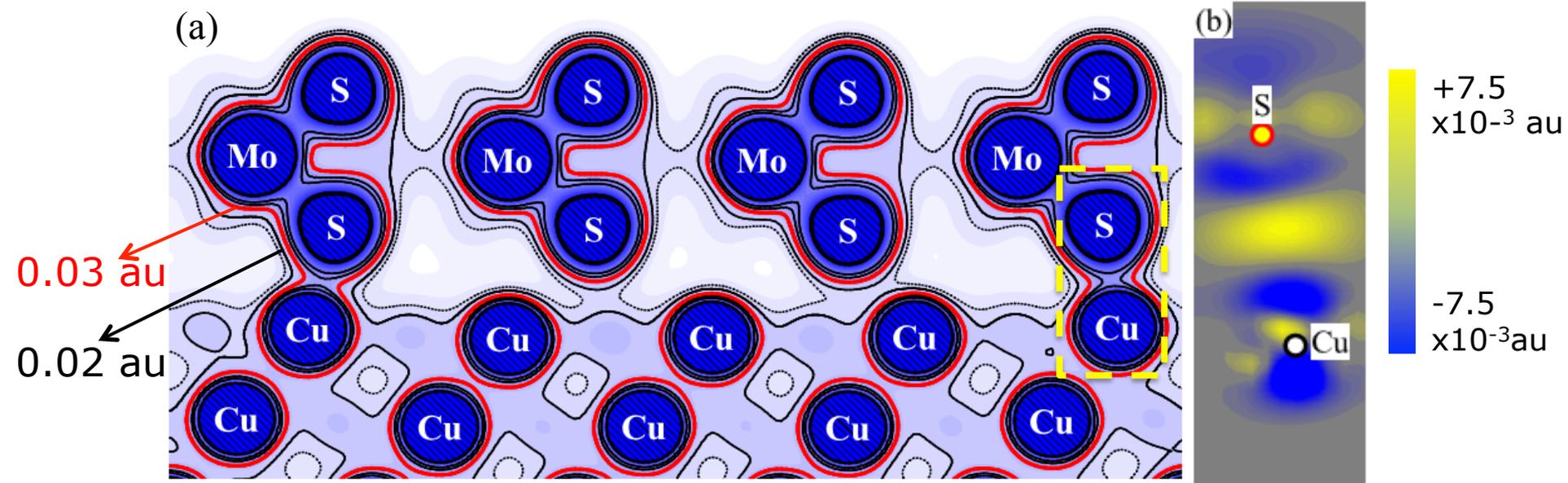
# Geometry of MoS<sub>2</sub> on Cu(111) - Buckling



Buckling along the longest diagonal of Moiré unitcell

- S, Mo layers buckling of  $\sim 0.1 \text{ \AA}$
- Cu surface buckles more  $\sim 0.3 \text{ \AA}$

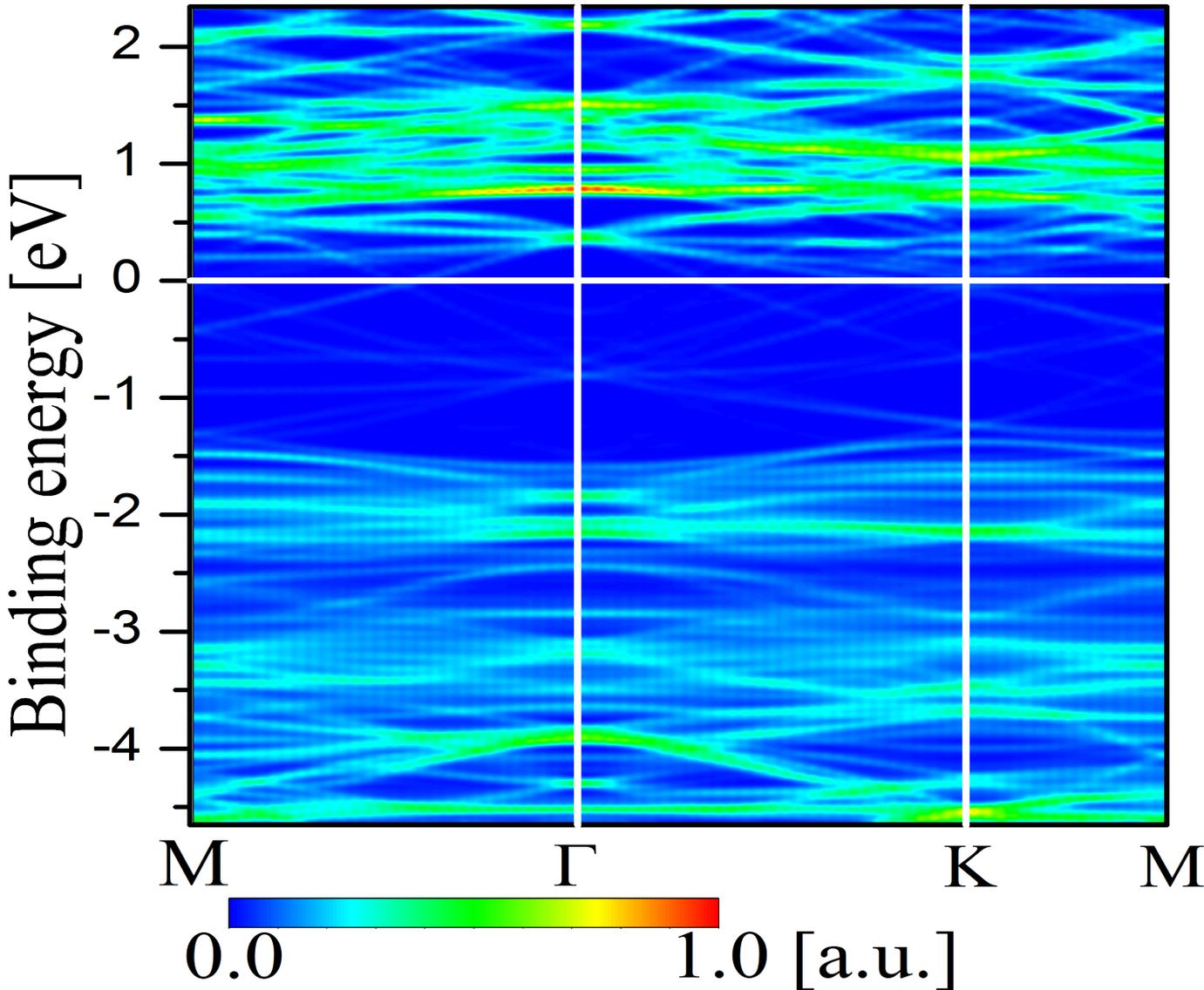
# Interaction between MoS<sub>2</sub> layer and Cu(111)



Take the case of  $\alpha$  stacking as an example:

- Large MoS<sub>2</sub>--Cu(111) separation ( $\sim 2.4\text{\AA}$ ) indicate weak interaction.
- Charge density along vertical plane passing through the longest diagonal of Moiré unit cell (a) shows indeed the formation of S-Cu chemical bonding.
- Charge density redistribution (b) shows noticeable accumulation of charge to the region between S-Cu => Covalent bonding

# Electronic Structures of MoS<sub>2</sub> and Cu(111)

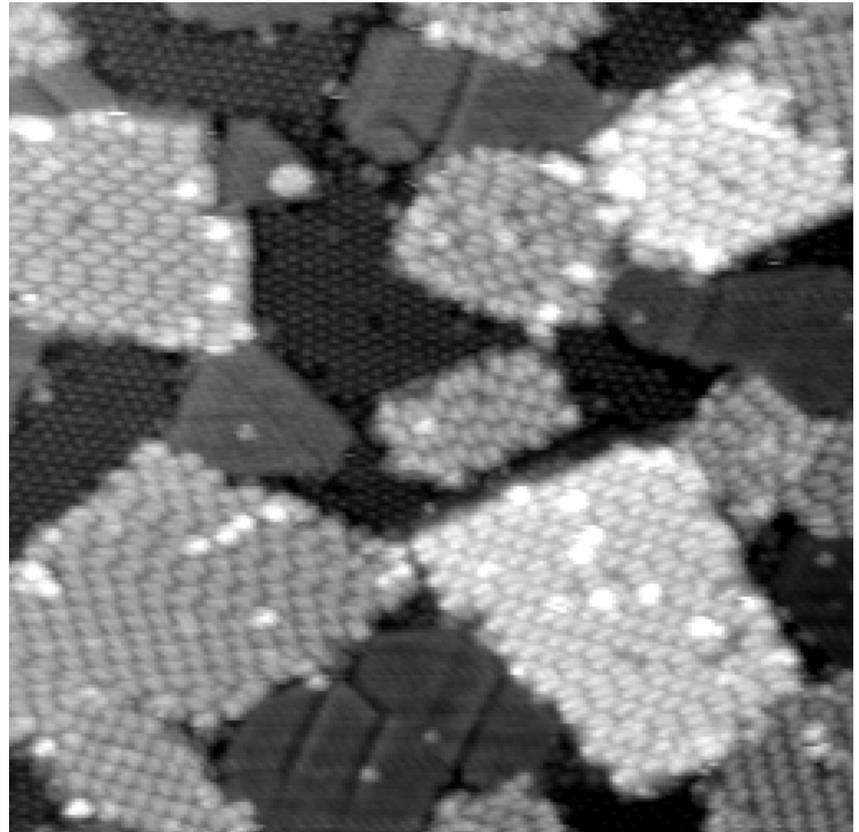
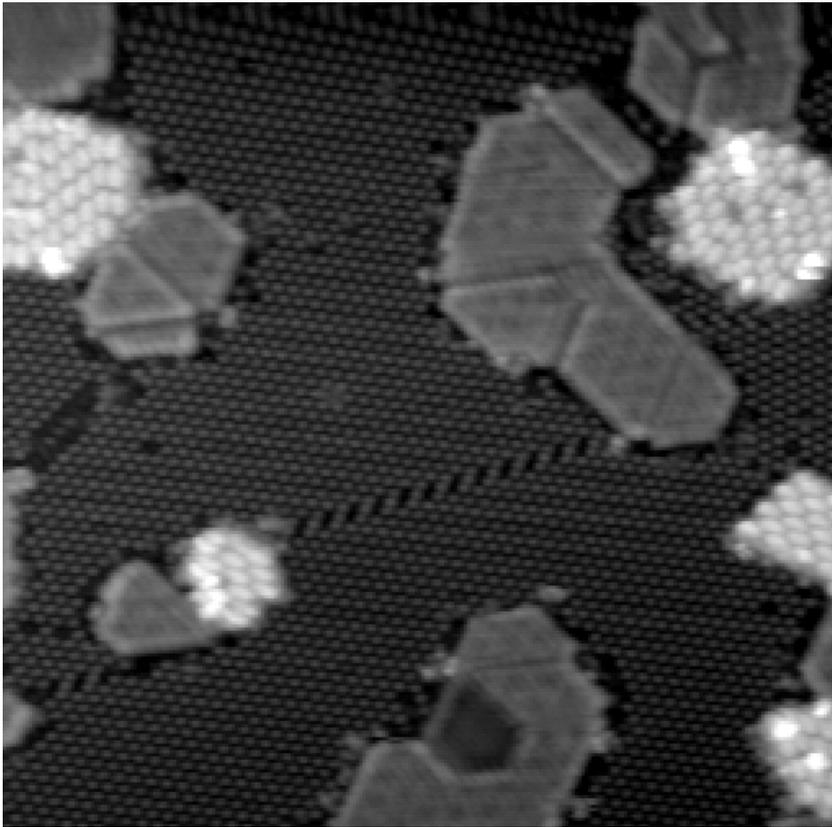


➤ Appearance of bands inside the gap of MoS<sub>2</sub> from hybridization of MoS<sub>2</sub> and Cu(111) orbitals.

➤ MoS<sub>2</sub> is n-doped

Electronic band structure for (4x4) MoS<sub>2</sub> when grown on Cu(111).

# Experiments



Anthraquinone (AQ) tends to adsorb on "square" structures ☺: indicating that this new material is potentially active for chemical reaction.

# Summary – Part A

- Our calculated optimum size of the Moiré pattern of (4x4) MoS<sub>2</sub>/(5x5) Cu(111) is in agreement with STM observations.
- We predict the size of Moiré patterns for MoS<sub>2</sub> on several close-packed metal substrates.
- Three energetically equivalent stacking types ( $\alpha$ ,  $\beta$ ,  $\gamma$ ) of MoS<sub>2</sub> on Cu(111) with distinguishable fingerprints in STM images.
- We find very little corrugation of MoS<sub>2</sub> layer but noticeable rearrangement of the Cu surface atoms.
- MoS<sub>2</sub> overlayer is chemisorbed, albeit weakly, to the Cu surface.

# Manipulating joined-edges in 1L MoS<sub>2</sub>: 1D Magnetism?

D. Le and T. S. R., "Joined edges in MoS<sub>2</sub>: metallic and half-metallic wires,"  
J. Phys.: Condens. Matter 25, 312201 (2013).

# The idea

single-layer-MoS<sub>2</sub>, distinct from those exfoliated from bulk material.

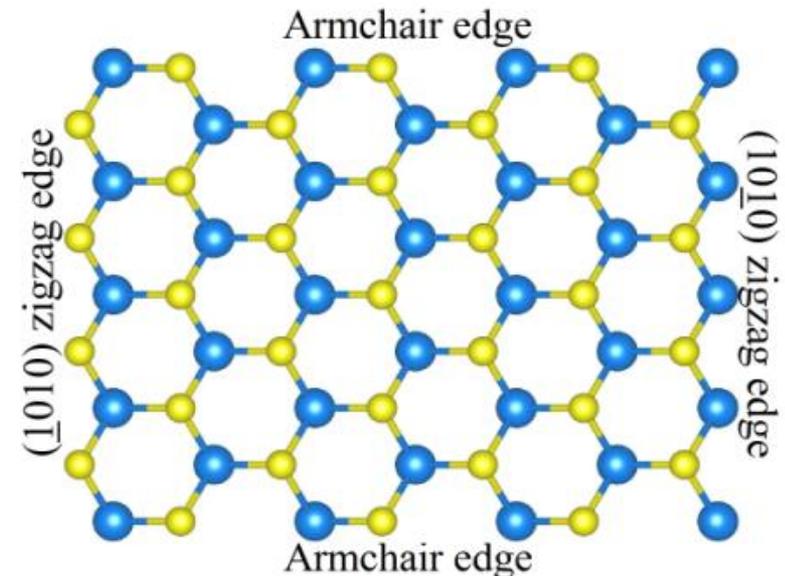
➤ During growth the different nucleation centers may lead to the formation of MoS<sub>2</sub> domains of various orientation on substrates.

➤ Dislocations and grain-boundaries (GBs) may be formed between MoS<sub>2</sub> domains. [Najmaei *et al.* [arXiv:1301.2812], van der Zande *et al.* [arXiv:1301.1985], [Zou *et al.*, Nano Lett. (2013)]

➤ A possible dislocation in MoS<sub>2</sub> is that formed between the edges of two domains: *joined-edge defect* (JED).

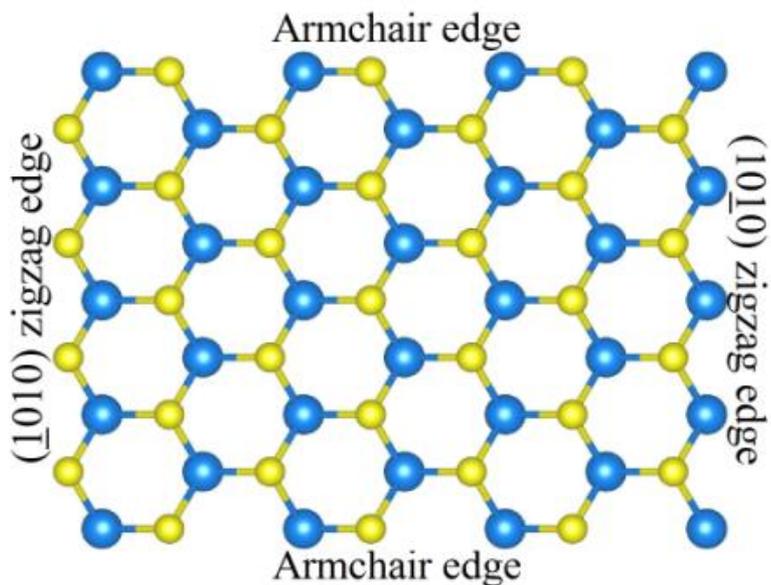
➤ The structural and electronic properties of symmetrical JEDs differ from that of MoS<sub>2</sub> layer and other dislocations and GBs.

➤ As prototypes: *symmetrical JEDs formed between zigzag edges of two MoS<sub>2</sub> domains by sharing the edge-atoms.*

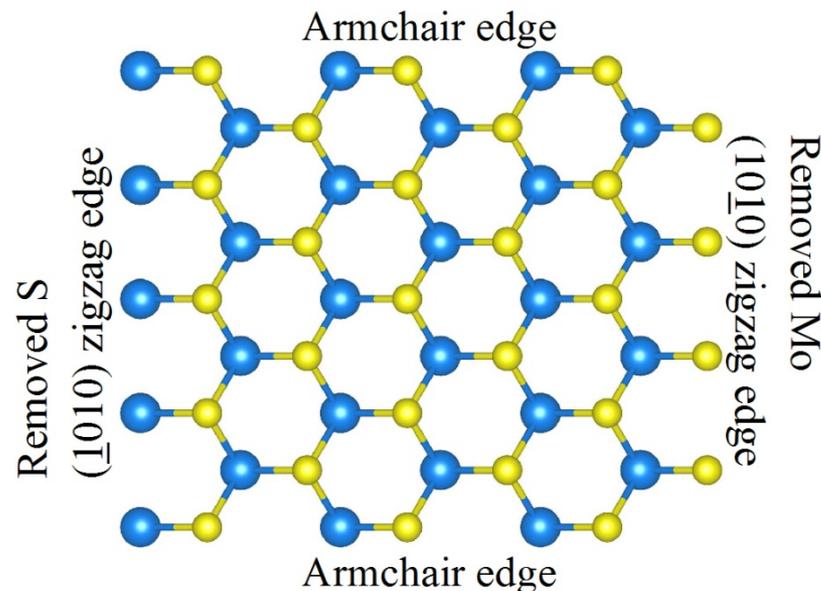


Ball-stick model of armchair and zigzag edges of MoS<sub>2</sub>: Blue (Mo) and Yellow

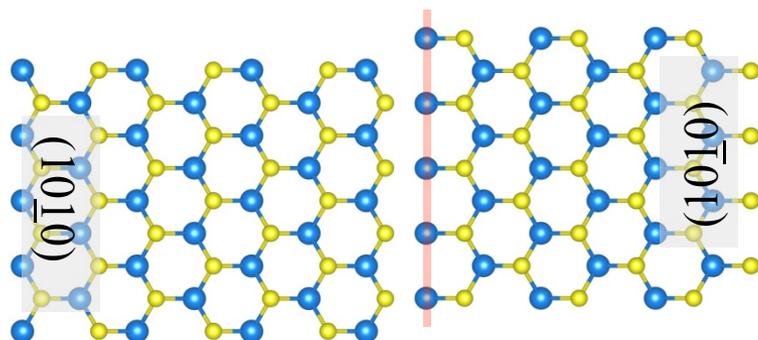
# The Edges of Single-layer MoS<sub>2</sub>



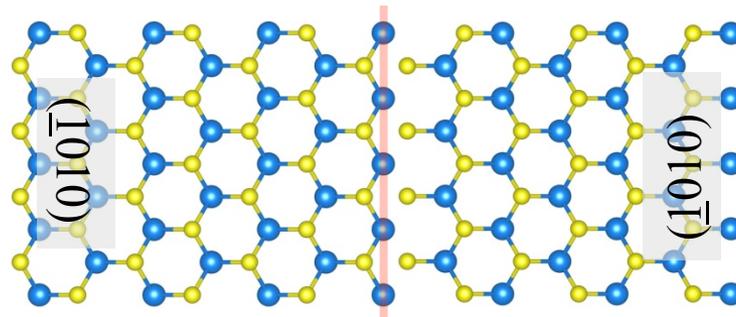
Zigzag and Armchair edges



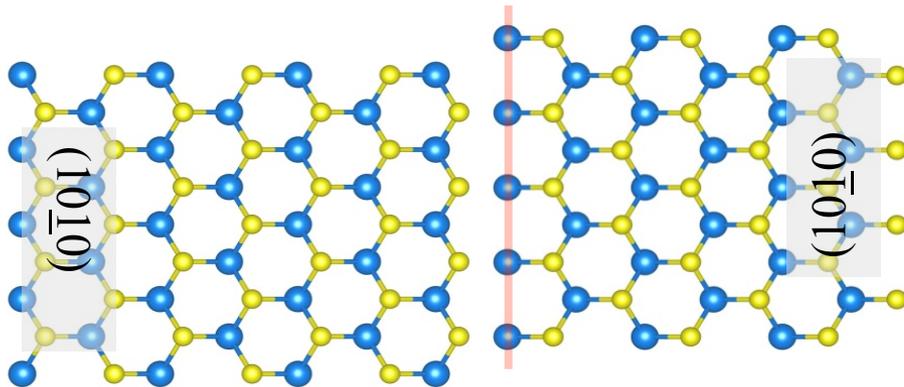
Zigzag edges with outer atoms removed



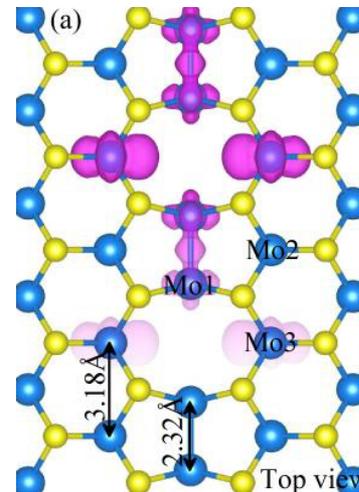
Mo-JED<sub>1</sub>



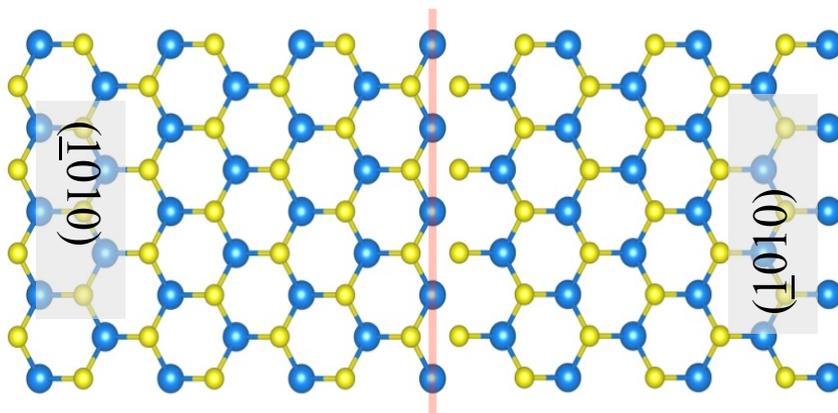
Mo-JED<sub>2</sub>



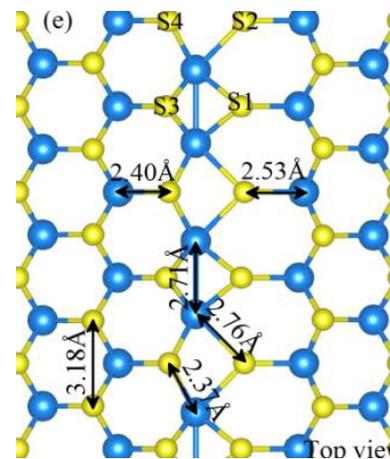
Mo-JED<sub>1</sub> unrelaxed



Mo-JED<sub>1</sub> relaxed

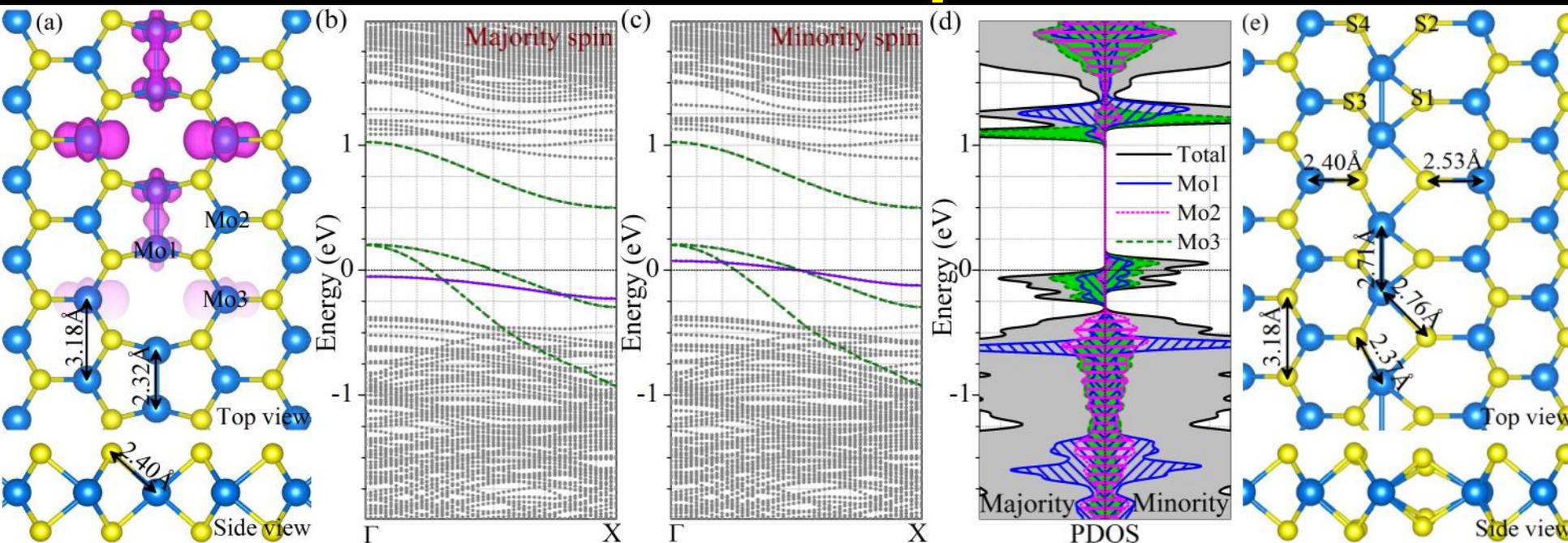


Mo-JED<sub>2</sub> unrelaxed



Mo-JED<sub>2</sub> relaxed

# Electronic Structure & Spin Distribution



- (a) Structure of Mo-JED<sub>1</sub> with spin-distribution (iso-surface of 0.006  $\mu_B/\text{\AA}^3$ ) --top.
- (b) Majority spin electronic band structure near the Fermi level (0 eV).
- (c) Minority spin electronic band structure near the Fermi level
- (d) PDOS onto orbitals of atoms near Mo-JED<sub>1</sub> (Total) and Mo1, Mo2, Mo3 as in (a).
- (e) Structure of Mo-JED<sub>2</sub>

Violet (Olive) lines highlight mid-gap states of Mo-JED<sub>1</sub>(Mo-JED<sub>2</sub>); Gaussian

# Summary

- Four candidates for symmetrical JEDs between two MoS<sub>2</sub> domains.
- We find three of them (Mo-JED<sub>1</sub>, S-JED<sub>1</sub>, and S-JED<sub>2</sub>) are mirror-symmetrical.
- We show that Mo-JED<sub>1</sub> (formed between (1010)-Mo edges of two MoS<sub>2</sub> domains), and S-JED<sub>2</sub> (formed between (1010)-Mo edges of two MoS<sub>2</sub> domains) undergo (2 × 1) reconstruction.
- **We predict/discover the half-metallic behavior for Mo-JED<sub>1</sub> and metallic for S-JED<sub>1</sub> and S-JED<sub>2</sub>.**
- These results suggest the possibility of using the JEDs as material for 1D transport or spin-transport (Mo-JED<sub>1</sub>) and raises questions about the effect of such defects on MoS<sub>2</sub>-based applications.

# Band Gap Engineering of 1L MoS<sub>2</sub>

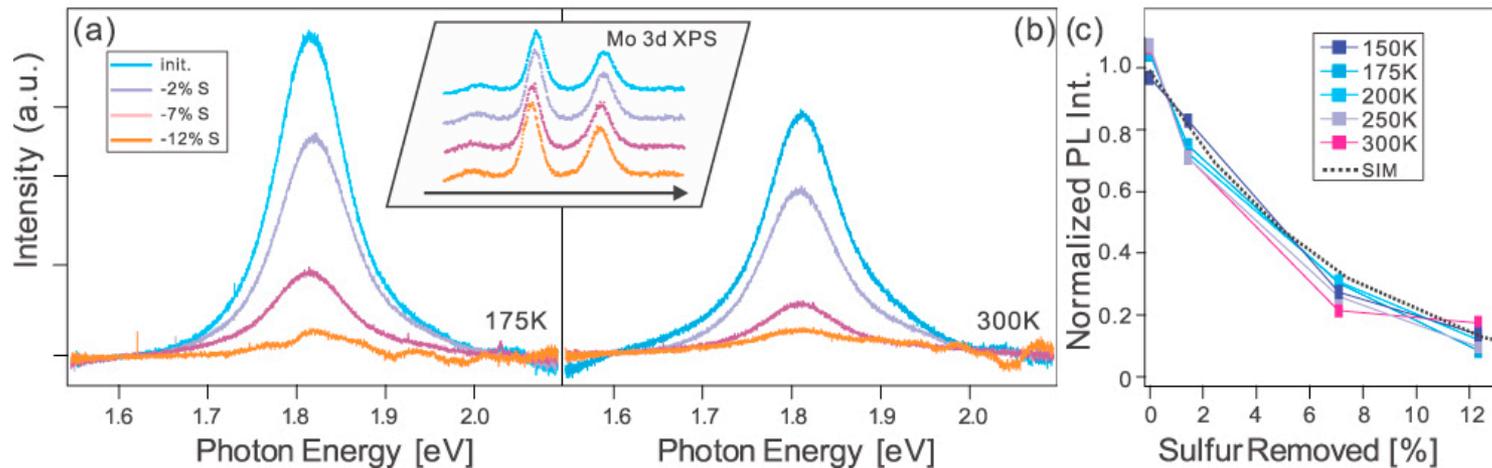
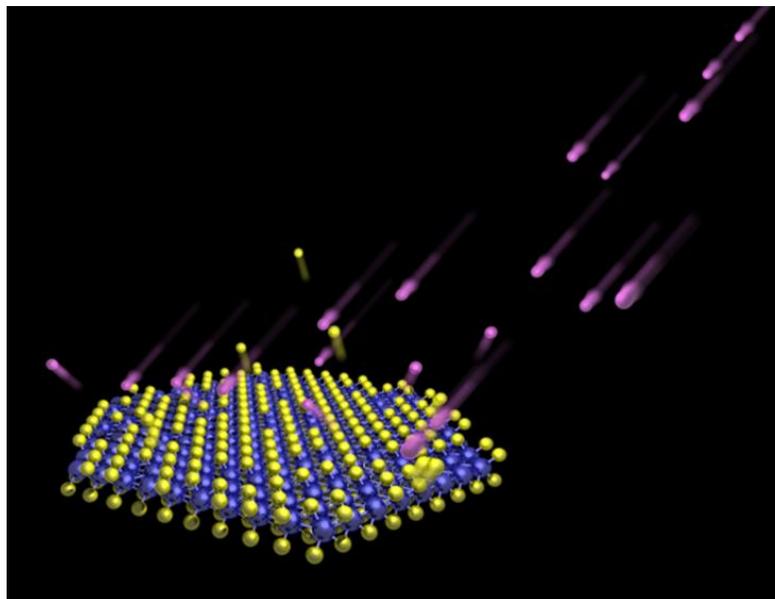
- Alloying
- Alkali Doping
- Hydrogenation
- Vacancies

- Vacancies
- Hydrogenation
- Alloying

# Vacancies & Alloying: $\text{MoS}_{2(1-x)}\text{Se}_{2x}$ Tunable Direct Band Gaps

J. Mann, et al. 2014

# Creation of Sulfur vacancies



Controlled Argon Beam-Induced Desulfurization of Monolayer Molybdenum Disulfide  
Q. Ma *et al.*, *JPCM* **25**, 252201 (2013).

# Filling S vacancies with Se

- It is possible to insert Se into S vacancy  
-> forming  $\text{MoS}_{2(1-x)}\text{Se}_{2x}$

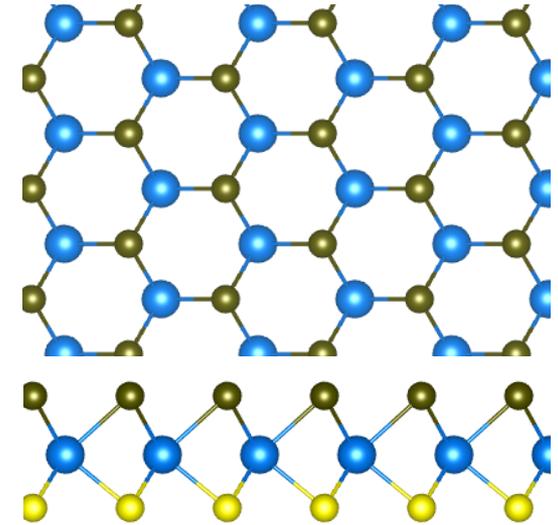
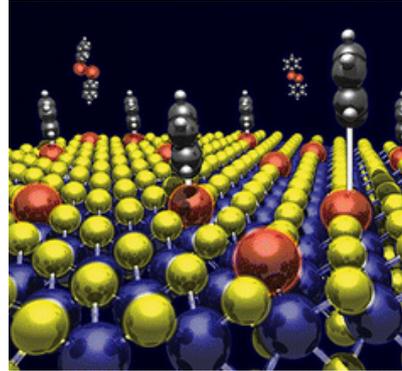
By using organic Se source (diselenodiphenyl)

- Possible applications:

- Heterogeneous junction
- Band gap tuning
- *Possibly new physics for polar metal dichalcogenide?*

"Post-Growth Tuning of the Bandgap of Single-Layer  $\text{MoS}_2$  Films by Sulfur/Selenium Exchange"

Q. Ma *et al.*, ACS Nano **8**, 4672 (2014)



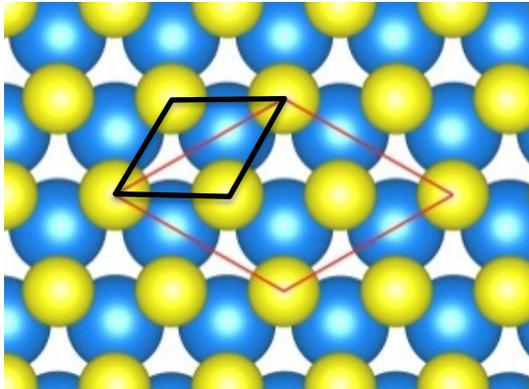
## Questions:

- Band gap as function of Se concentrations
- Stability

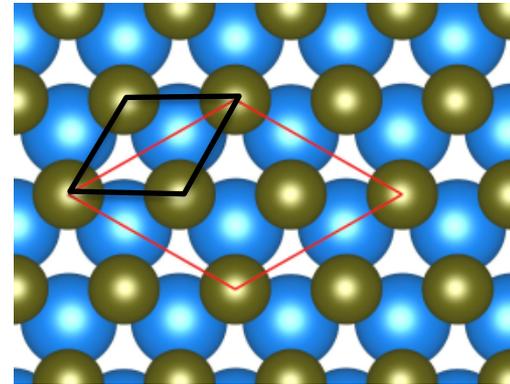
# Band-gap engineering

➤  $\text{MoS}_{2(1-x)}\text{Se}_{2x}$  alloy: allows tuning of band-gap over a short range

**MoS<sub>2</sub>**



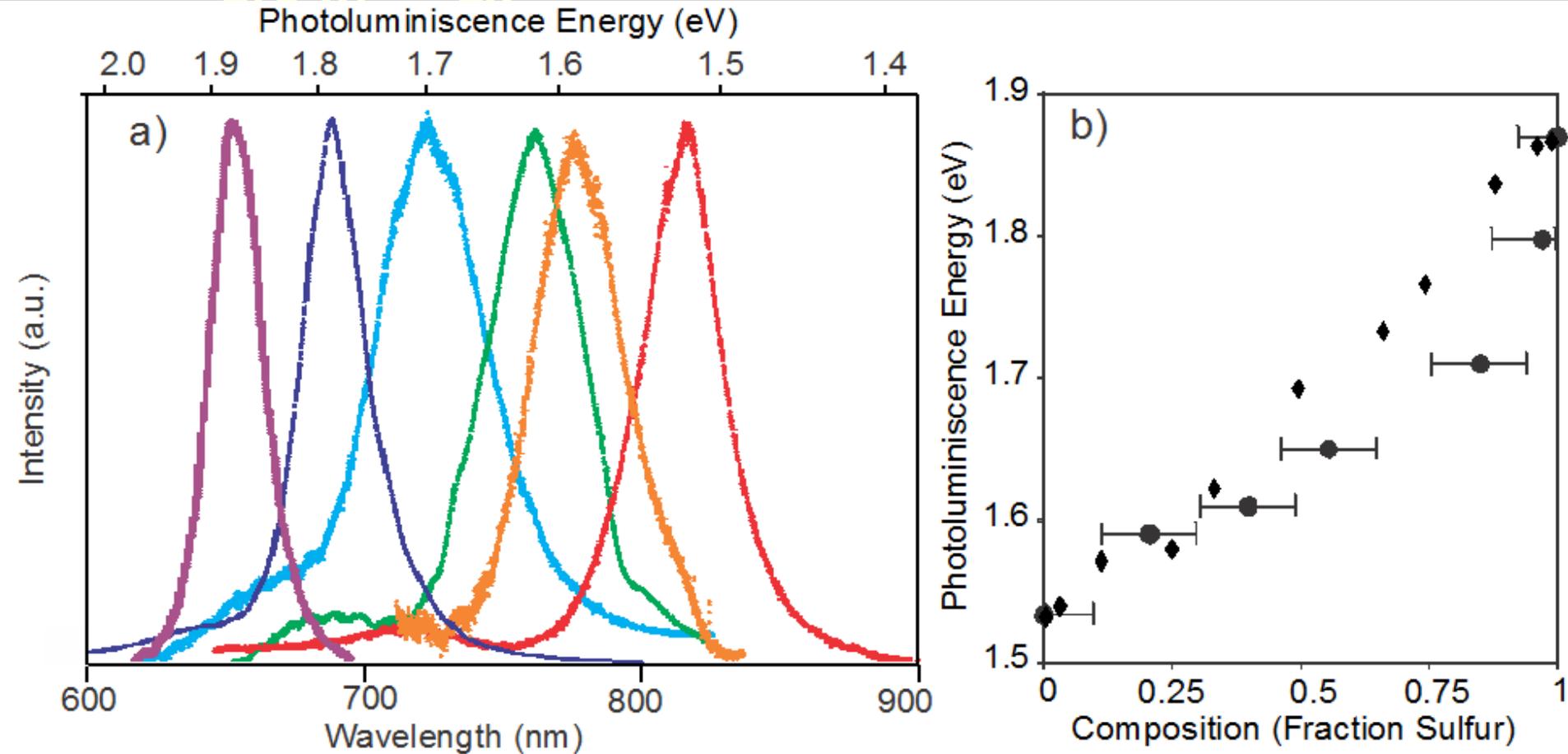
**MoSe<sub>2</sub>**



<b>DFT - PBE Band gap</b>	<b>1.68 eV</b>
<b>Experimental PL peak</b>	<b>1.87 eV</b>

<b>1.45 eV</b>
<b>1.54 eV</b>

# MoS<sub>2(1-x)</sub>Se<sub>2x</sub>: experimental data & theory

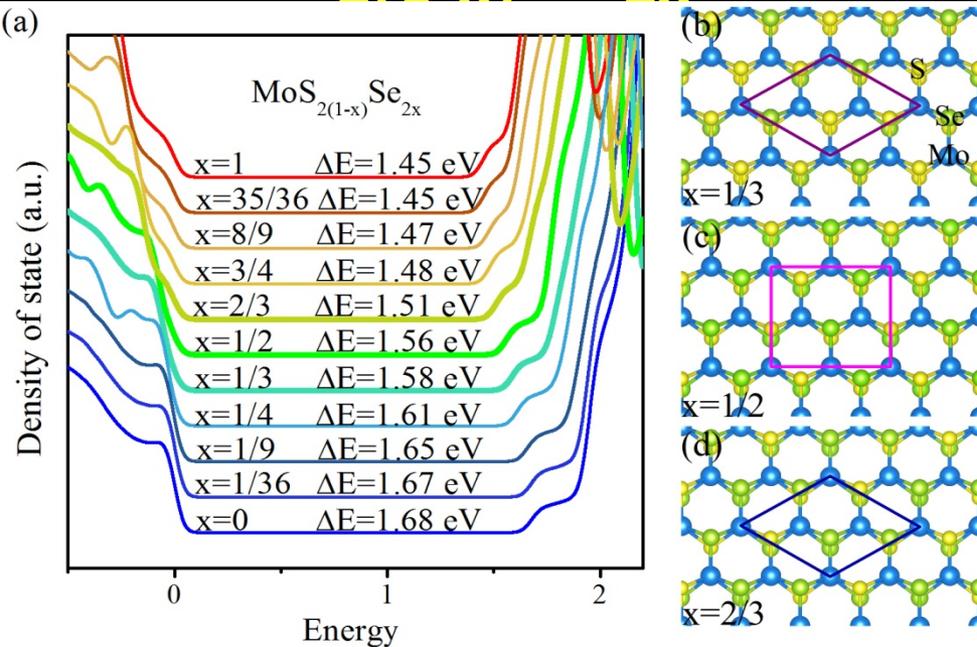


- a) Normalized RT PL spectra on MoS<sub>2(1-x)</sub>Se<sub>2x</sub> films of different composition.
- b) Variation of the PL photon energy with composition (XPS).

black diamond: indicate theoretical predictions of the bandgap (scaled).

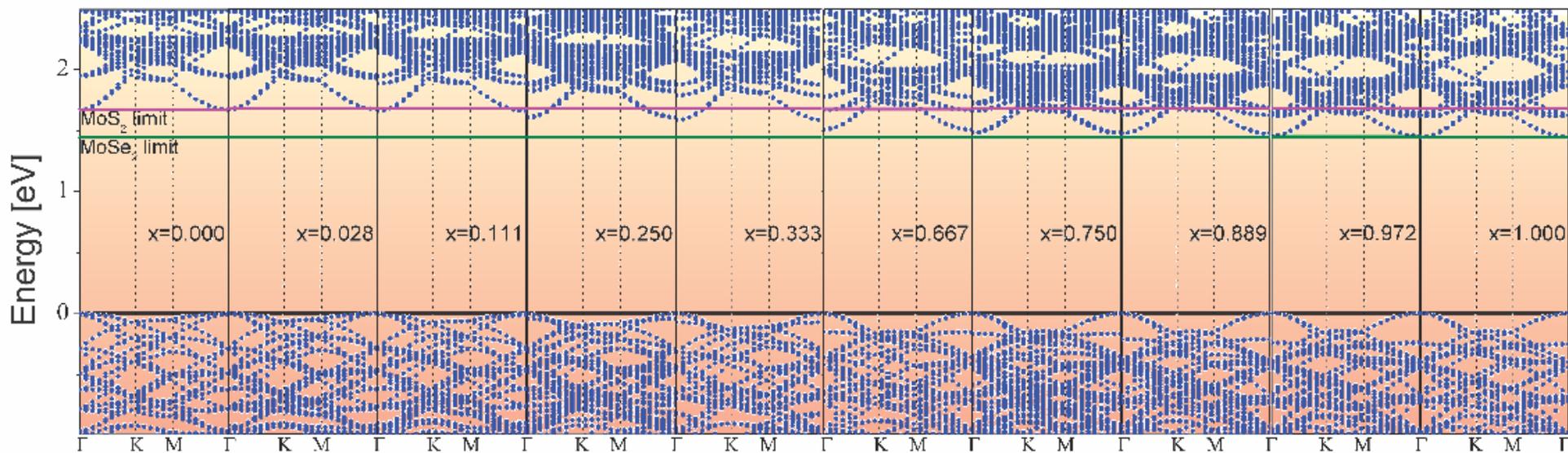
J. Mann *et al.*, Adv. Mater. **26**, 1399 (2014).

# MoS<sub>2(1-x)</sub>Se<sub>2x</sub>: calculated energy bands

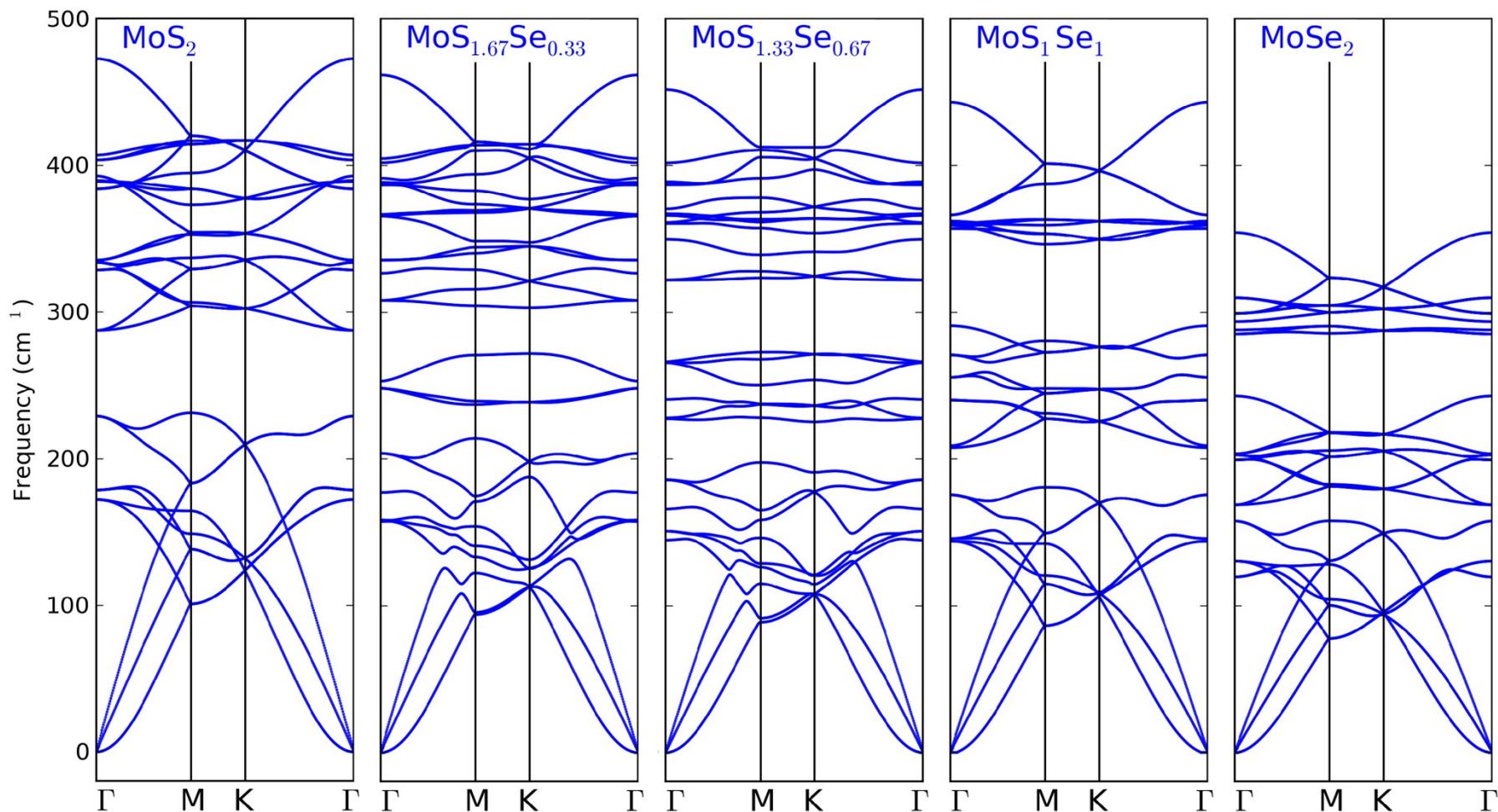
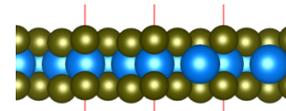
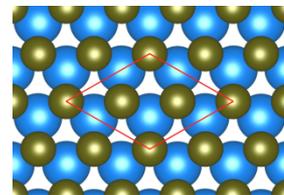
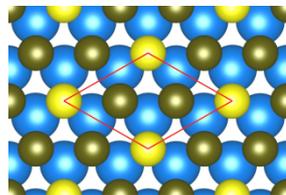
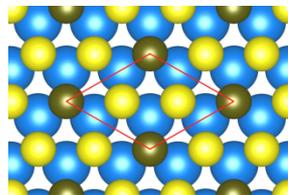
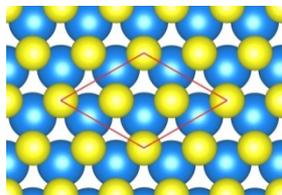


(a) Evolution of density of state of MoS<sub>2(1-x)</sub>Se<sub>2x</sub>. (b-d) Structures with x = 1/3, 1/2, and 2/3.

Below is the evolution of band structures of (6x6) supercell

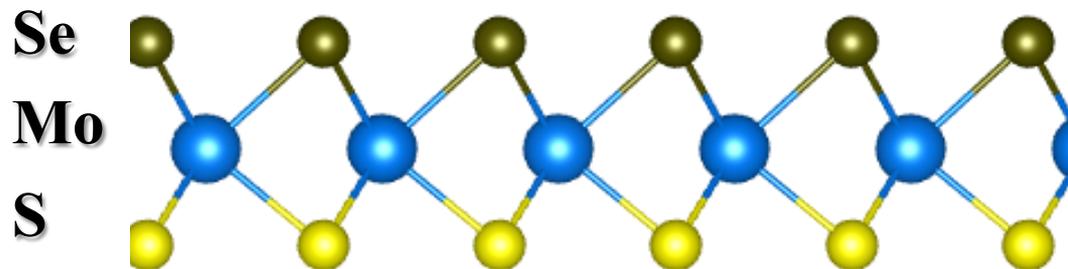
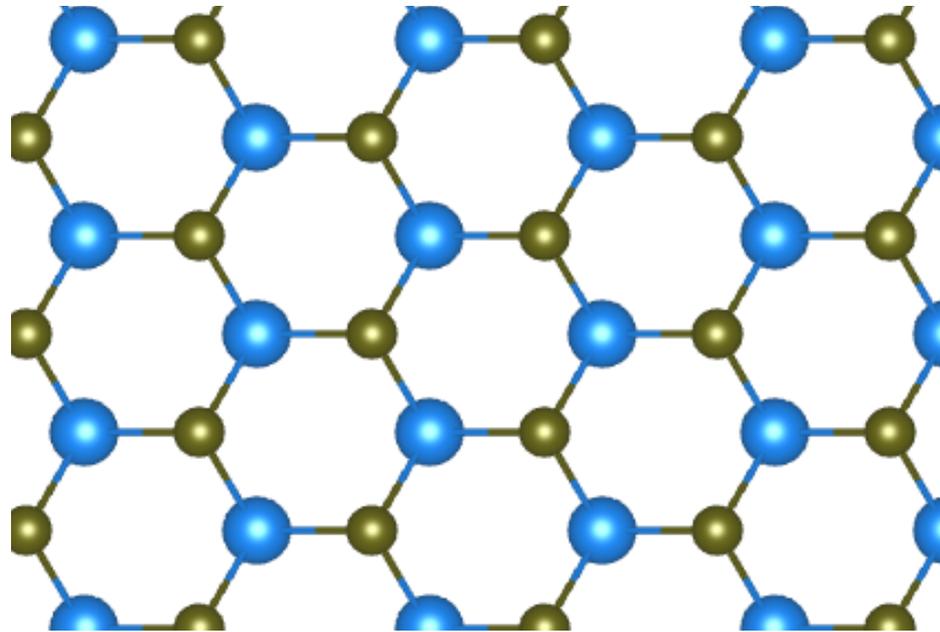


# Stability of $\text{MoS}_{2(1-x)}\text{Se}_{2x}$

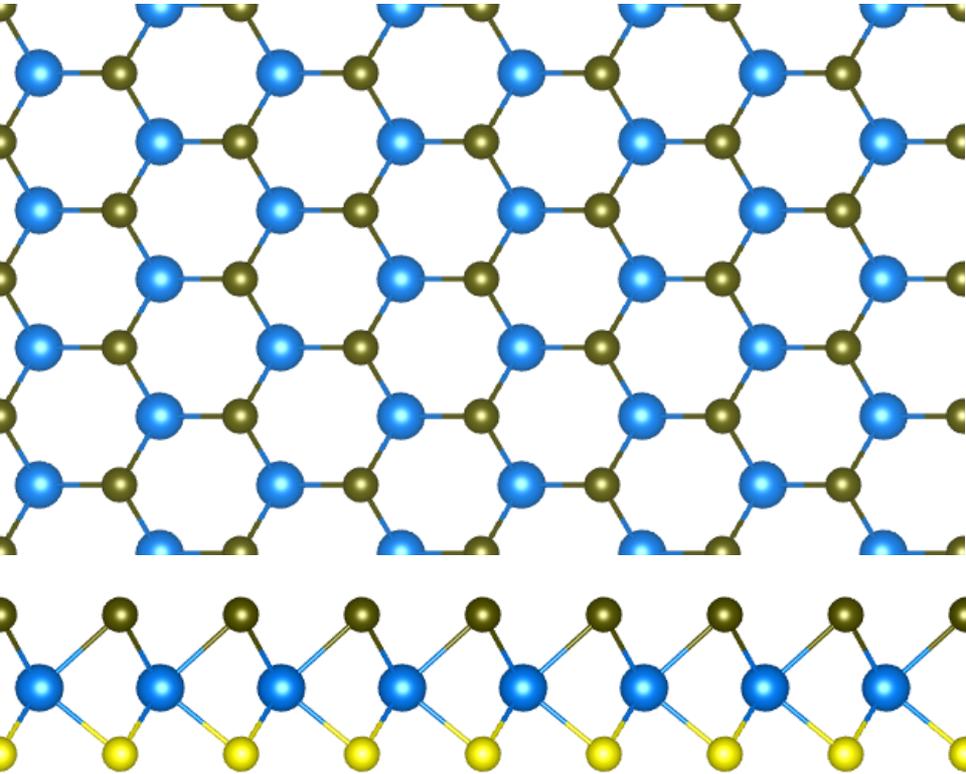


# Interesting question

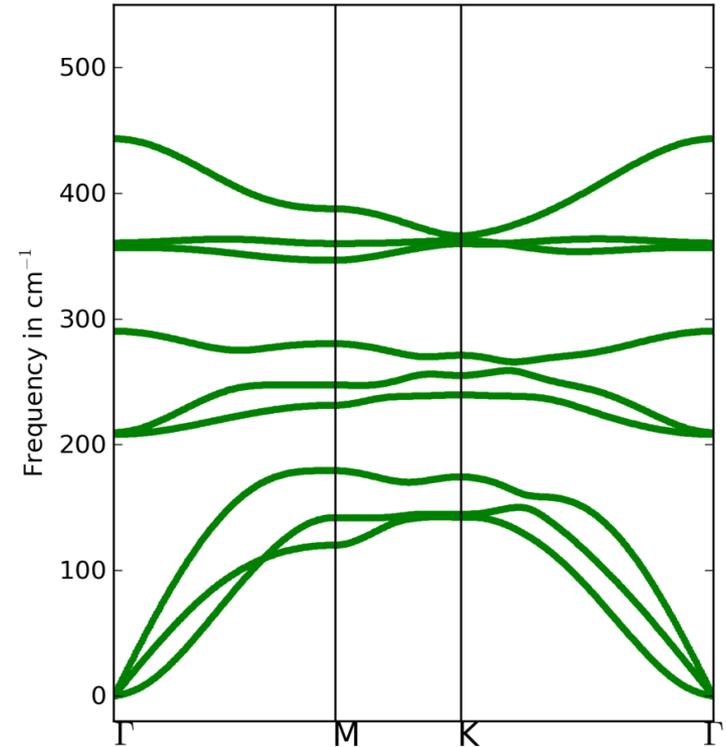
Can one make  $\text{MoS}_{2(1-x)}\text{Se}_{2x}$  alloys in which Se present only on the top layer?



# Stability of MoSSe



Phonon dispersion of  $\text{MoSS}_{(1-x)}\text{Se}_x$ ,  $x=1.0$



Phonon dispersion calculated with DFPT using  $12 \times 12 \times 1$  q-mesh.

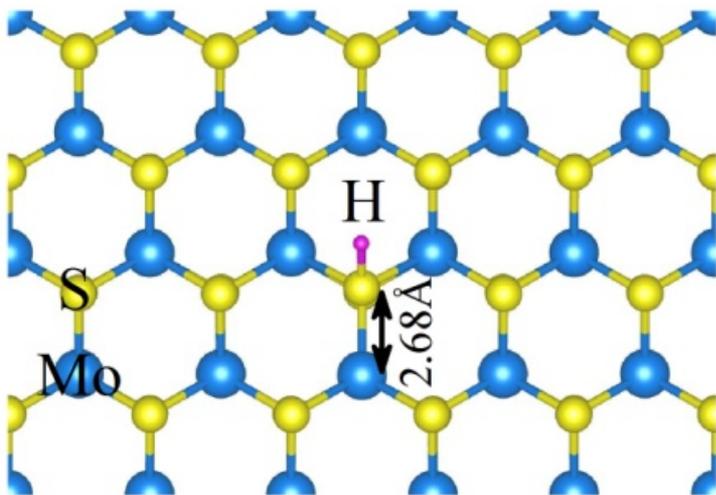
# Highlights

- Isotropic  $\text{MoS}_{2(1-x)}\text{Se}_{2x}$  has tuneable band-gaps
- Band-gap of polar  $\text{MoS}_{2(1-x)}\text{Se}_{2x}$  linearly varies with respect to Se concentrations.
- Variation of band-gap of polar  $\text{MoS}_{2(1-x)}\text{Se}_{2x}$  is the results of the competition between the effect of strain and that of Se concentration.
- Phonon dispersions are calculated for various  $\text{MoS}_{2(1-x)}\text{Se}_{2x}$ . We found no imaginary mode suggesting the stabilities of the material.

# **Hydrogenation/Flourination**

(with Ishigami group, UCF)

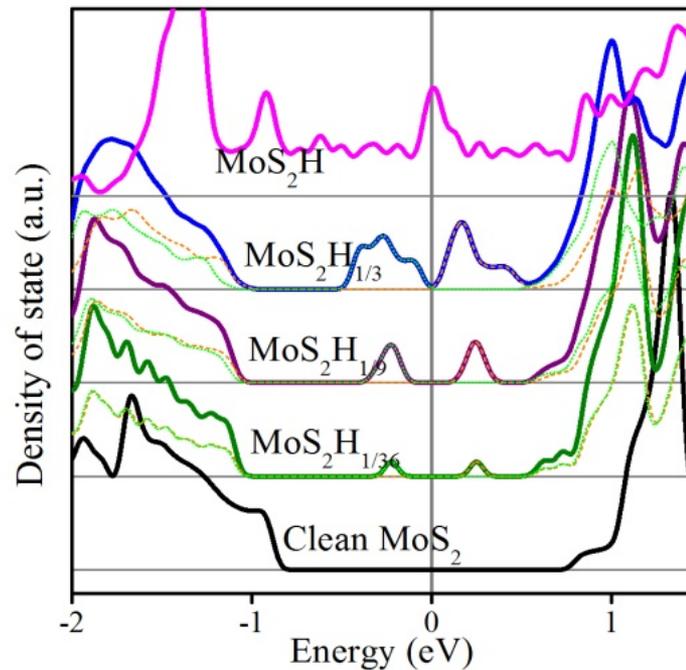
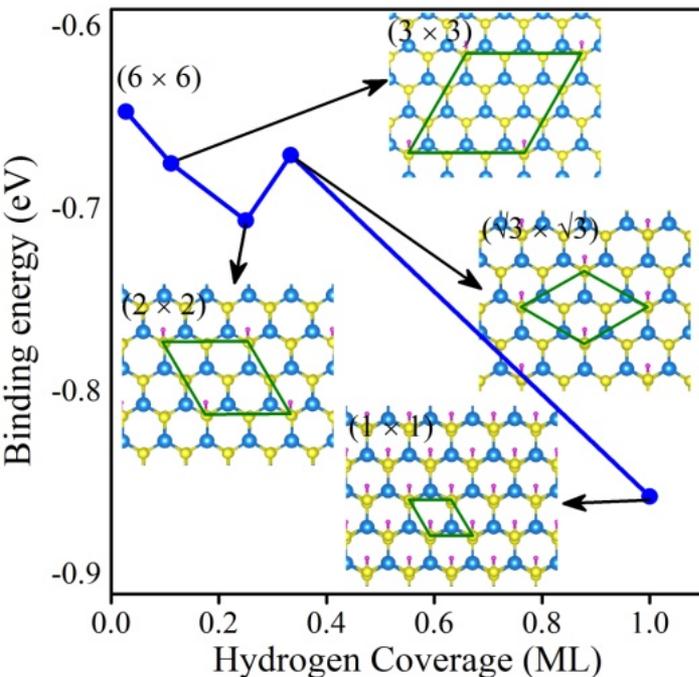
(with Ishigami group, UCF)



➤ S-H bonds prefer to be tilted an angle  $\beta$  with respect to the normal direction. The tilt angle is:  $\beta=46^\circ$ . This adsorption configuration is preferred over the reported configuration) by 140 meV.

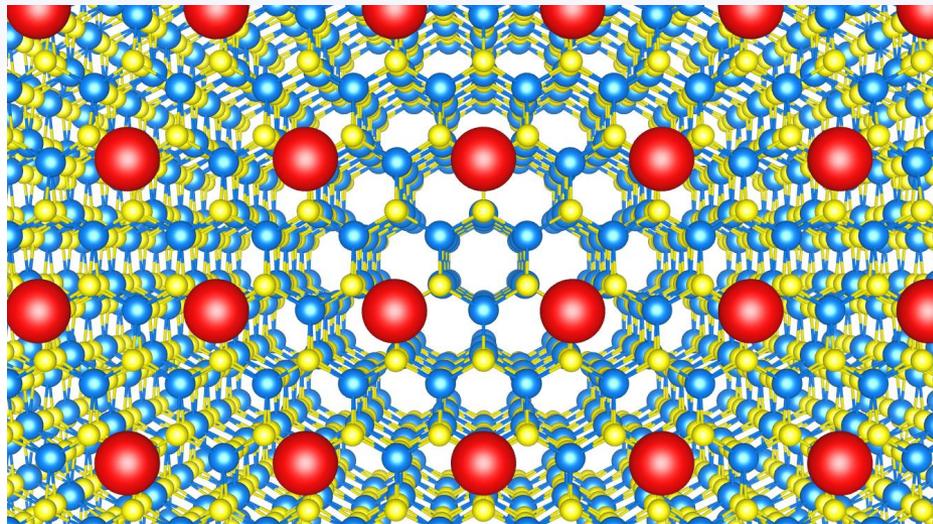
➤ the adsorption of H causes the deformation of MoS<sub>2</sub>. Mo-S bondlengths at the adsorption site increase from 2.41 Å (without H adsorption) to 2.44 Å and 2.68 Å, indicating the weakening Mo-S bond at the adsorption site.

➤ At low coverage (< 100%) The binding energy of an atomic H on MoS<sub>2</sub> is the lowest (most preferable) at  $\frac{1}{4}$  coverage (left figure below). However, the binding energy of H on MoS<sub>2</sub> is the lowest when (1×1) structure formed (Will discuss about this later). The evolution of density of electronic states as increasing H coverage is shown in the right figure below. Note that, in the case of MoS<sub>2</sub>H<sub>1/36</sub>, MoS<sub>2</sub>H<sub>1/9</sub>, and MoS<sub>2</sub>H<sub>1/3</sub>, the mid-gap states are spin-polarized: spin-up is occupied and spin down is un-occupied (dot and dash lines, respectively).



# Na doping of MoS<sub>2</sub> ARPES & DFT

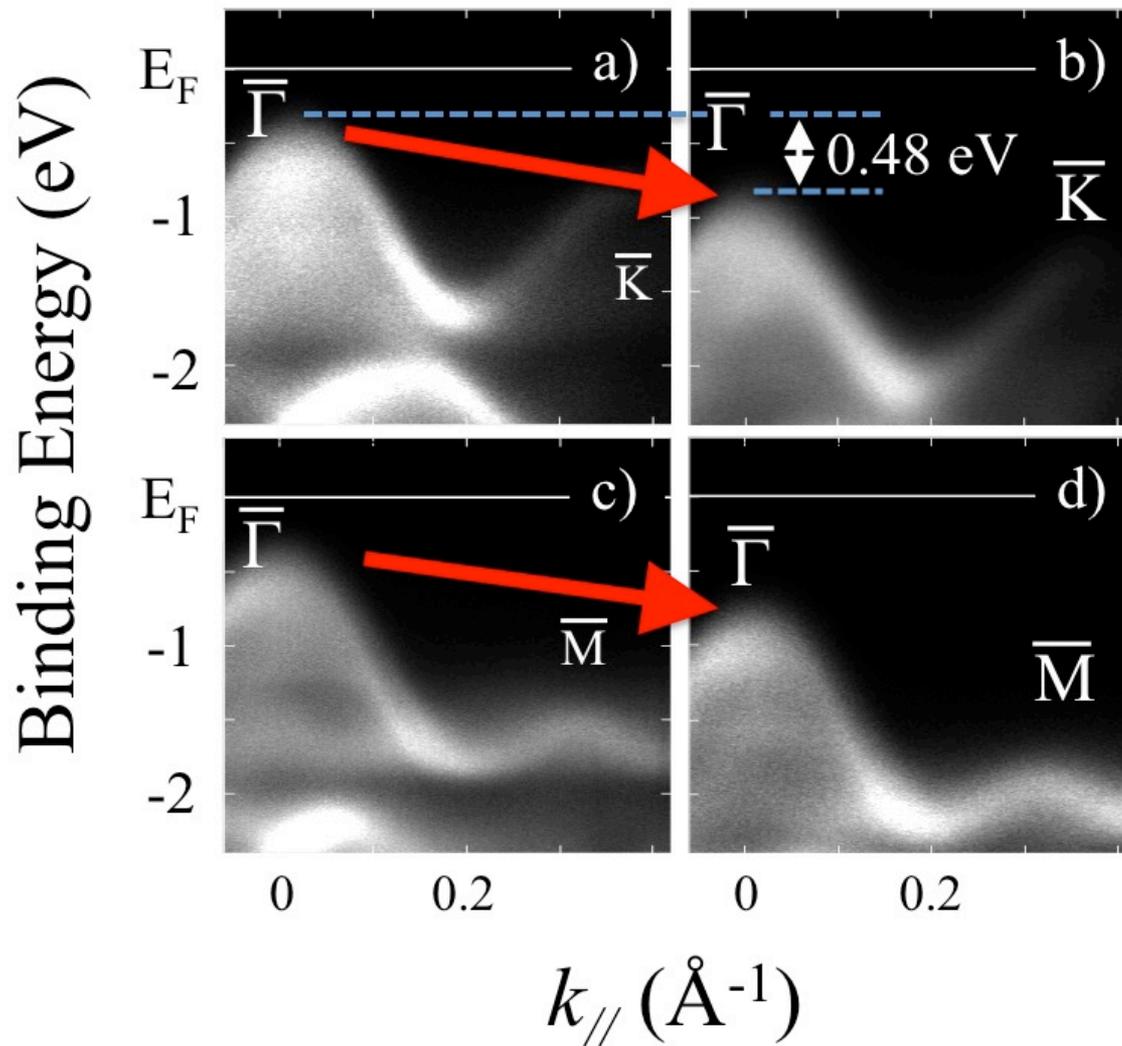
(With Peter Dowben group, U Nebraska)



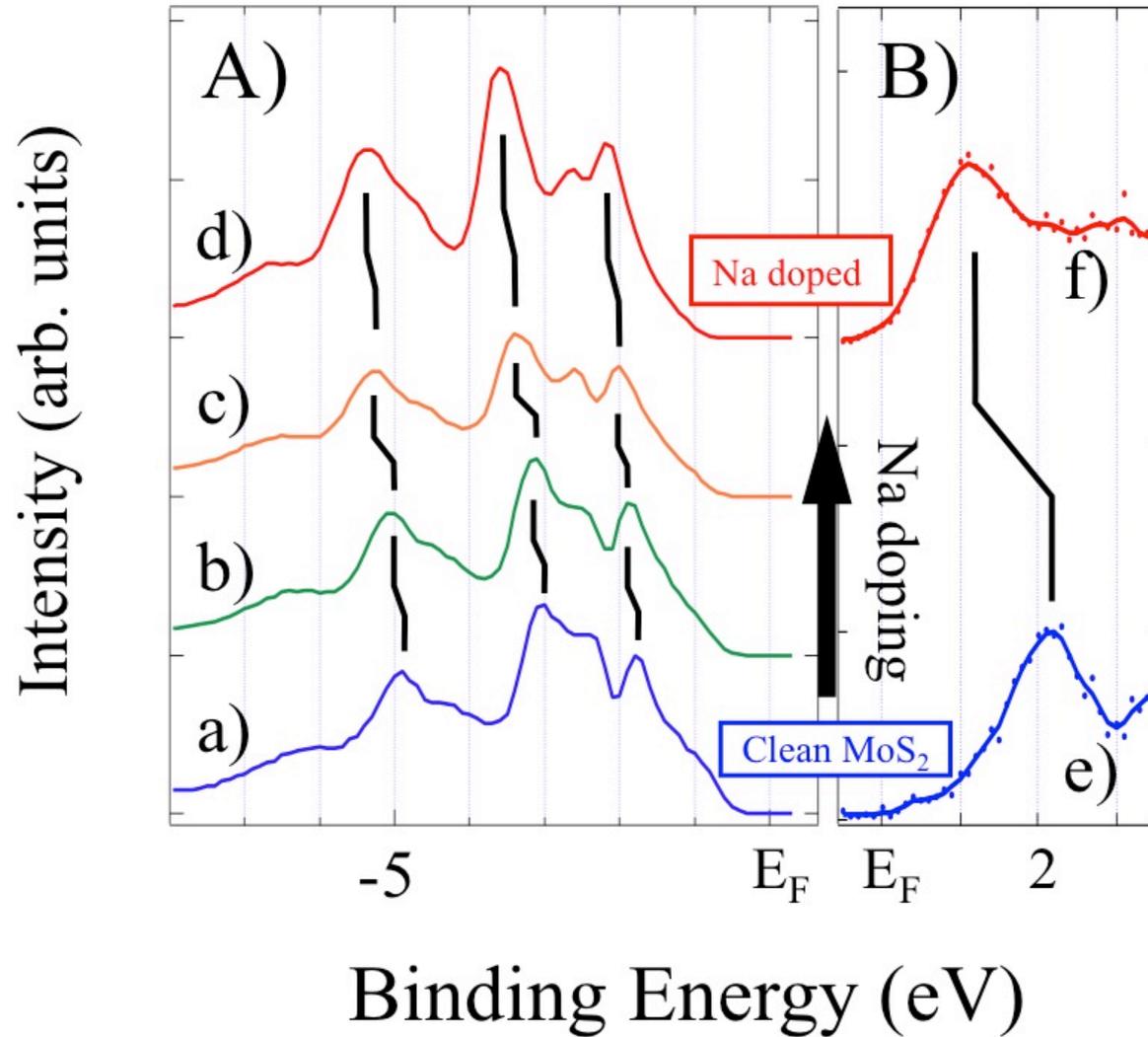
# METHODS

- Theory: DFT with van der Waals interaction
- Experiment:
  - High-resolution angle-resolved photoemission spectroscopy (ARPES) (HiSOR, Japan)
  - Unoccupied state spectra were acquired in separate ultrahigh vacuum systems equipped with the inverse photoemission (IPES), low energy electron spectroscopy (LEED) and x-ray photoemission spectroscopy (XPS).

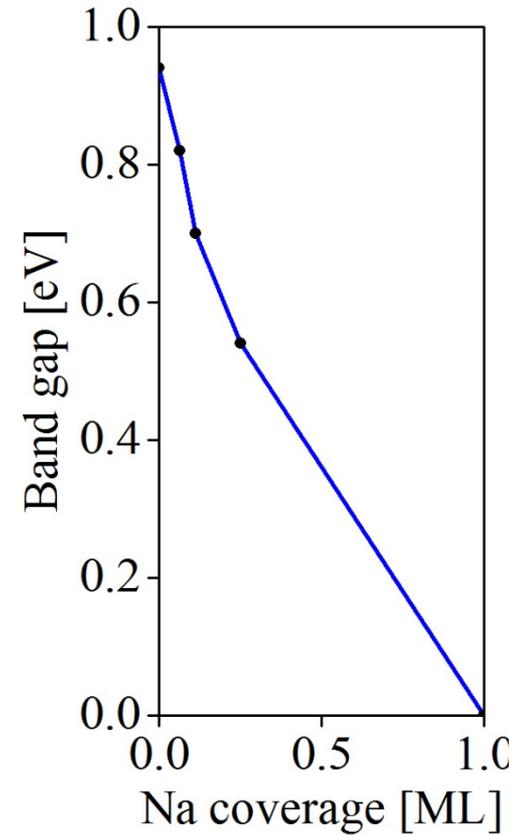
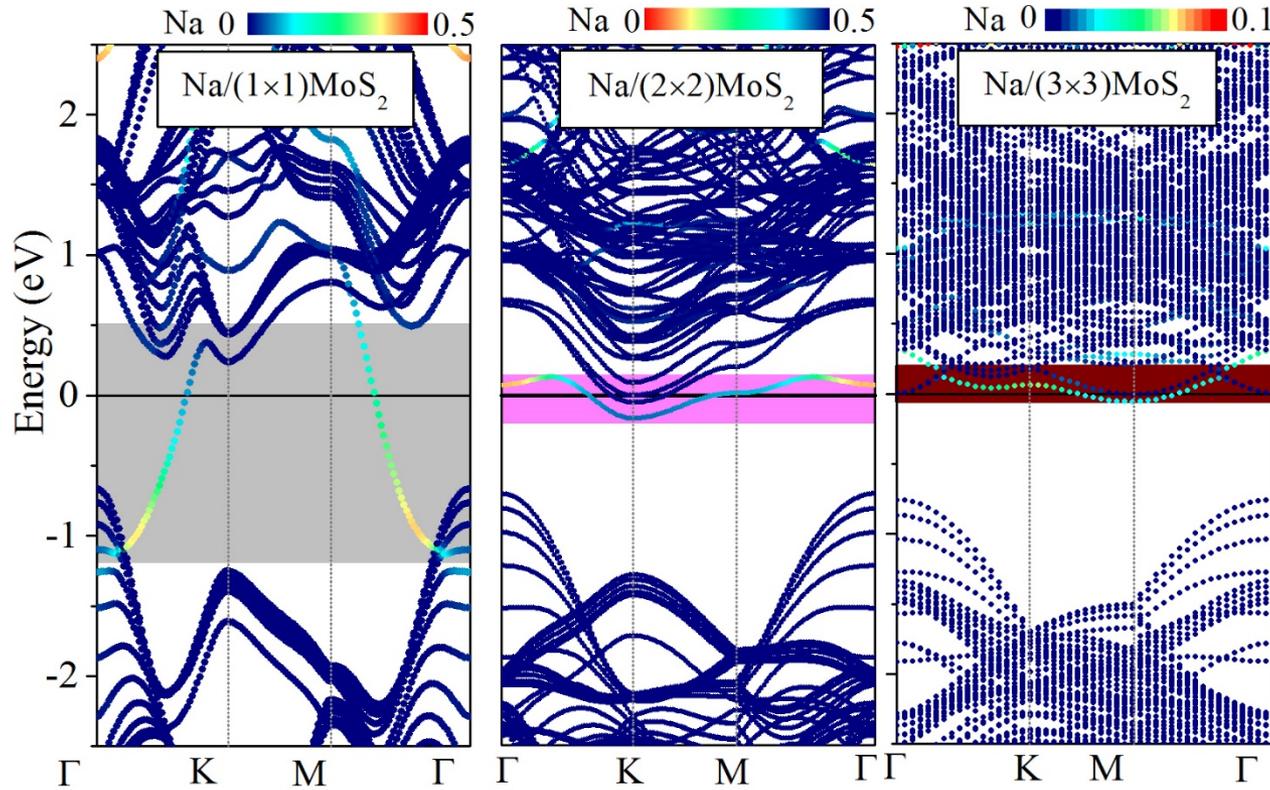
# Na/MoS<sub>2</sub>(0001): Occupied bands



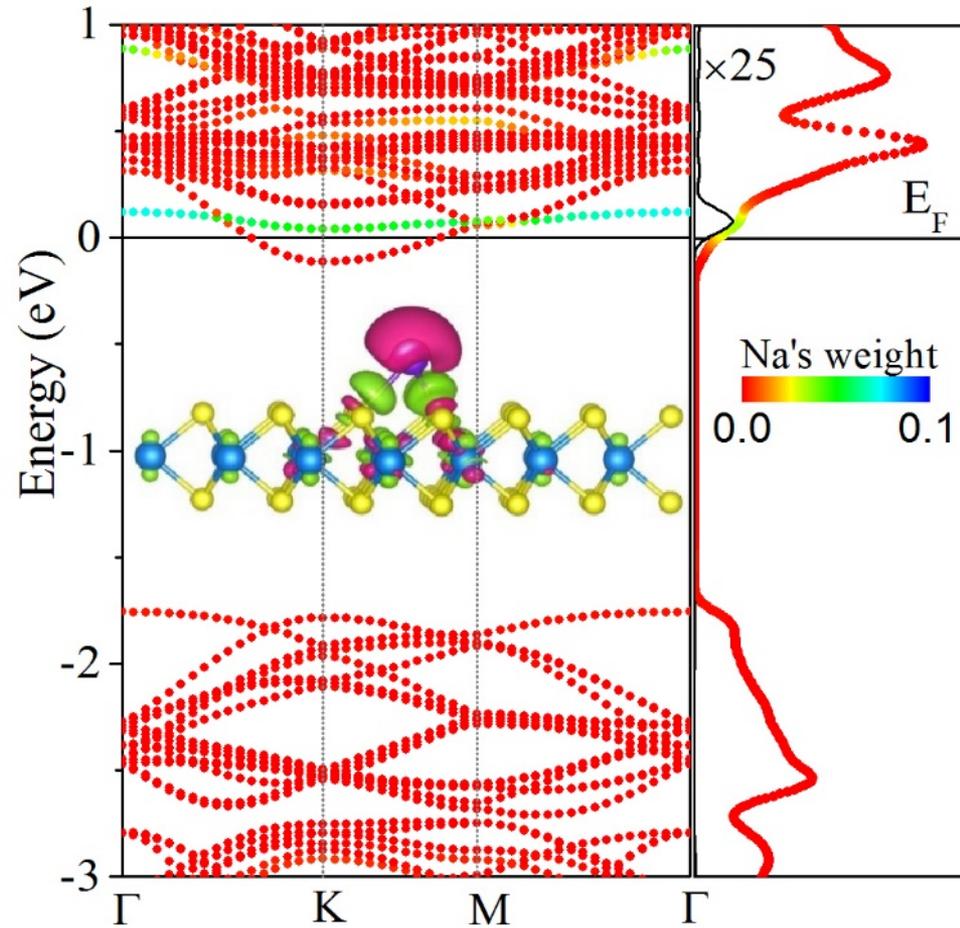
# Na Doped MoS<sub>2</sub>(0001): Spectra



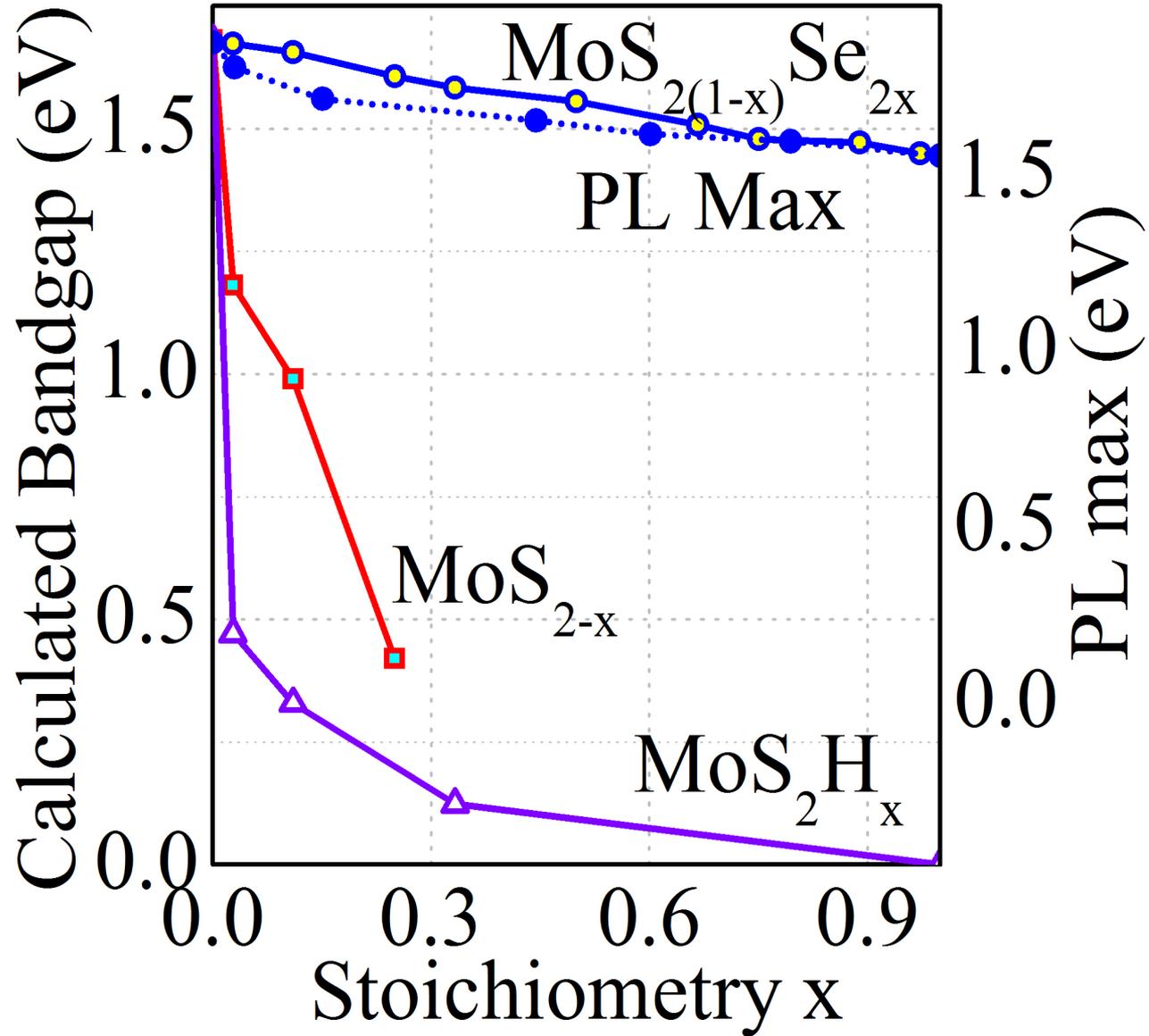
# Na/MoS<sub>2</sub>(0001): Band Structure



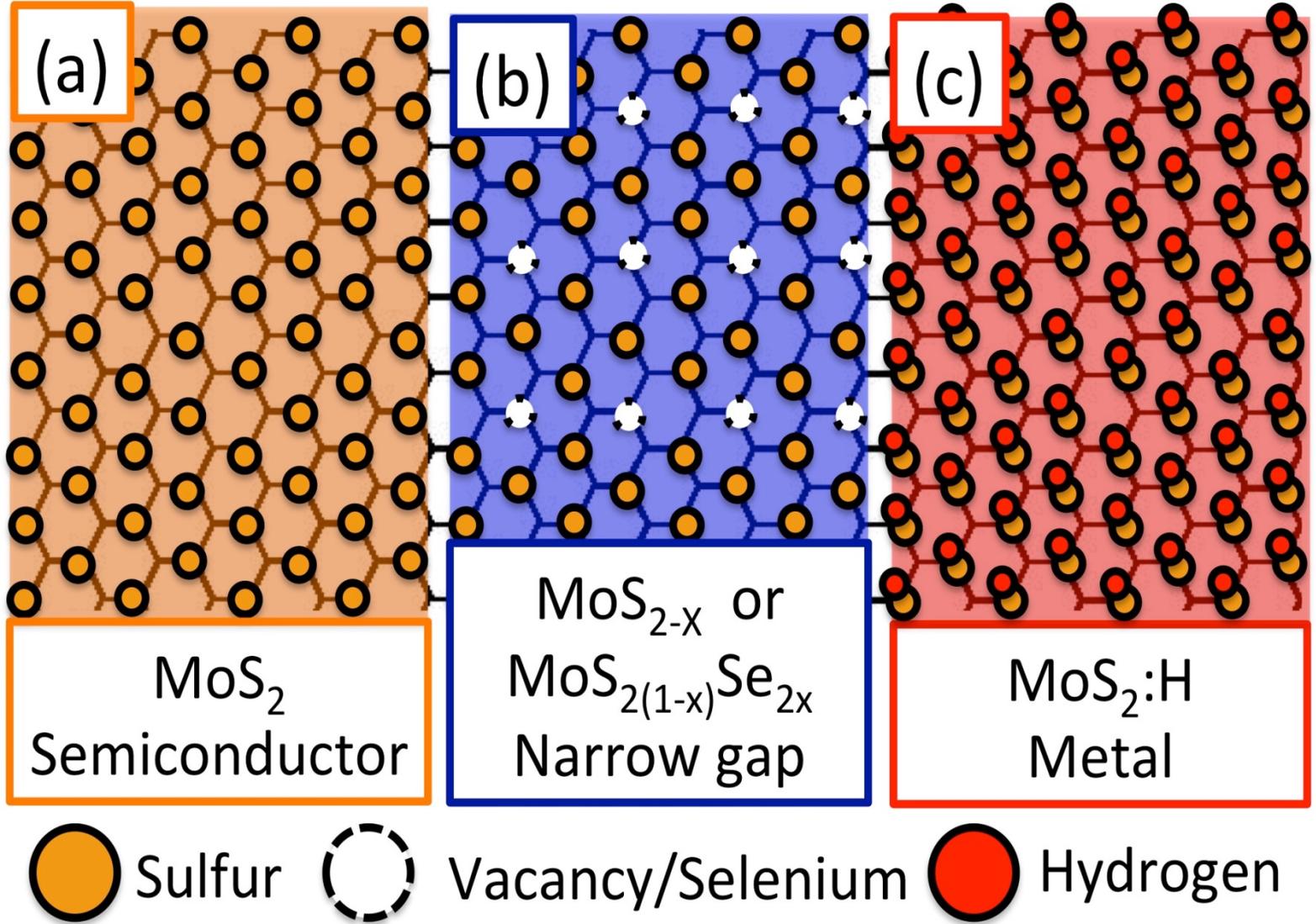
# Na/Single Layer MoS<sub>2</sub>: Charge transfer



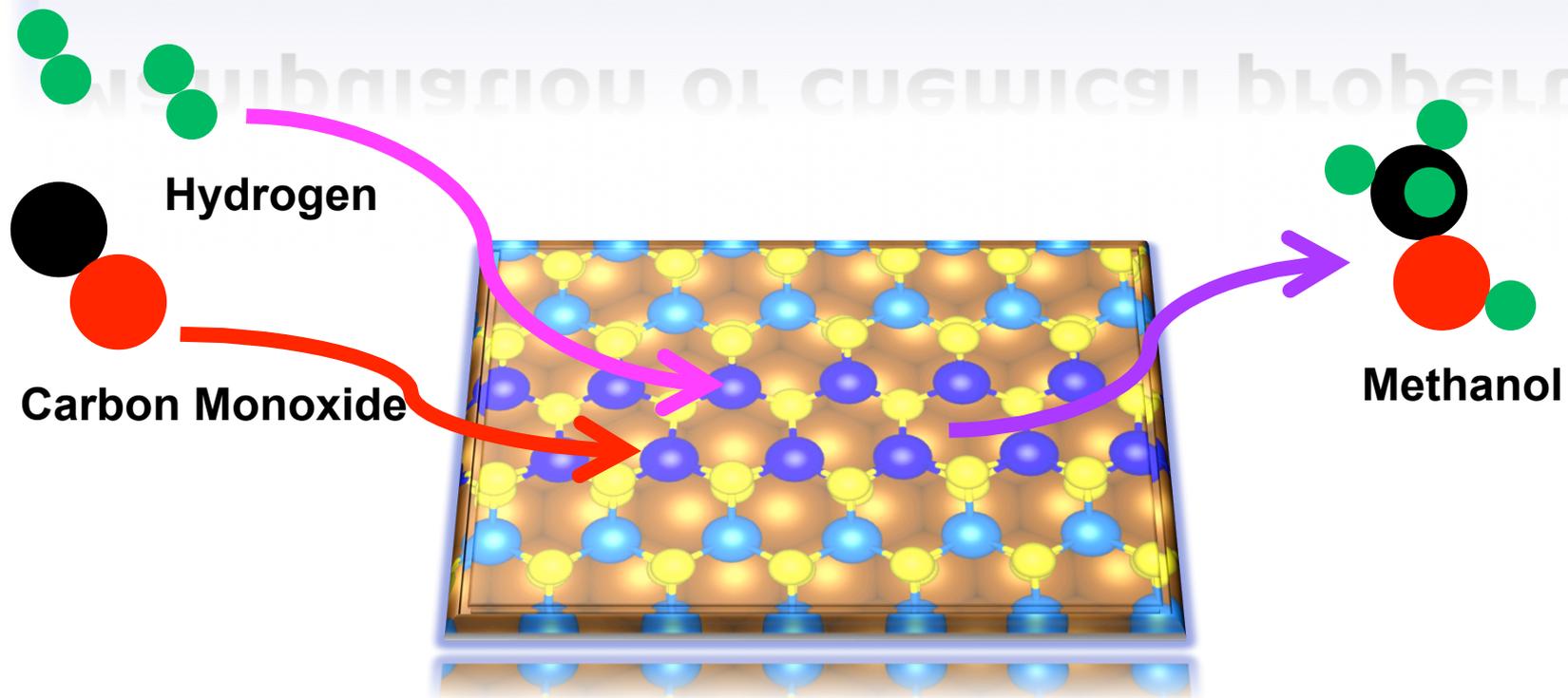
# Calculated Band Gaps for Functionalized MoS<sub>2</sub>



# Summary: Functionalization of Molybdenene

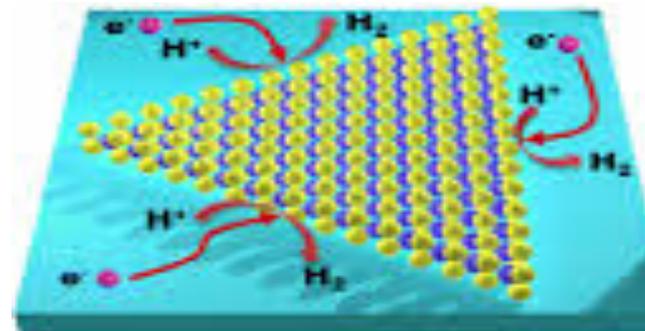


# Manipulation of chemical properties

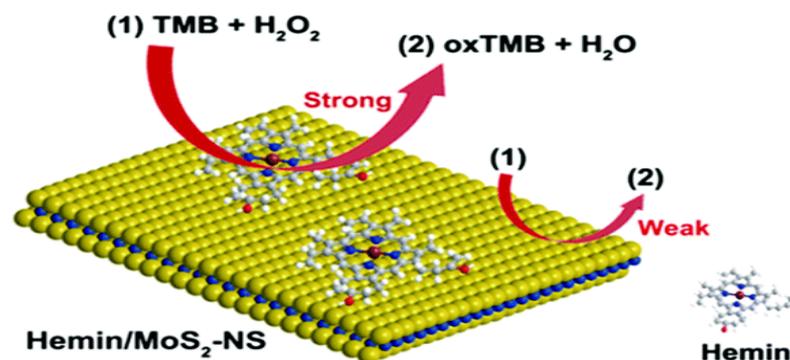


# Chemistry on Single-layer MoS<sub>2</sub>

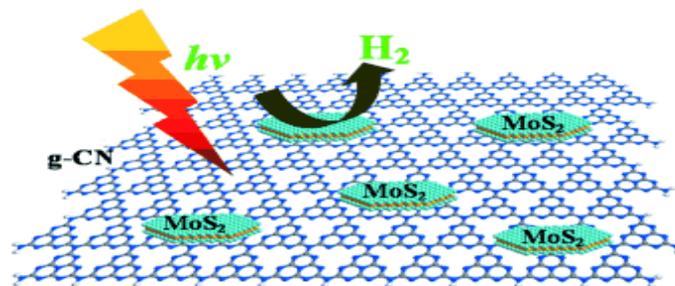
Controllable Growth and Transfer of Monolayer MoS<sub>2</sub> on Au Foils and Its Potential Application in Hydrogen Evolution Reaction, J. Shi et al., *ACS Nano*, **8**, (2014), 10196



Hemin-functionalized MoS<sub>2</sub> nanosheets: enhanced peroxidase-like catalytic activity with a steady state in aqueous solution, B. L. Li, *RSC Adv.*, **4**, (2014) 24256



Layered Nanojunctions for Hydrogen-Evolution Catalysis, H. Yidong et al., *Ang. Chem. Int. Ed.*, **52**, (2013), 3621



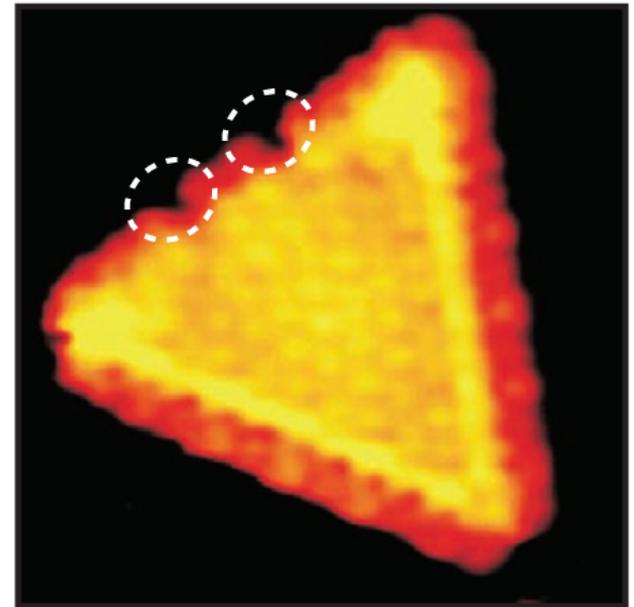
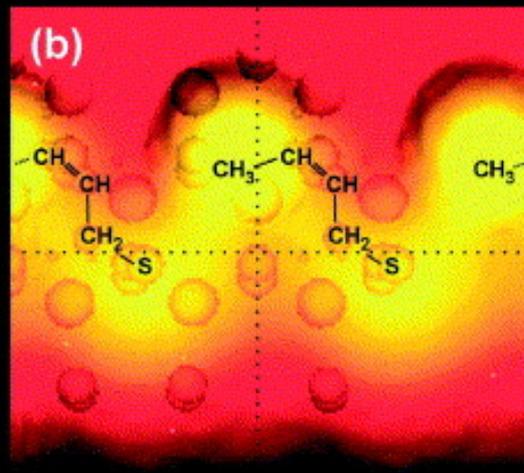
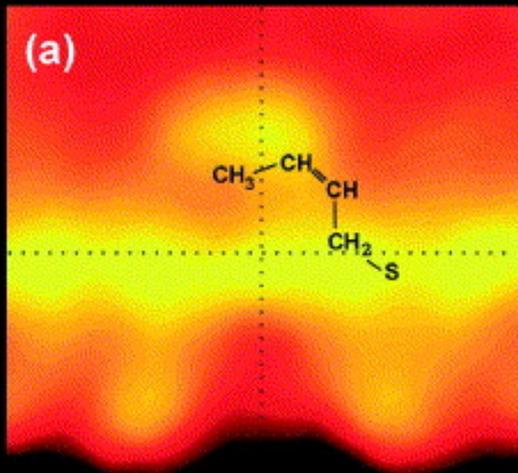
**Is it the edge?  
Vacancies?  
Metallic Support?  
Interface with nanoparticle?**

Interface with nanoparticles?  
Metallic support?

# MoS<sub>2</sub> for Hydro-desulfurization

Hydro-desulfurization reaction on MoS<sub>2</sub> nanoclusters:

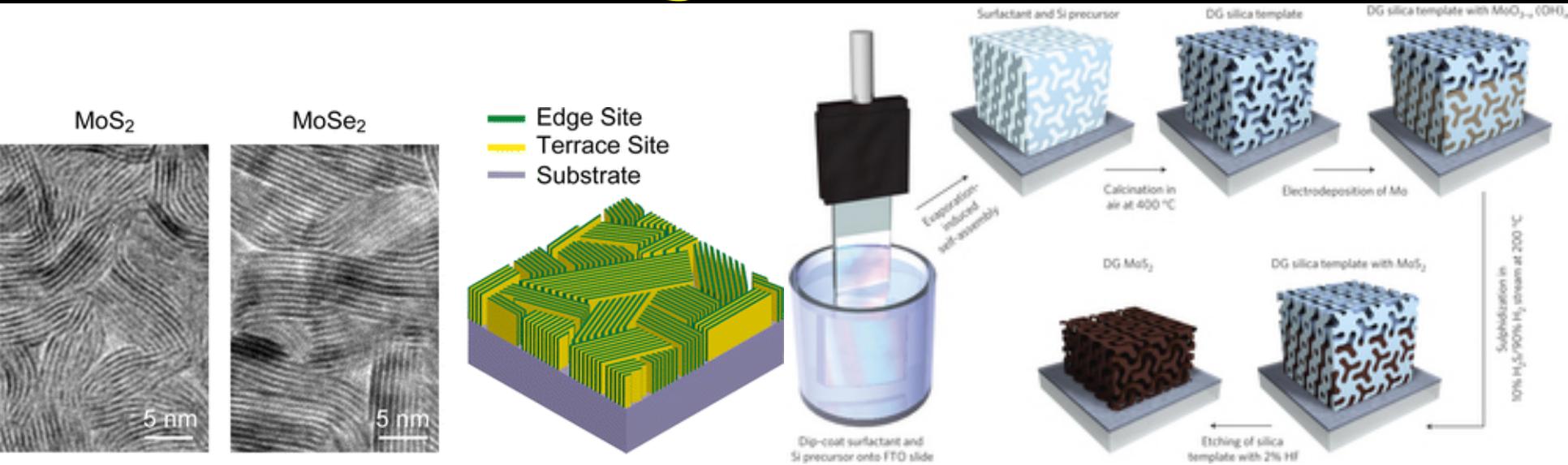
Edges are the reaction sites



J. V. Lauritsen *et al.*, *J. Catal.* (2004).

J. Kibsgaard, PhD Thesis (2008)

# Create edges for reactions



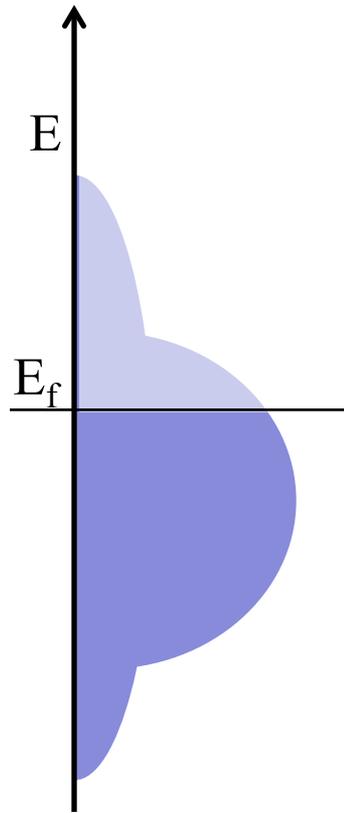
Synthesis of MoS<sub>2</sub> and MoSe<sub>2</sub> Films with Vertically Aligned Layers

D. Kong *et al.*, *Nano Lett.* (2013).

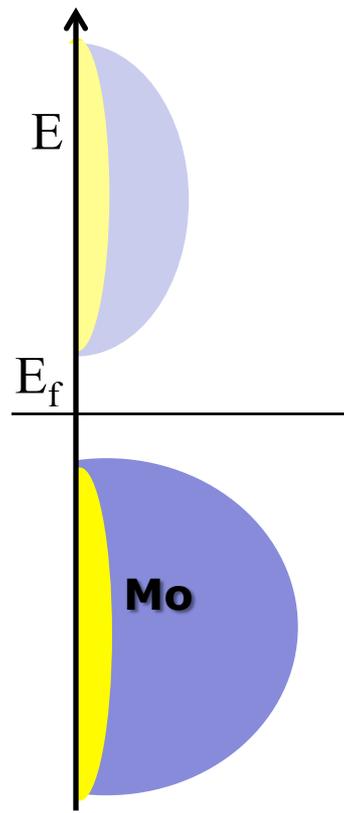
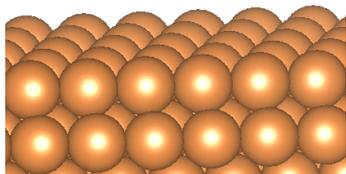
Engineering the surface structure of MoS<sub>2</sub> to preferentially expose active edge sites for electrocatalysis

J. Kibsgaard *et al.*, *Nature Mater.* (2012).

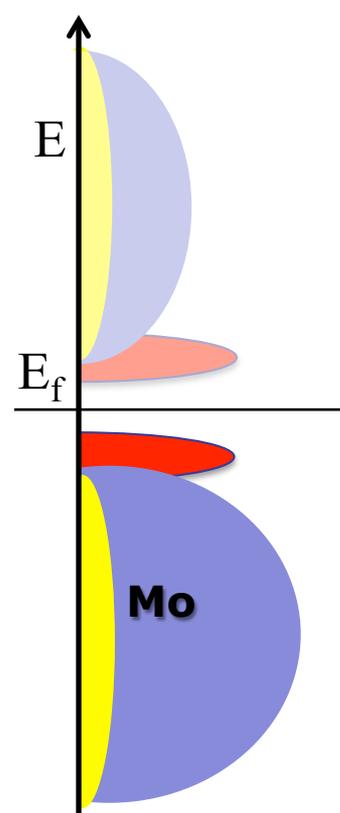
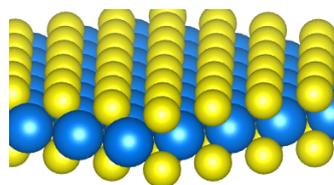
# Manipulating Chemical Reactivity



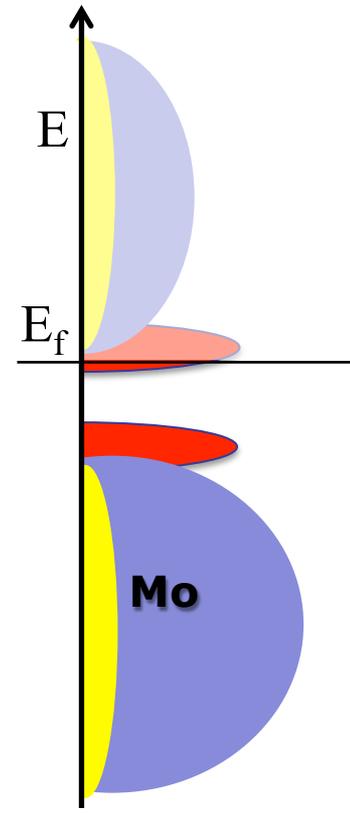
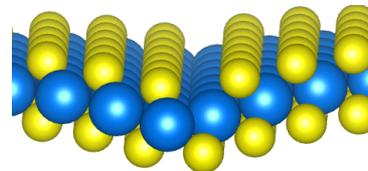
Transition  
Metal



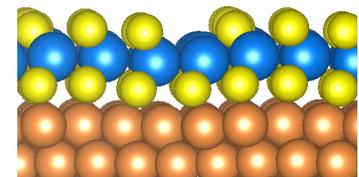
$\text{MoS}_2$



$\text{MoS}_2$   
with S vacancy row



$\text{MoS}_2$   
with S vacancy row  
on Cu(111)



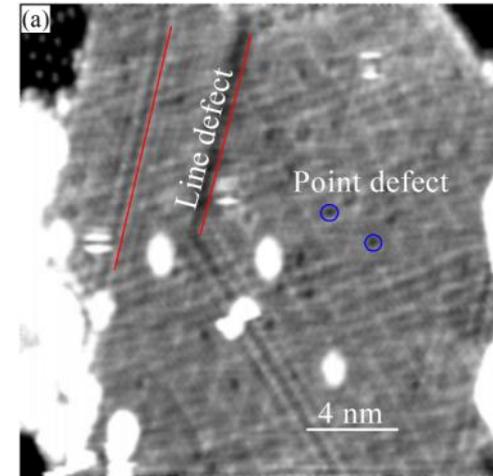
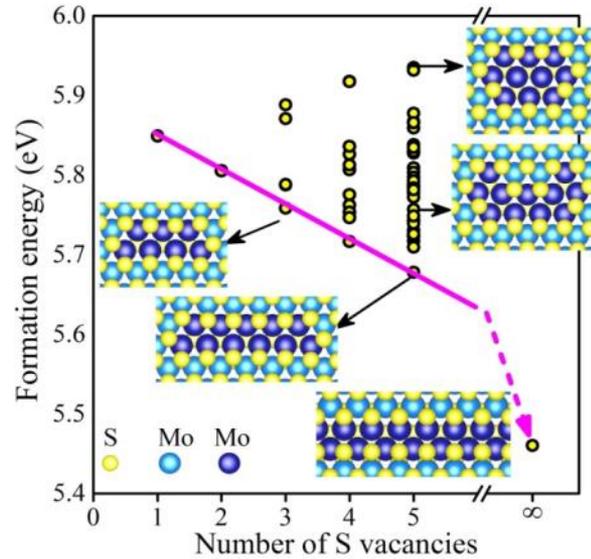
# Remarks

➤ Sulfur vacancies tend to form row structures.

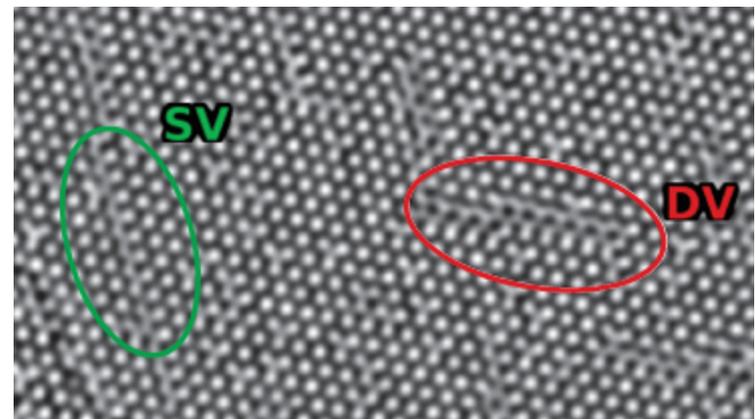
- Formation energy is lowest when sulfur vacancies form row.

➤ The longer the row structure, the more stable it is

- Barrier for diffusion of an nearby S atom to sulfur vacancy row increases as the row elongates.
- The reversed barrier is always lower.



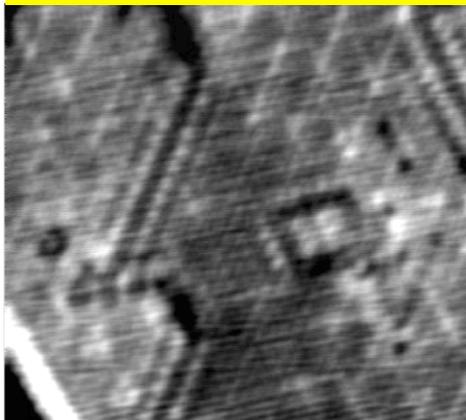
L. Bartels' group



Komsa et al, 2013

# Electronic Structure of Defect-laden MoS<sub>2</sub>

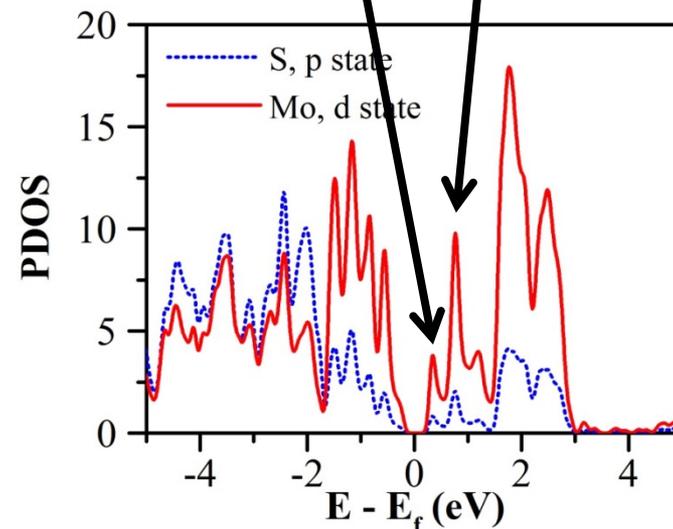
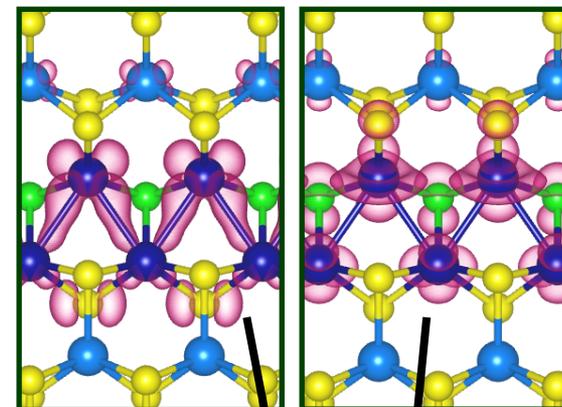
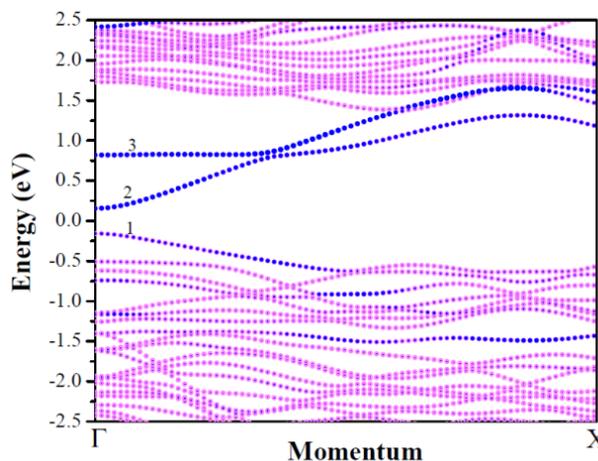
## MoS<sub>2</sub> on Cu(111)



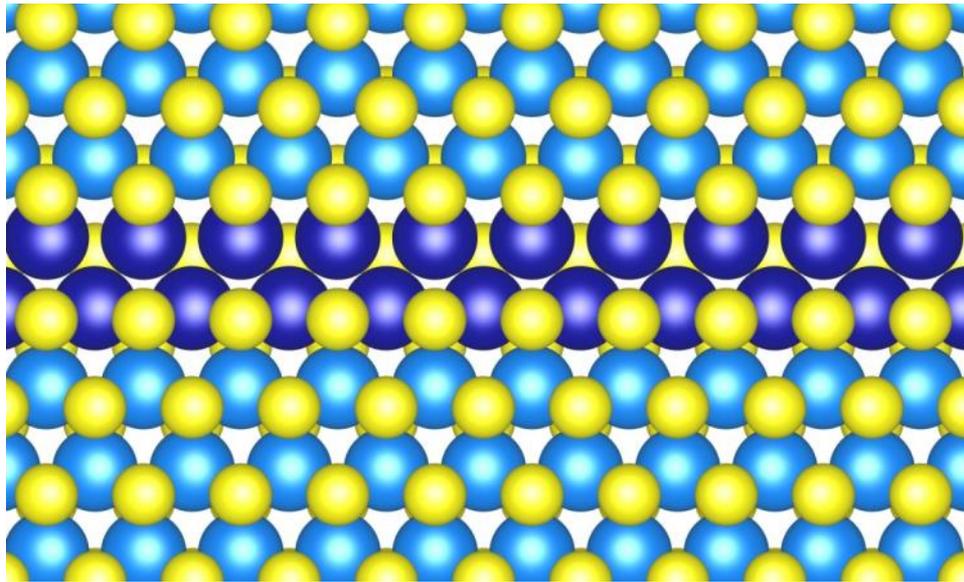
D. Le, T. B. Rawal, T. S. R,  
*Jour. Phys. Chem C*, **118**, (2014), 5346

From L. Bartels group

- Both theoretical and experimental findings clearly indicate that line defect (S-vacancy row) forms on MoS<sub>2</sub>.
- DFT results show that “defect states” are predominantly Mo d orbitals, that will participate in bonding.

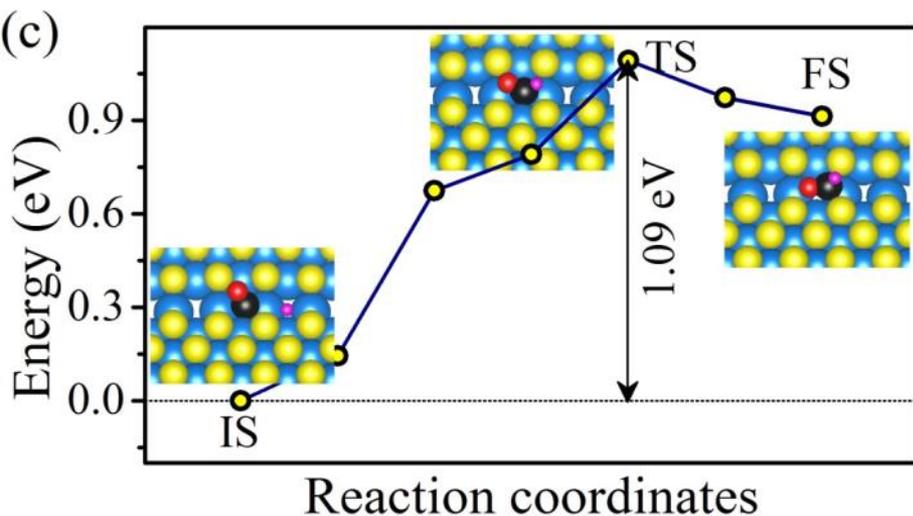
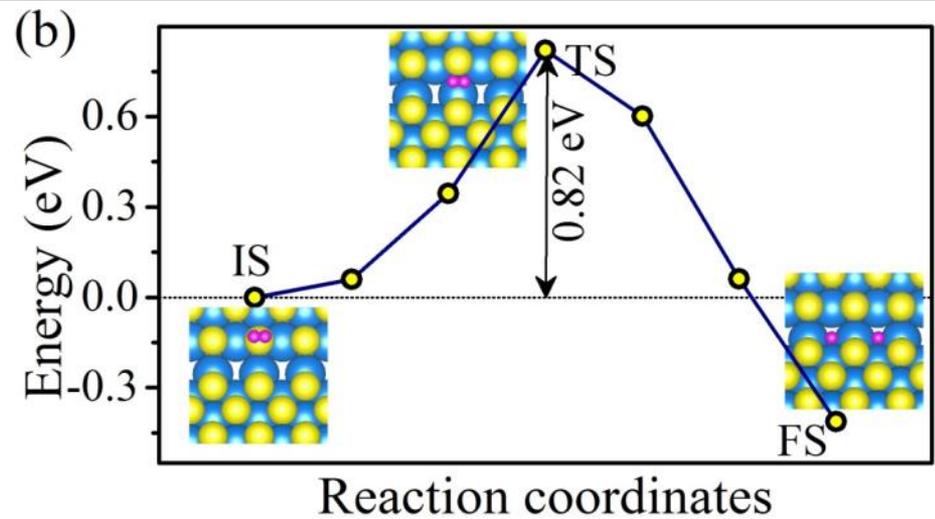
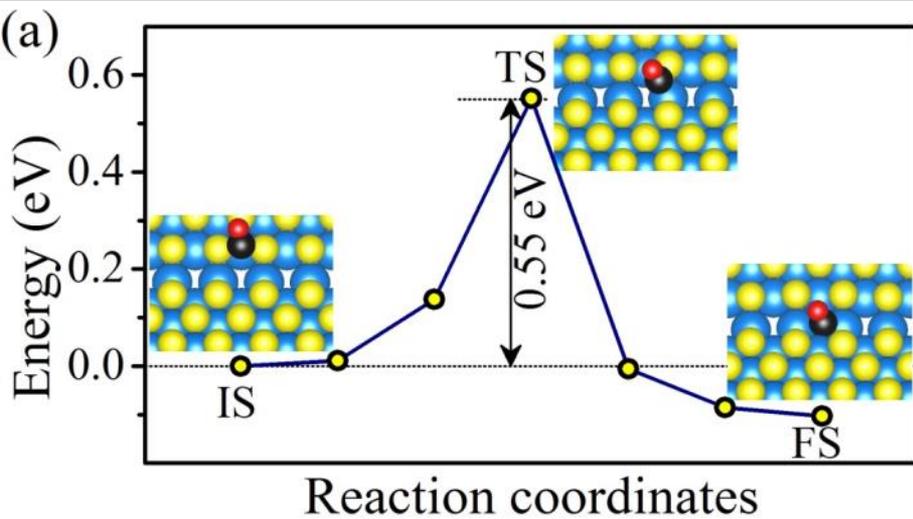


# Model system: MoS<sub>2</sub> with S vacancy row



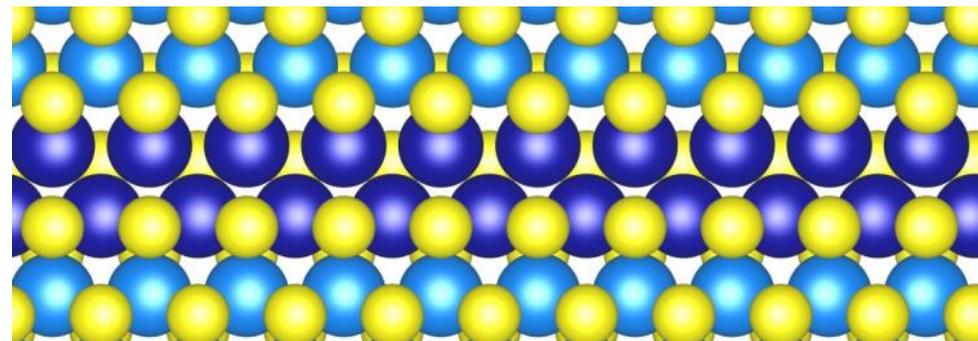
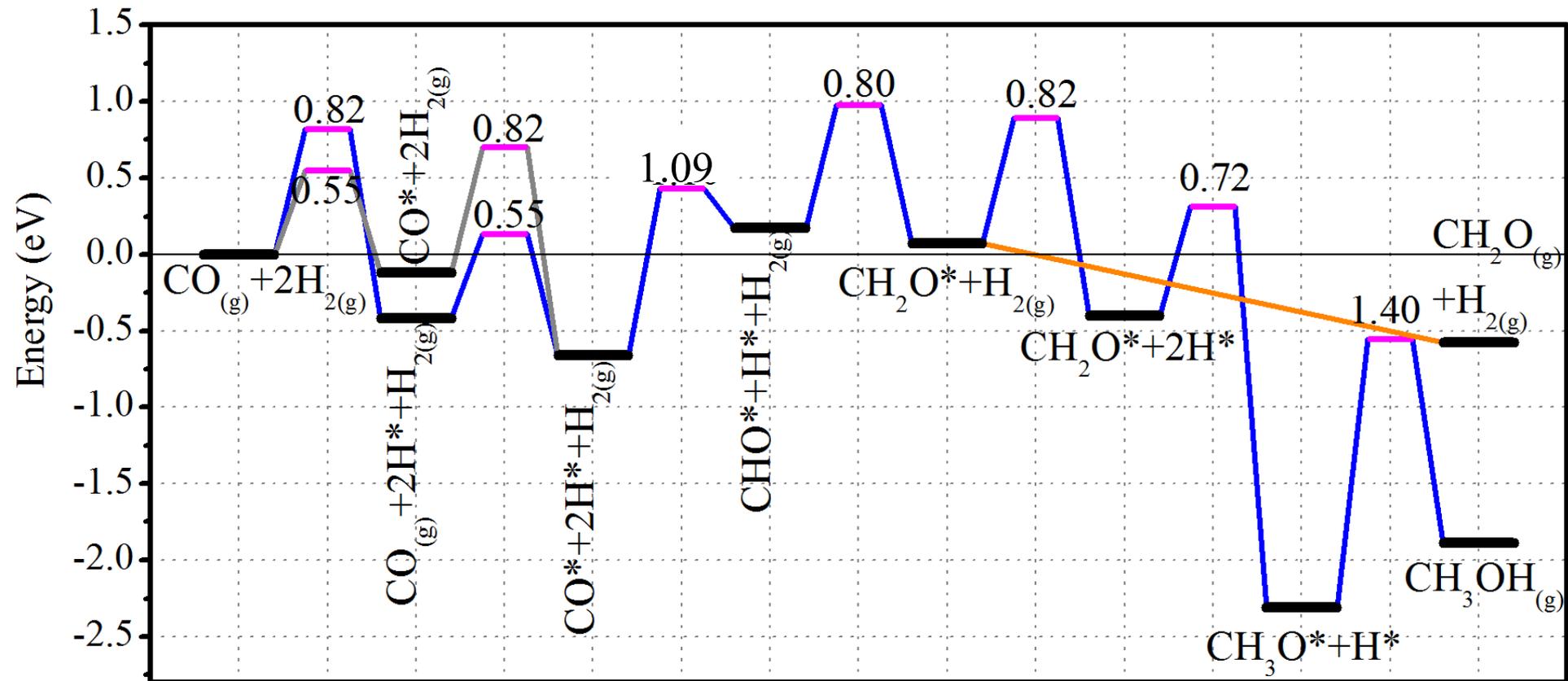
- Sulfur vacancies: Mo atoms and their *d* electrons are exposed to adsorbates.
- Sulfur vacancies: Possible catalyst.
- We examine the CO hydrogenation reaction, as an example.

# RESULTS: CO hydrogenation

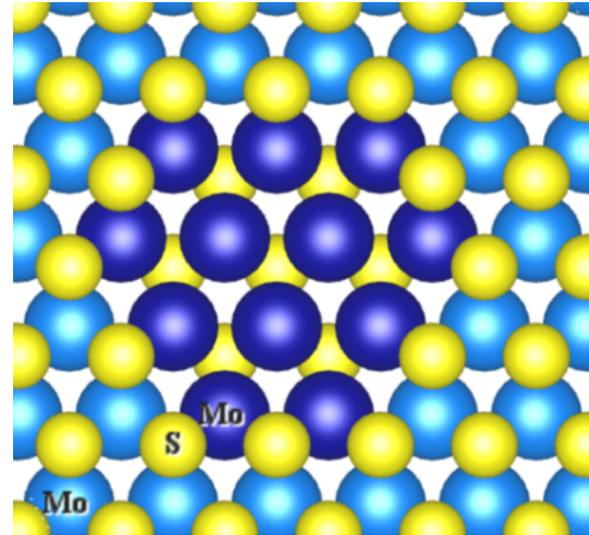


(CI)-NEB results of the adsorption of CO (a), dissociative adsorption of  $H_2$  (b), and the formation of  $CHO^*$  (c) on  $MoS_2$  with sulfur vacancy row. **Cyan, yellow, black, red, and magenta** (smallest) balls represent **Mo, S, C, O, and H** atoms, respectively.

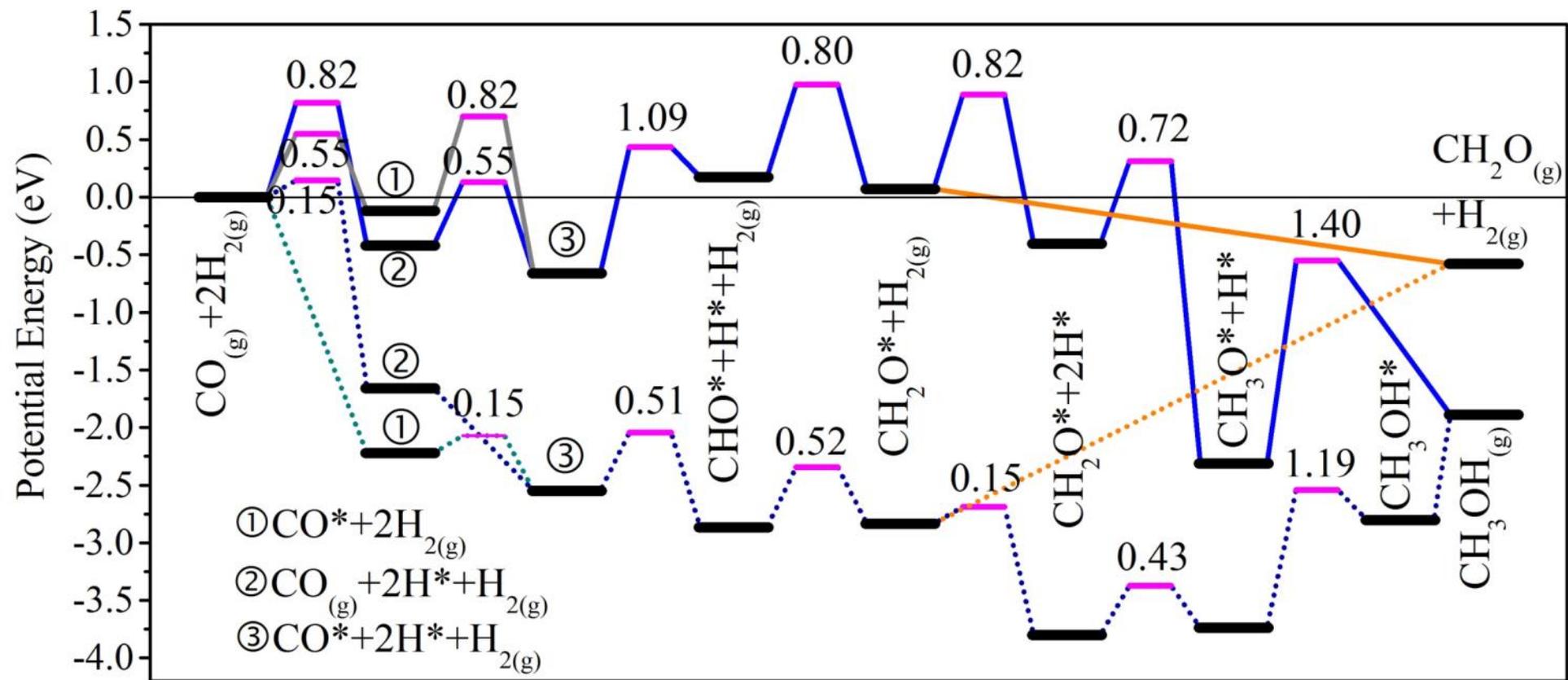
# RESULTS: CO hydrogenation



- The barriers are high  $\Rightarrow$  S-vacancy row may not be a good candidate for MeOH synthesis from CO and  $H_2$
- Main parameters controlling reaction: Barrier of H diffusion. Most of processes are H diffuse to CO, CHO,  $CH_2O$ ,  $CH_3O$  to hydrogenate.
- The high barrier is due to the narrow size of the S-vacancy row  $\Rightarrow$  One can manipulate the distribution of S-vacancy for obtaining better results.



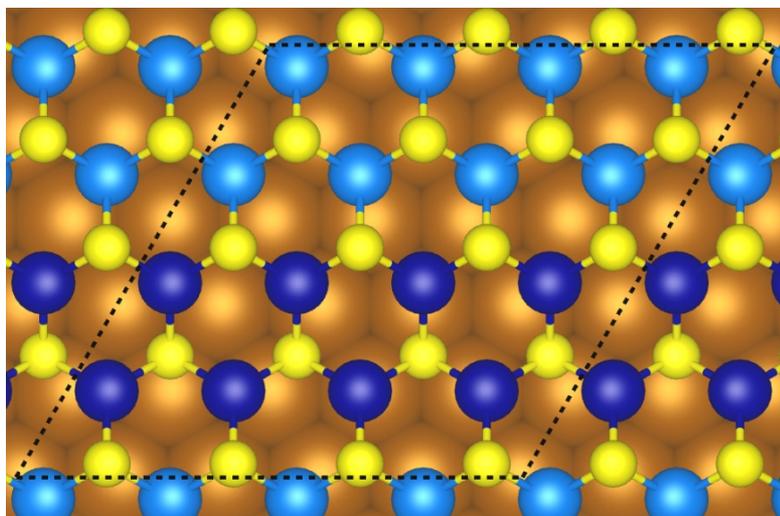
Formation energy of vacancy structures other than row is not much higher than that of row structure  $\Rightarrow$  possibility of their existences.



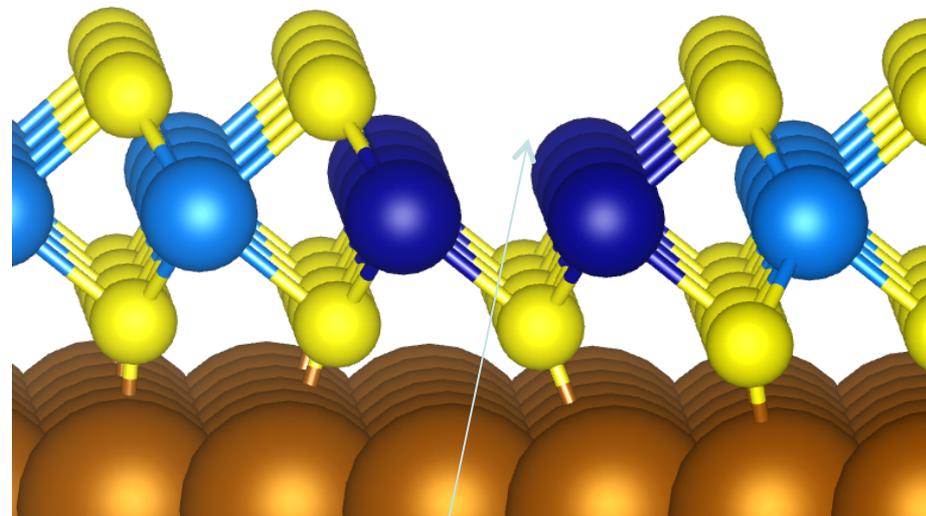
Potential energies along the reaction pathway of the formation of  $\text{CH}_3\text{OH}$  via the  $\text{CO}$  hydrogenation on  $\text{MoS}_2$  with a row of sulfur vacancies (Solid connections) and with a patch of 7 sulfur vacancies (dotted connections). Thicker-longer bars represent the intermediate states while thinner-shorter bars represent transition states. Numbers (in eV) are energetic barriers. Superscript \* indicates adsorbed specie. Subscript (g) indicates gas phase.

# Model system: MoS<sub>2</sub> with S-vacancy row on Cu(111)

Top View



Side View

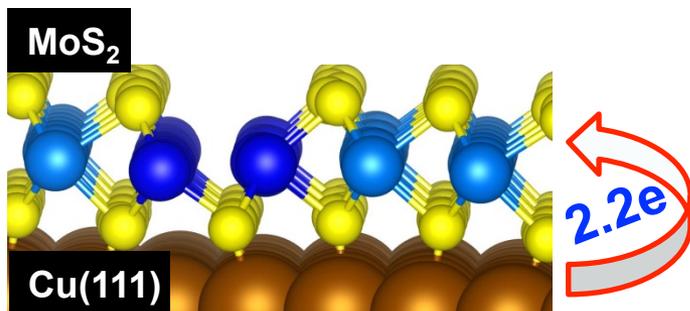


-  Mo atom
-  Exposed Mo atom near the S-vacancy
-  Sulfur atom

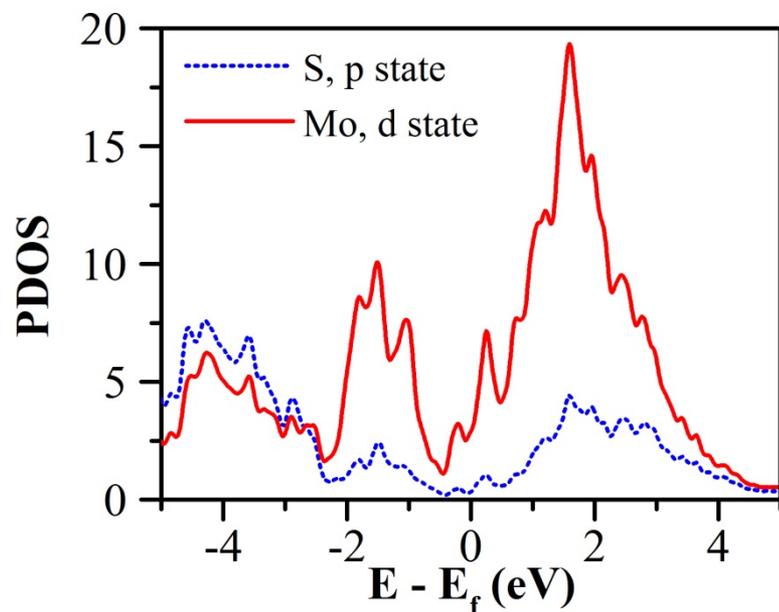
**S**  
**vacancies**

# Electronic Structure

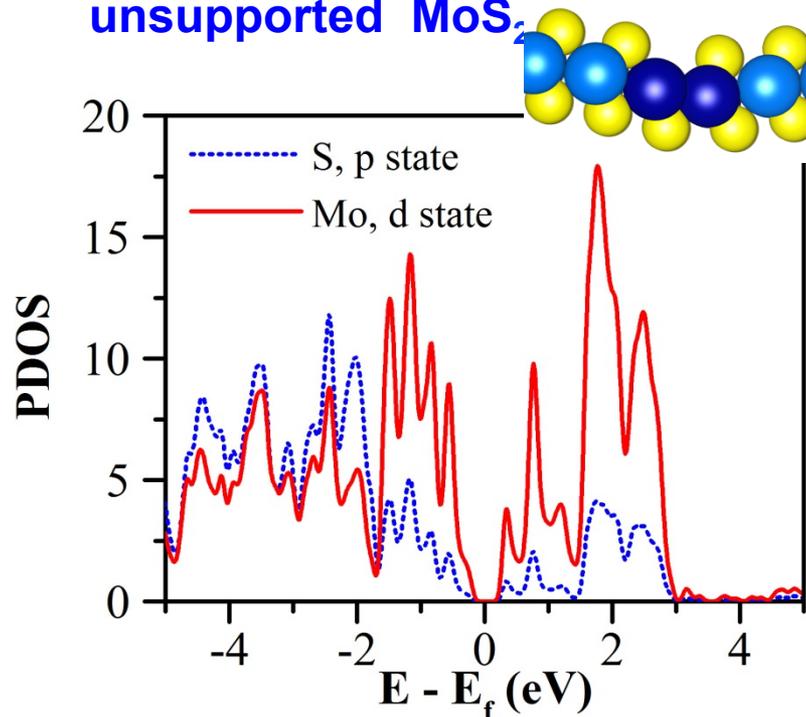
## □ Charge transfer



## □ Projected density of states of defect-laden MoS<sub>2</sub>/Cu(111)

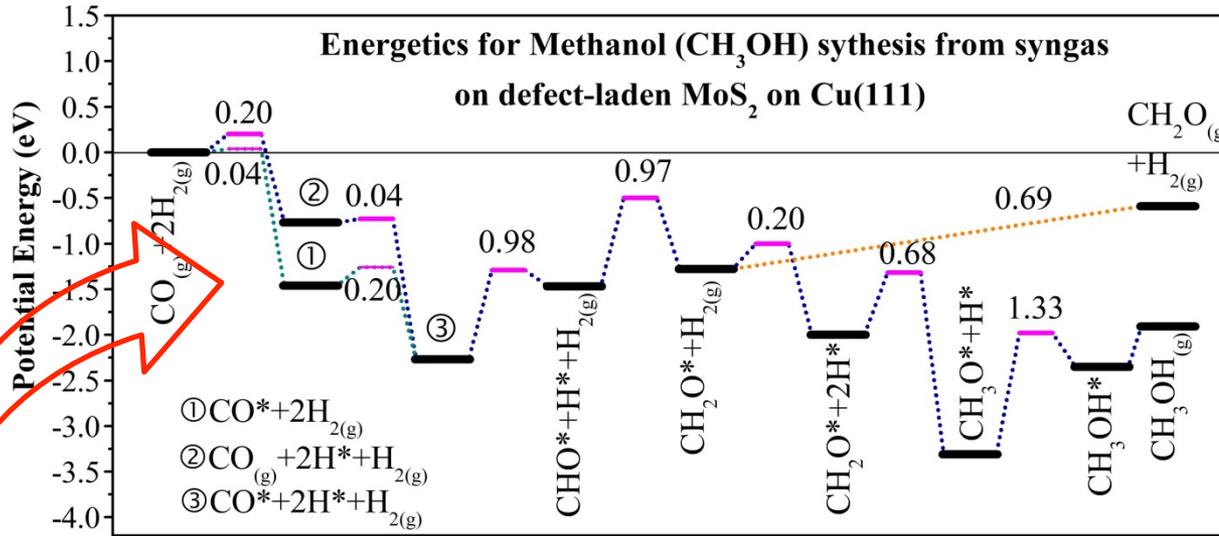


## □ PDOS of defect-laden, unsupported MoS<sub>2</sub>

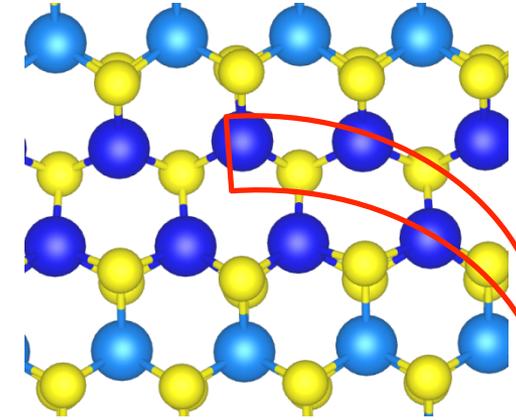


- Because of the **charge transfer** from Cu to MoS<sub>2</sub>, and the interaction between MoS<sub>2</sub> and Cu(111), the **frontier orbitals** are shifted towards the Fermi level and hence easily accessible to adsorbates.

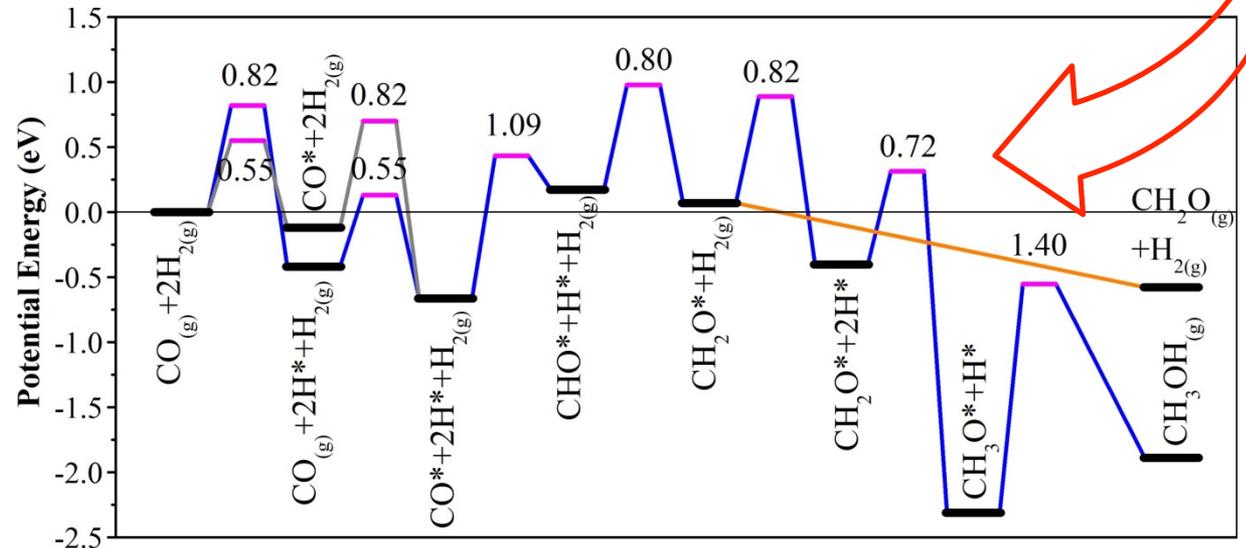
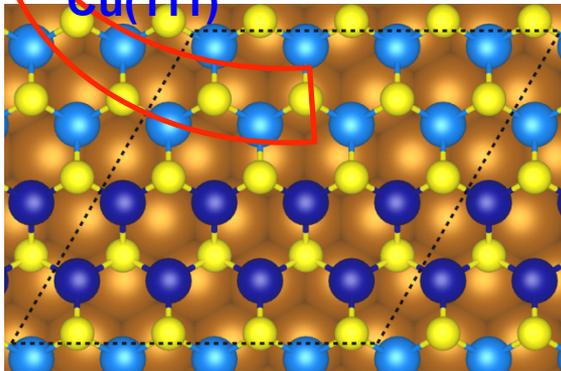
# Comparison of energetics



**Defect-laden unsupported  $\text{MoS}_2$**

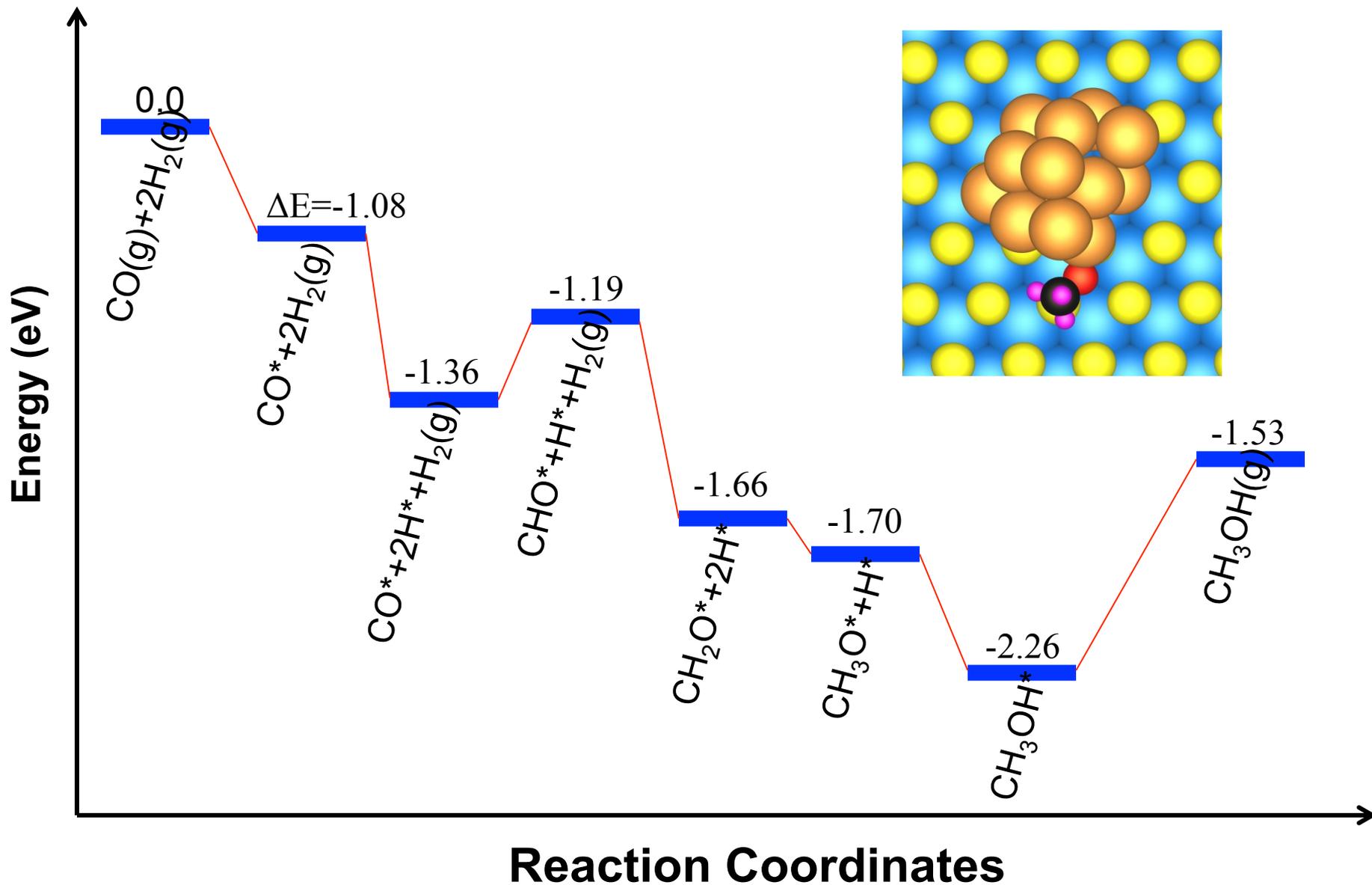


**Defect-laden  $\text{MoS}_2/\text{Cu}(111)$**

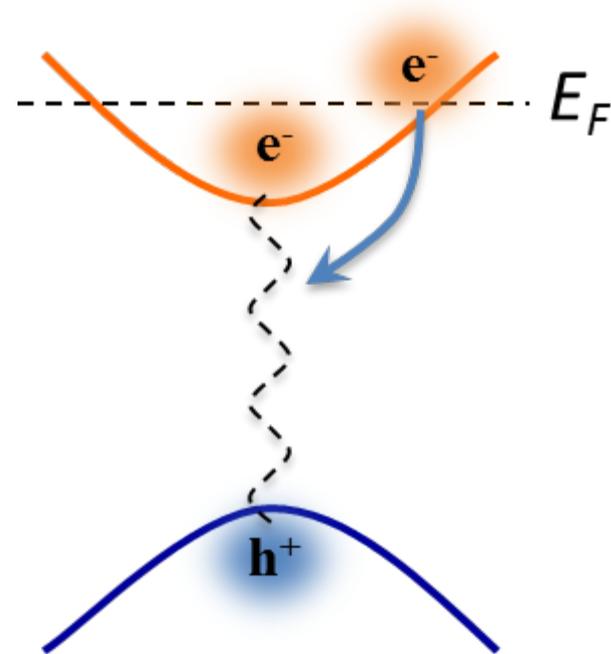
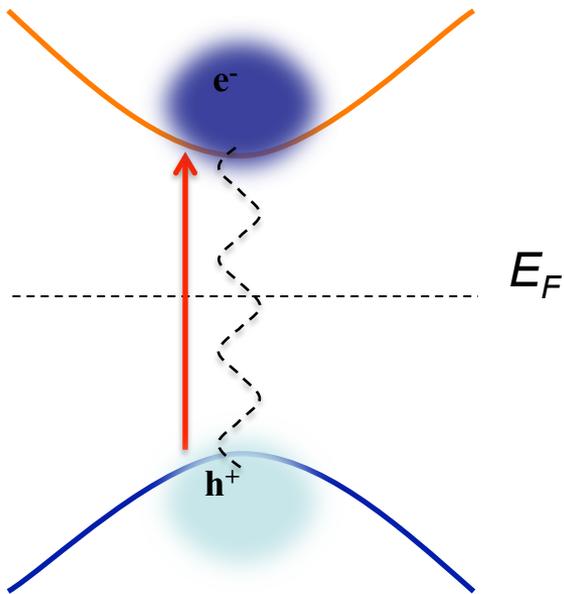


D. Le, T. B. Rawal, T. S. Rahman, *Jour. Phys. Chem C*, **118**, (2014), 5346

# Methanol formation on Au<sub>13</sub> NPs@MoS<sub>2</sub>

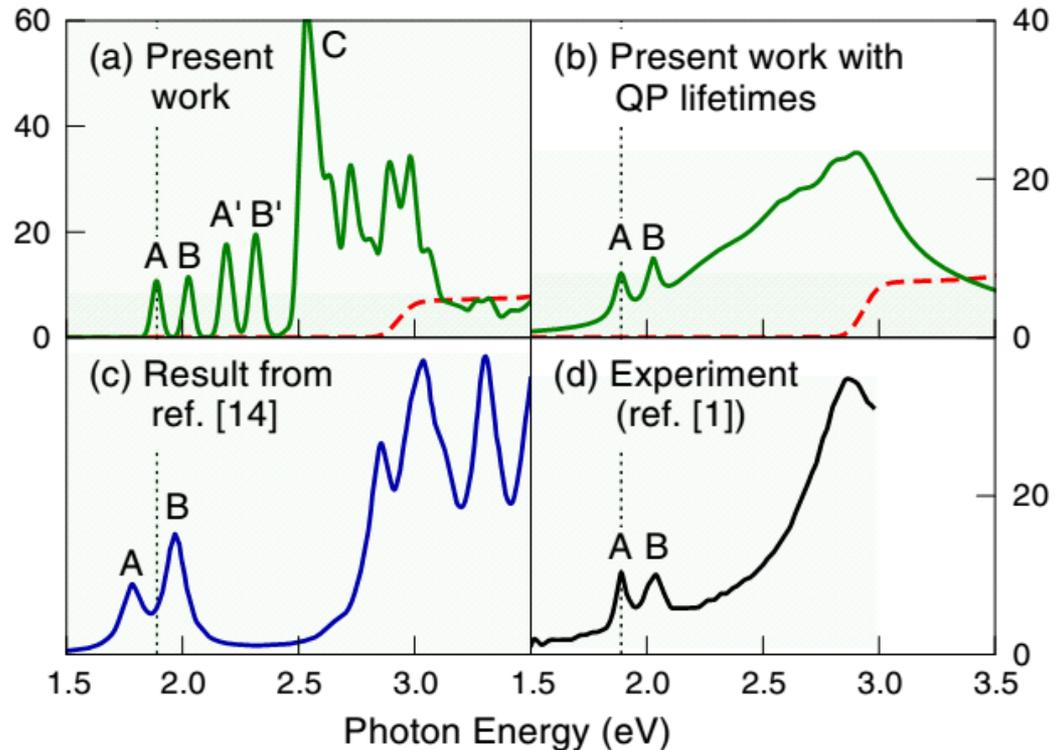
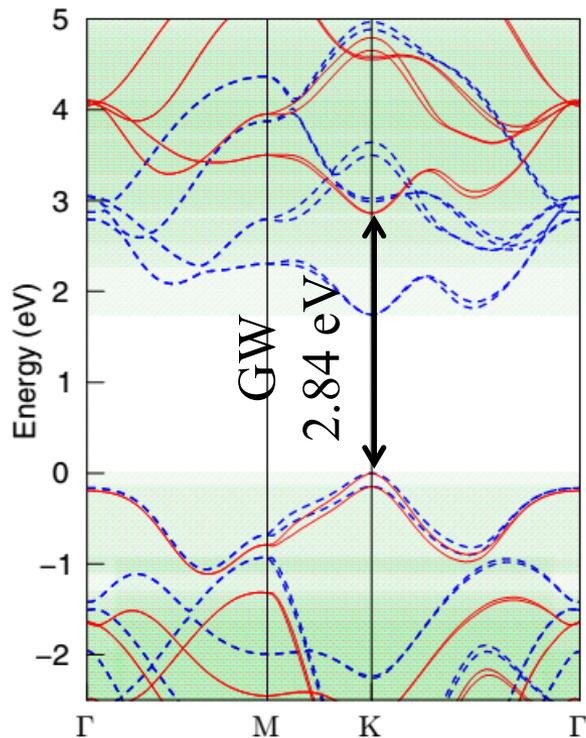


# Questions about fundamental band-gap of TDMCs: Excitons & trions



# Binding energy of exciton

- There used to be confusions about optical band gap and fundamental band gap because the experimental PL peaks are very close to DFT band-gap.
- DFT underestimates band-gap (for sure, every one knew)
- GW + Bethe-Salpeter equation: resolve very large binding energy of exciton. But they are too large. So is GW band gap.



From: D. Y. Qiu, F. H. da Jornada, and S. G. Louie, Phys. Rev. Lett. **111**, 216805 (2013).

# Binding energy of exciton

- Binding energy of trions in MoS<sub>2</sub> is about 18 meV (K. F. Mak *et al.*, Nat Mater **12**, 207 (2013))
- Binding energy of exciton should be about 10 times as large (theoretical estimation for isotropic 2D semiconductor with similar electron and hole masses).
- Recent experiment:

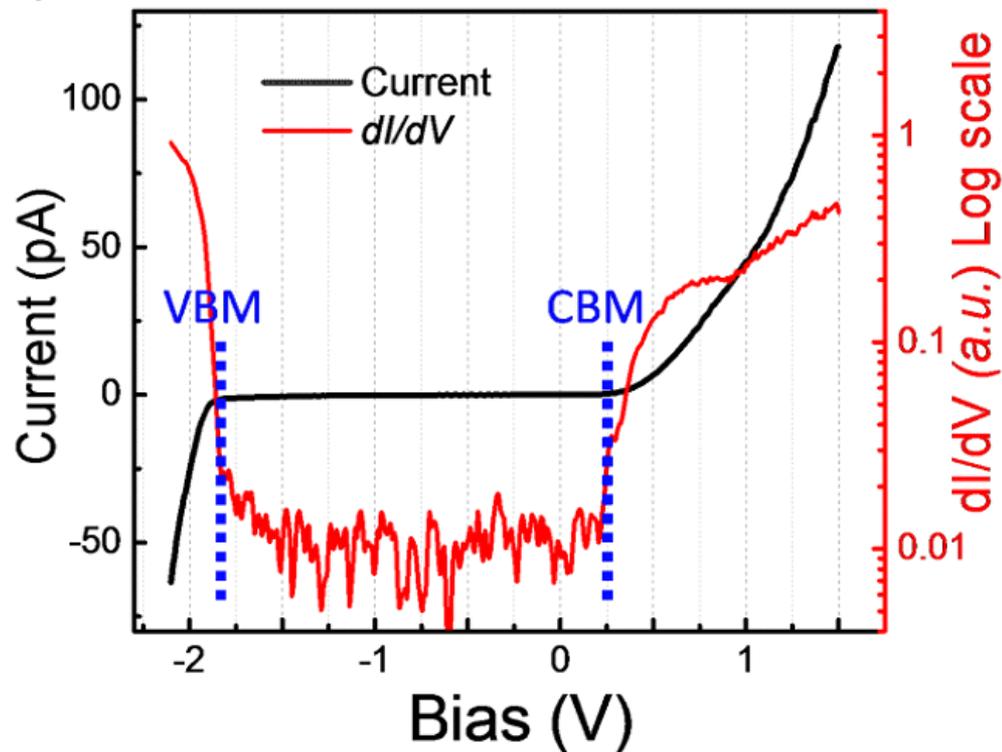
- Using STS to measure band-gap of MoS<sub>2</sub>: ~2.1 eV

Too small in comparison with GW. Little bit large vs. DFT

- Comparing with PL peak, binding energy of exciton: 220 meV

Too small VS. BSE

- Need to find better theory for accurate prediction.



C. Zhang *et al.*, arXiv:1401.5100

# Outline

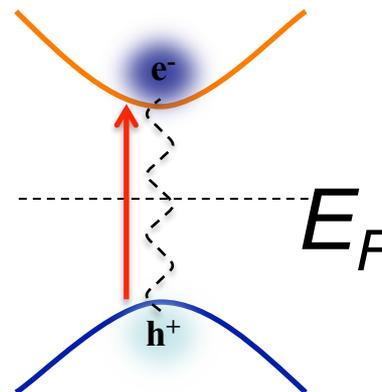
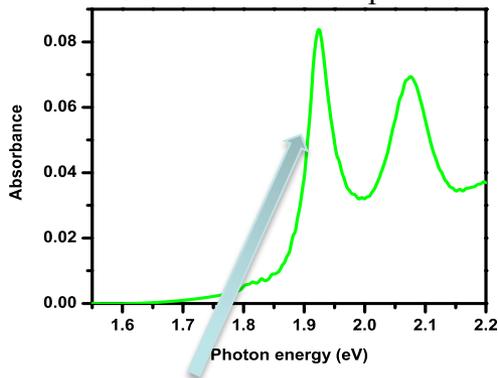
- **Motivation**
- **Density-Matrix TDDFT**
- **Excitons: in 1L vs. 2L systems**
- **Trions and biexcitons**
- **Ultrafast inter-layer hole transfer**
- **Ultrafast collective charge response**
- **Concluding Remarks**

# Motivation

## Excitons and the absorption spectrum in 1L MoS2

K.F. Mak et al., Nature Mat. 12, 207 (2013).

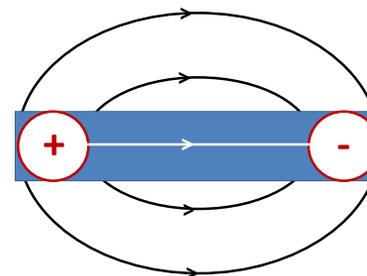
Exciton – bound electron-hole pair



Excitonic peak in the undoped MoS2

Material	Exciton energy, meV
GaAs	3.27
$\alpha$ -GaN	20.4
$\beta$ -GaN	26.0
CdS	28
CdSe	15

Exp.: Parenteau et al., J. Appl. Phys. 71, 3747 (1992); As et al., APL 70, 1311(1997); Muth et al., APL, 71, 2572 (1997); Jacobson et al., J. Crys. Growth 138, 225 (1994); Voigt et al., Phys. Stat. Sol. B 91, 189 (1979).



Binding energy,  $\sim 0.2-0.6\text{eV}$ , is extremely large even for systems with reduced dimensionality and low screening.

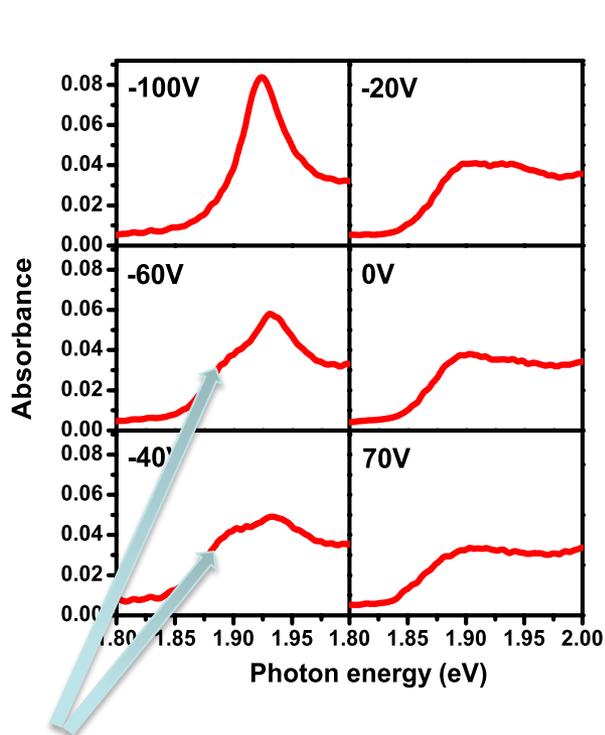
It is an order of magnitude larger than the values for “standard” bulk semiconductors, including the sulfur and selenium compounds.

# Excitons, trions & absorption spectrum

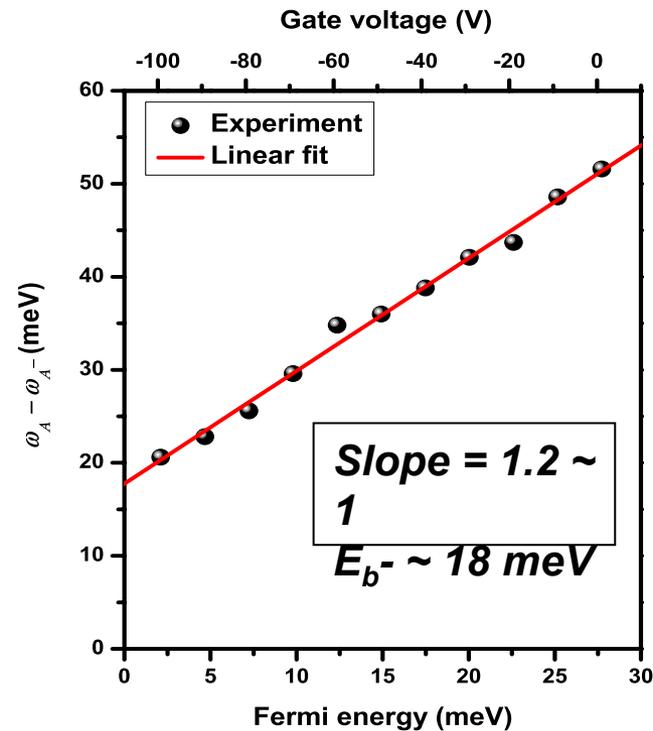
## Single Layer MoS<sub>2</sub>

K.F. Mak, K. He, C. Lee, G.H. Lee, J. Hone, T.F. Heinz, and J. Shan, Nature Mat. 12, 207 (2013).

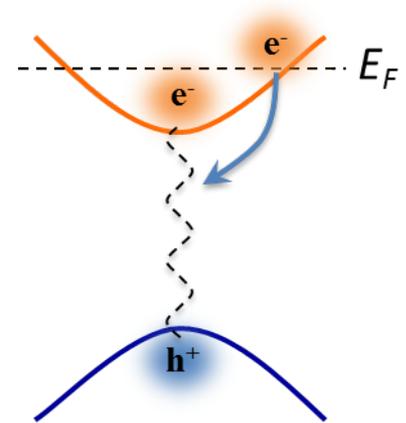
Trion – bound state of exciton and electron (hole)  
 Binding energy – energy necessary to separate them



Trion features below excitonic peak  
 in doped MoS<sub>2</sub>



Bound energy  $\sim 20$  meV  
 Trion effects must be pronounceable  
 at room temperature!

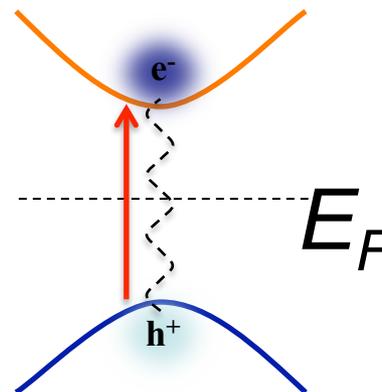
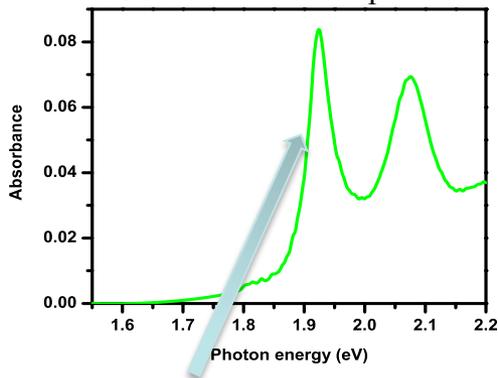


# Motivation

## Excitons in the absorption spectrum of 1L MoS<sub>2</sub>

K.F. Mak et al., Nature Mat. 12, 207 (2013).

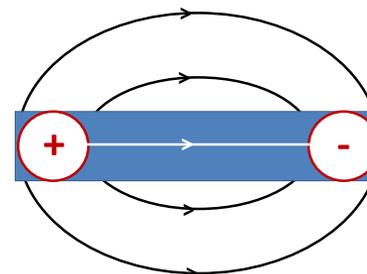
Exciton – bound electron-hole pair



Excitonic peak in the undoped MoS<sub>2</sub>

Material	Exciton Binding energy (meV)
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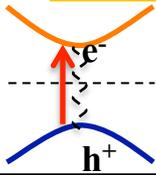
Exp.: Parenteau et al., J. Appl. Phys. 71, 3747 (1992); As et al., APL 70, 1311(1997); Muth et al., APL, 71, 2572 (1997); Jacobson et al., J. Crys. Growth 138, 225 (1994); Voigt et al., Phys. Stat. Sol. B 91, 189 (1979).



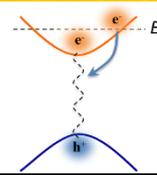
Binding energy  $\sim 0.2-0.6\text{eV}$ , is extremely large even for systems with reduced dimensionality and low screening.

It is an order of magnitude larger than the values for “standard” bulk semiconductors, including the sulfur and selenium compounds.

# Experimental Observations of excitations in 1L TMDC



**Excitons:**



**Trions:**

**Biexcitons:**

**MoS<sub>2</sub>**

K.F. Mak et al., PRL. **105**, 136805 (2010).  
F. Wu et al., PRB **91**, 075310 (2015)

**(220-570 meV)**

K.F. Mak et al., Nature Mat. **12**, 208 (2013)  
C. H. Lui, PRL **113**, 166801 (2014)  
C. Zhang et al., PRB **89**, 205436 (2014)

**(18-40 meV)**

E.J. Sie et al., **92**, 125417 (2015)

**(40-60 meV)**

**MoSe<sub>2</sub>**

J. S. Ross et al., Nat. Commun.  
**4**, 1474 (2013).  
Y. Li, PRL **113**, 266804 (2014).  
G.Wang et al., arxiv:1504.06333 (2015)  
A. Arora et al., arxiv:1509.06439 (2015)

**(500-550 meV)**

J. S. Ross et al., Nat. Commun.  
**4**, 1474 (2013).  
Y. Li, PRL **113**, 266804 (2014).  
A.Singh et al., arxiv:1507.04463 (2015)

**(30 meV)**

?

**WS<sub>2</sub>**

E.J. Sie et al., Nature Mat. **14**, 290 (2015)  
A. Chernikov et al., PRL **115**, 126802 (2015)  
G. Plechinger et al., arxiv:1507.01342 (2015)

**(320-700 meV)**

G. Plechinger et al.,  
arxiv:1507.01342 (2015)

**(30 meV)**

G. Plechinger et al.,  
arxiv:1507.01342 (2015)

**(65 meV)**

**WSe<sub>2</sub>**

A. Srivastava et al., Nature Phys. **11**, 141 (2015)  
A.A. Mitiouglu et al., arxiv:1507.00496 (2015)

**(370 meV)**

A. M. Jones et al., arXiv:1303.5318 (2013).  
A.A. Mitiouglu et al., arxiv:1507.00496 (2015)  
H.J. Liu et al., 2D Mat. **2**, 034004 (2015)

**(20-30 meV)**

Y. You et al.,  
Nature Phys. **11**, 477 (2015)

**(52 meV)**

**Most monolayers demonstrate strongly-bound  
exciton, trion and biexciton**

# Experimental Observations of excitations in 2L TMDC

## Homo-stacks:

**2L MoS<sub>2</sub>**

T. Jiang et al., Nature Nanotech. **9**, 825 (2014).  
K. Liu et al., Nature Comm. **5**, 4966 (2014)  
B.R. Carvalho et al, PRL **114**, 136403 (2015)  
J.-U. Lee et al., arxiv:1501.02525 (2015)  
H. Yu et al., arxiv:1504.01215 (2015)

**(~100-300 meV)**

**2L MoSe<sub>2</sub>**

H. Dery et al, PRB **92**, 125431 (2015)  
A. Arora et al., arxiv:1509.06439 (2015)  
H.J. Liu et al., 2D Mat. **2**, 034004 (2015)

**(160-260 meV)**

**2L WS<sub>2</sub>**

Q. Liu, PRL **114**, 087402 (2015)

**(~100-150 meV)**

**2L WSe<sub>2</sub>**

S. Kumar et al., arxiv:1509.01085 (2015)  
M. Yankowitz, PRL **115**, 136803 (2015)  
H. Dery, PRB **92**, 125431 (2015)  
H.J. Liu et al., 2D Mat. **2**, 034004 (2015)

**(130-330 meV)**

**2L WS<sub>2</sub>**

B. Zhu, PNAS **111**, 11606 (2014)

**(45 meV)**

## Excitons

## Hetero-stacks:

**MoS<sub>2</sub>-MoSe<sub>2</sub>**

L.H.G Tizei et al., PRL **114**, 107601 (2015)

**(~100-400 meV)**

**MoS<sub>2</sub>-WS<sub>2</sub>**

X. Hong et al., Nature Nanotech. **9**, 682 (2014)  
Q. Liu et al., PRL **114**, 087402 (2015)

**(~100 meV)**

**MoSe<sub>2</sub>-WSe<sub>2</sub>**

P. Rivera et al., Nature Comm. **6**, 6242 (2015)

**(~100-300 meV)**

## Trions

**2L MoSe<sub>2</sub>**

H.J. Liu et al., 2D Mat. **2**, 034004 (2015)

**(~28 meV)**

**Several two-layer systems demonstrate excitonic states  
More trions and biexcitons - coming soon ?...**

# TDDFT: density-matrix formulation

**Kohn-Sham equations:**

$$H\psi_k^v(r,t) = i \frac{\partial}{\partial t} \psi_k^v(r,t), \quad n(r,t) = 2 \sum_{k \in B.Z.} |\psi_k^v(r,t)|^2$$
$$H = -\frac{1}{2m} \nabla^2 + V_{nucl}(r) + V_{ext}(r,t) + V_H[n](r,t) + V_{xc}[n](r,t)$$

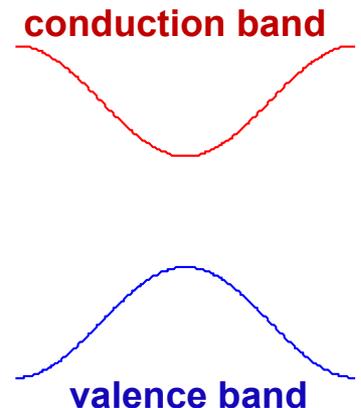
The time-dependent wave function is expanded in terms of the static wave functions  $\psi_k^{l(0)}(r)$ , that are the solution of the static DFT Kohn-Sham equations

$$H\psi_k^{l(0)}(r) = \varepsilon_k^l \psi_k^{l(0)}(r)$$

In this case:

$$\psi_k^v(r,t) = \sum_l c_k^l(t) \psi_k^{l(0)}(r)$$

**Two-band approximation:**



# TMDC systems: excitons and trions

## Monolayers

Slater XC, screening  $\epsilon$

(binding energies in meV)

System	Exciton (exp. in brackets)	Trion (exp. in brackets)
MoS2	361 (220-570)	40 (18-40)
MoSe2	388 (500-640)	43 (30)
WSe2	210 (370-790)	5 (20-30)

## Bi-layers

(binding energies in meV)

System	Exciton (exp. in brackets)	Trion (exp. in brackets)
MoS2	204 (~100-300)	27
MoSe2	208 (160-260)	22 (28)
WSe2	133 (130-330)	4

TDDFT results give correct order of magnitude for the excitations in most cases (except trions for WSe2) and correct ratio between different energies:

- Trion energies are ~10 smaller than the exciton ones
- In 2L, the energies are ~ 1/2 that of 1L case

Exp.:

Zhang et al., Nano Lett. **14**, 2443 (2014).

Ugeda et al., arXiv:1404.2331 (2014).

He et al., PRL **113**, 026803 (2014)

Cheiwchanchamnangij et al., PRB **85**, 205302 (2012).

Berkelbach et al., PRB **88**, 045318 (2013).

Liu et al., 2D Mat. **2**, 034004 (2015).

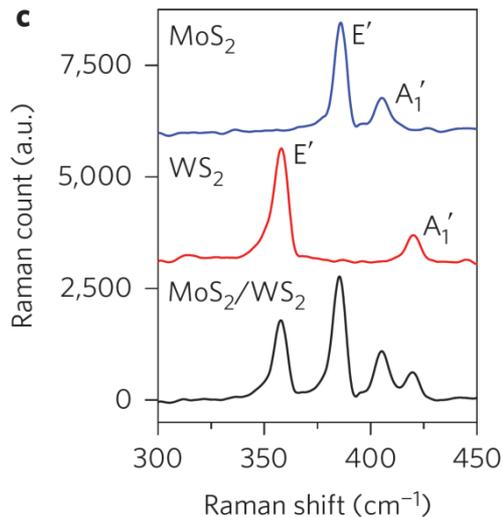
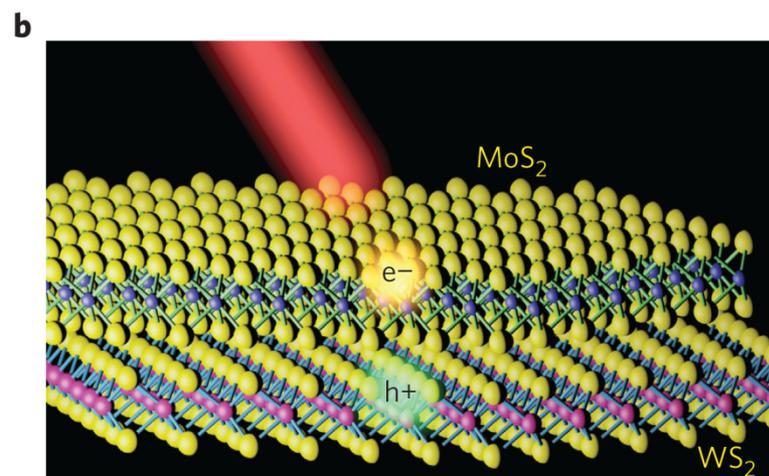
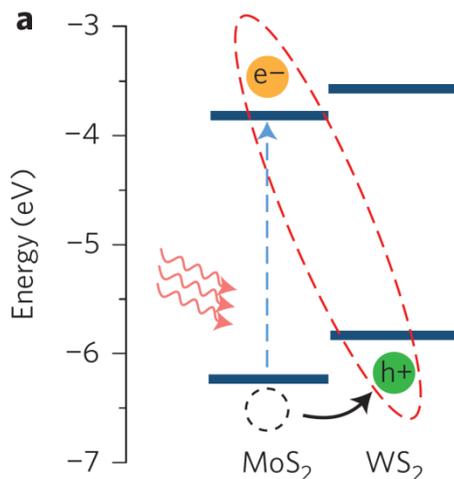
# Ultrafast electron-hole separation in bi-layer TMDCs

## MoS<sub>2</sub>-WS<sub>2</sub>

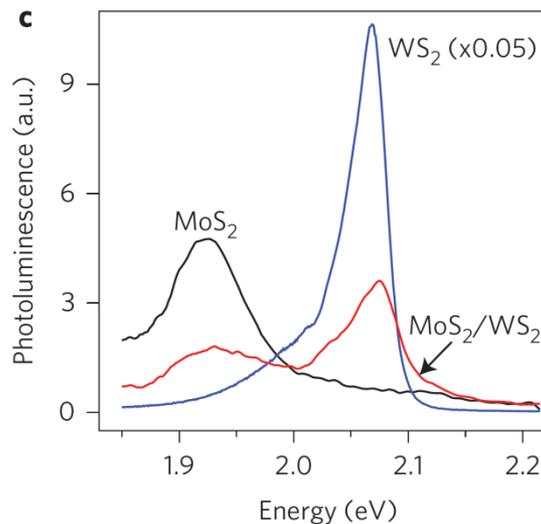
50fs inter-layer hole transfer,  
unusual for a van der Waals system

## Type II Heterojunction

Hong et al., Nature Nano 9, 682 (2014)



Raman spectrum of the coupled layers  
is practically the sum of the individual  
layer spectra, suggesting their weak interaction



Quenched exciton luminescence in the coupled  
system support the hole transfer

# Questions

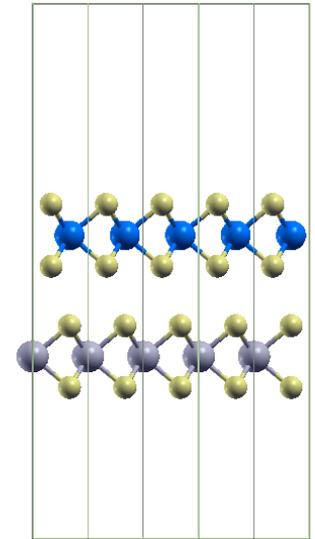
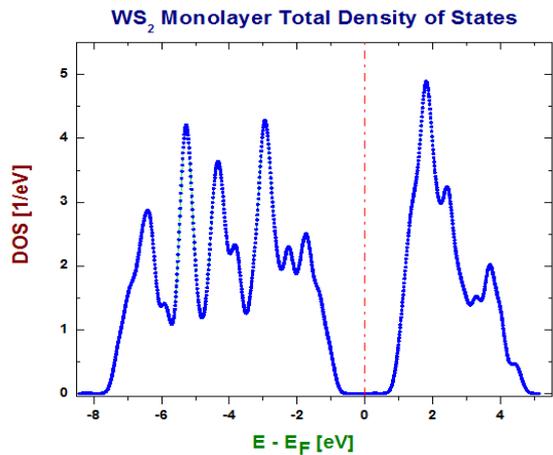
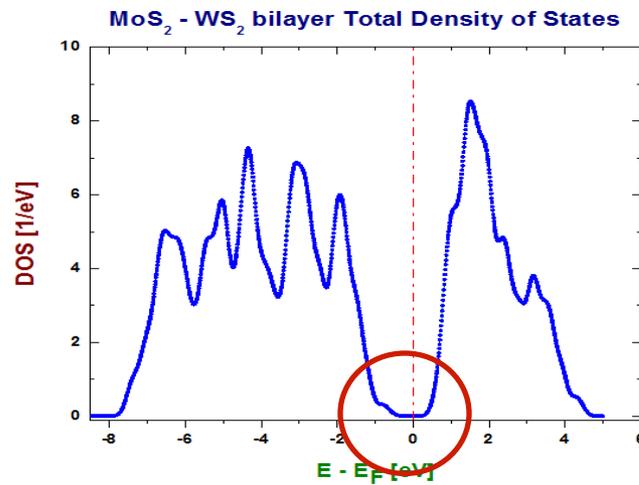
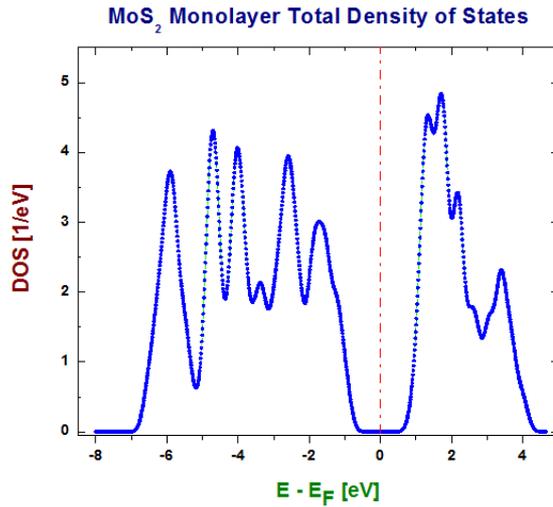
- How do strong electron–electron interactions and excitonic effects affect charge transfer processes?
- How fast can charge transfer take place between van der Waals-coupled layers?

Note that exciton binding energy is larger in the single layer than in the bilayer

- Will the exciton in the bilayer decay?

# Ultrafast electron-hole separation in MoS<sub>2</sub>-WS<sub>2</sub>

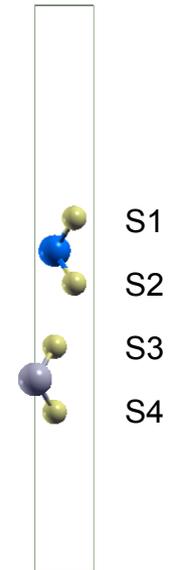
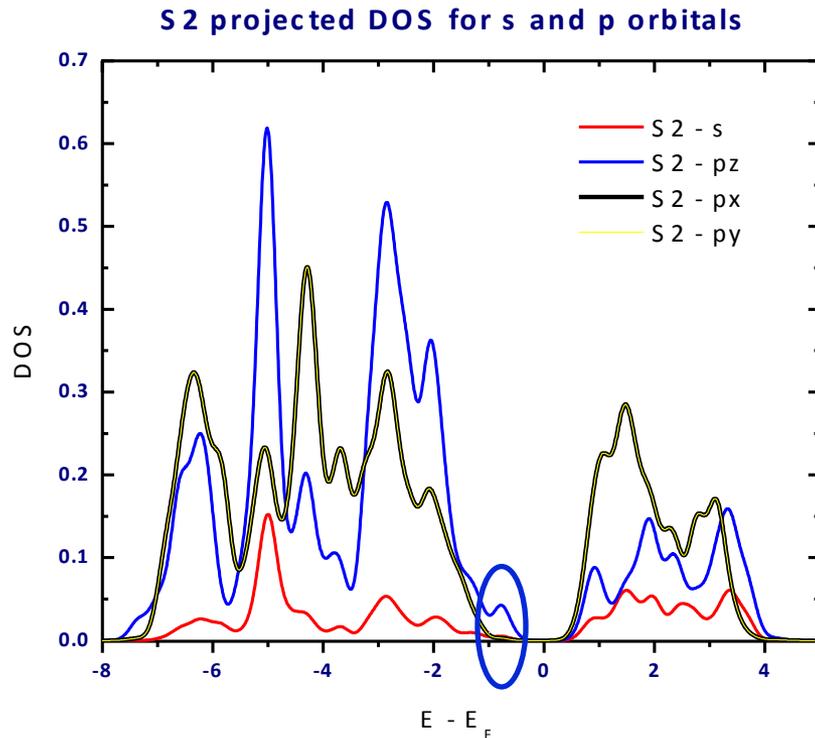
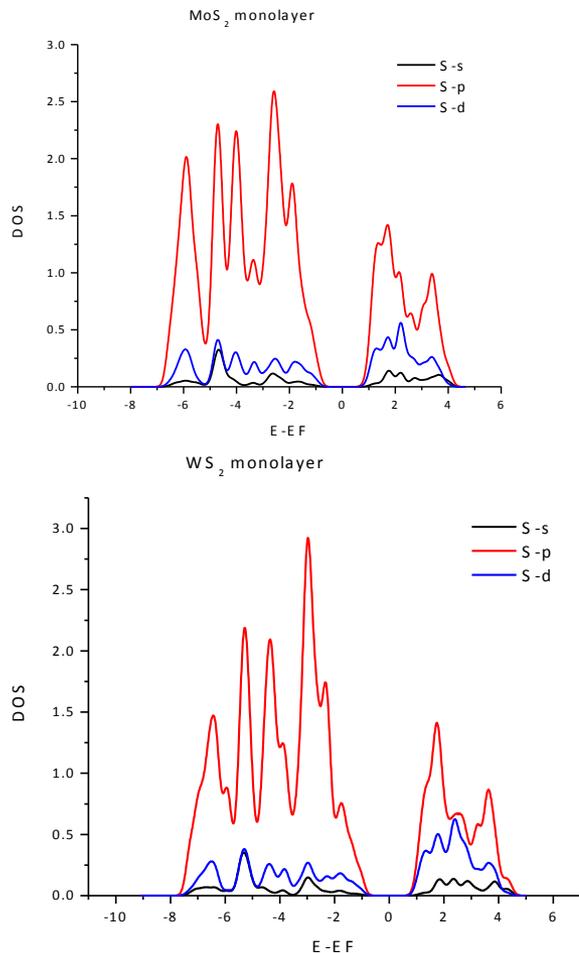
## DFT DOS



**In the coupled system, the valence (hole) bands have significantly different features as compared to the isolated monolayers**

# Ultrafast electron-hole separation in MoS<sub>2</sub>-WS<sub>2</sub>

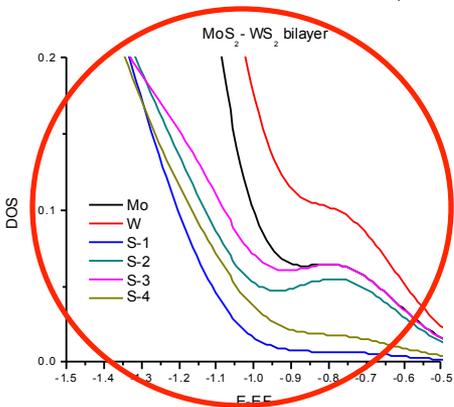
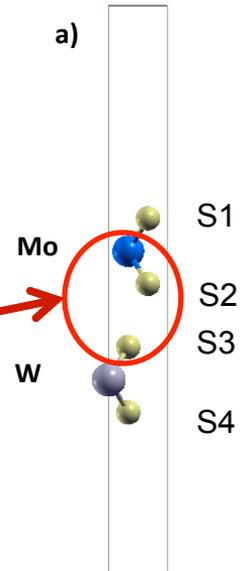
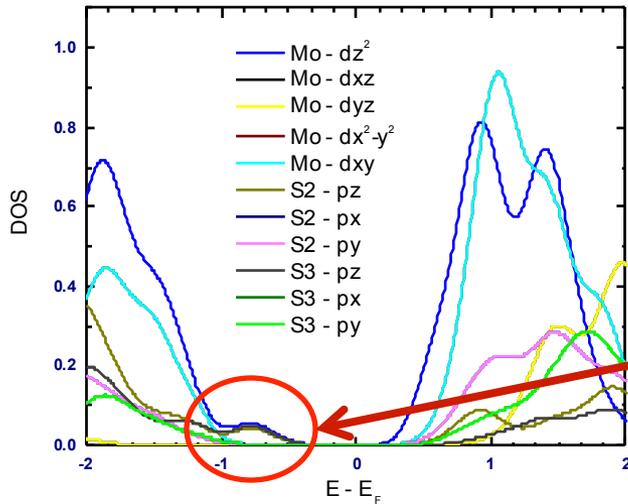
## The nature of the hole states



**The low-energy holes are mainly formed by p<sub>z</sub>-orbital of the sulfur atoms, suggesting their inter-layer hybridized nature**

# Bi-layer MoS2-WS2: electronic spectrum

Mo, S2 and S3 projected DOS



**DFT calculations demonstrate that, contrary to one-layer MoS2, in the coupled MoS2-WS2 system there is a significant amount of the hole charge in the “internal/central” S layer.**

**The vicinity of the MoS2 hole charge to the WS2 layer facilitates the inter-layer hole transfer.**

# Ultrafast electron-hole separation in bi-layer TMDCs

## Exciton binding energies (meV)

TDDFT, Slater XC kernel

System	Exciton binding energy
2L MoS2	204
2L MoSe2	208
MoS2-WS2	180

## Hole transfer and exciton recombination times (ps)

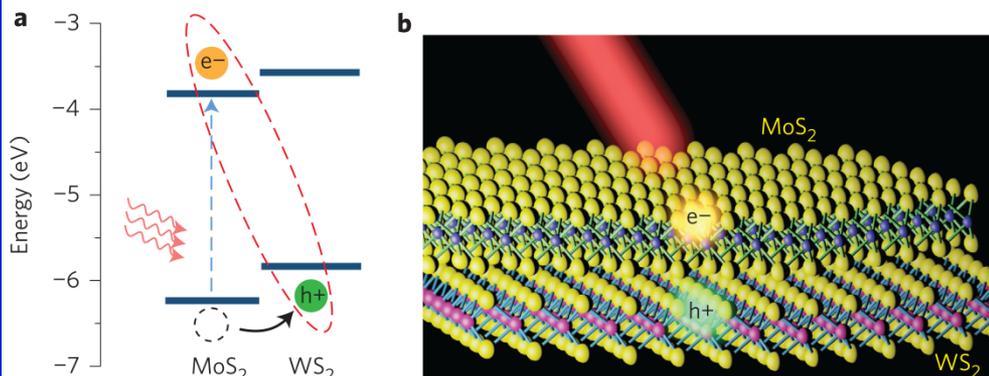
System	Hole transfer time	Exciton lifetime
2L MoS2	0.36	10.0
2L MoSe2	0.42	14.1
MoS2-WS2	0.12	5.4

Lifetimes obtained from the results for the oscillator strength:

$$\tau \sim \frac{1}{|\langle \psi^2 | er | \psi^1 \rangle|^2}$$

## MoS2-WS2

50fs inter-layer hole transfer



Hong et al., Nature Nano 9, 682 (2014)

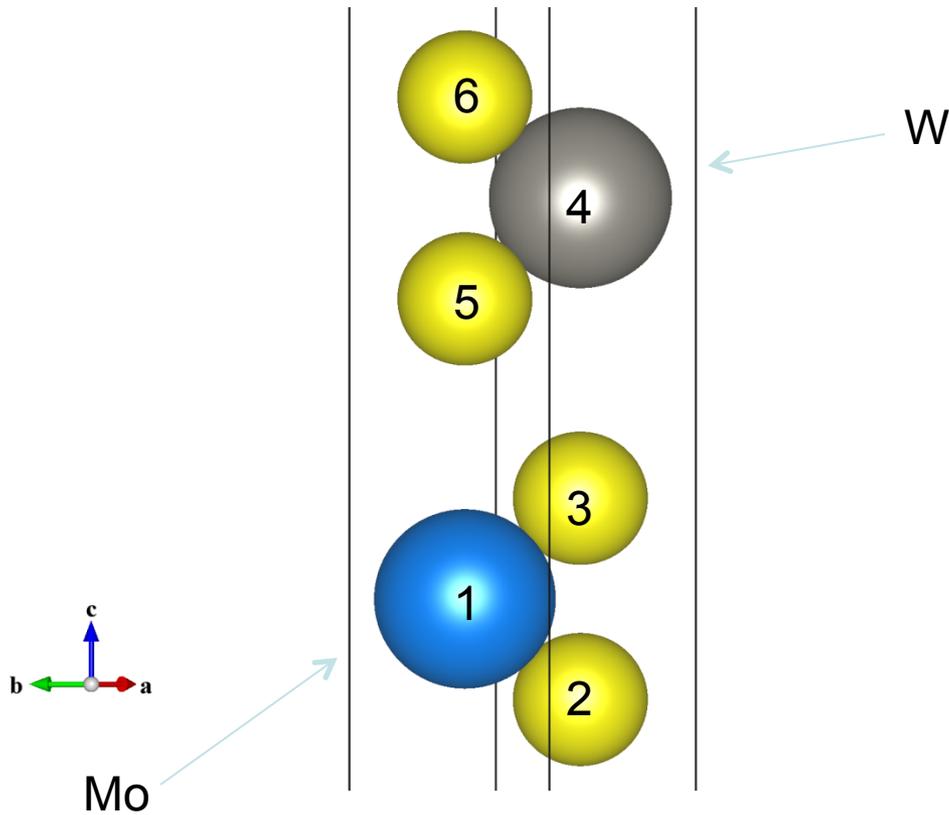
**For all the systems, the hole transfer times are much shorter than the MoS2 exciton lifetime and are in agreement with the available experimental data for MoS2-WS2.**

# Conclusion

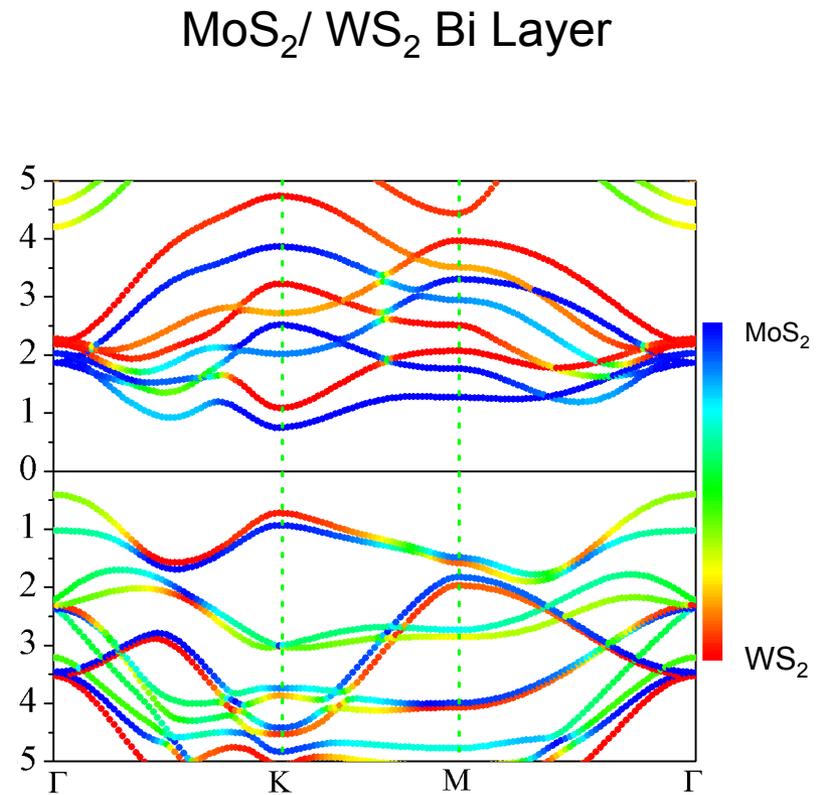
- ◆ **Single layer MoS<sub>2</sub> is indeed a promising material**
- ◆ **Manipulation of characteristics possible in many ways:**
  - Support
  - Defects
  - Edges, joint edges
  - Hydrogenation etc
- ◆ **Growth of large scale wafers a challenge**
- ◆ **Excitons/trions may have large technological implications**
- ◆ **Probe of ultrafast processes may shed light of interactions**
- ◆ **Much work remains to be done**

.

**Thank you for your attention!**

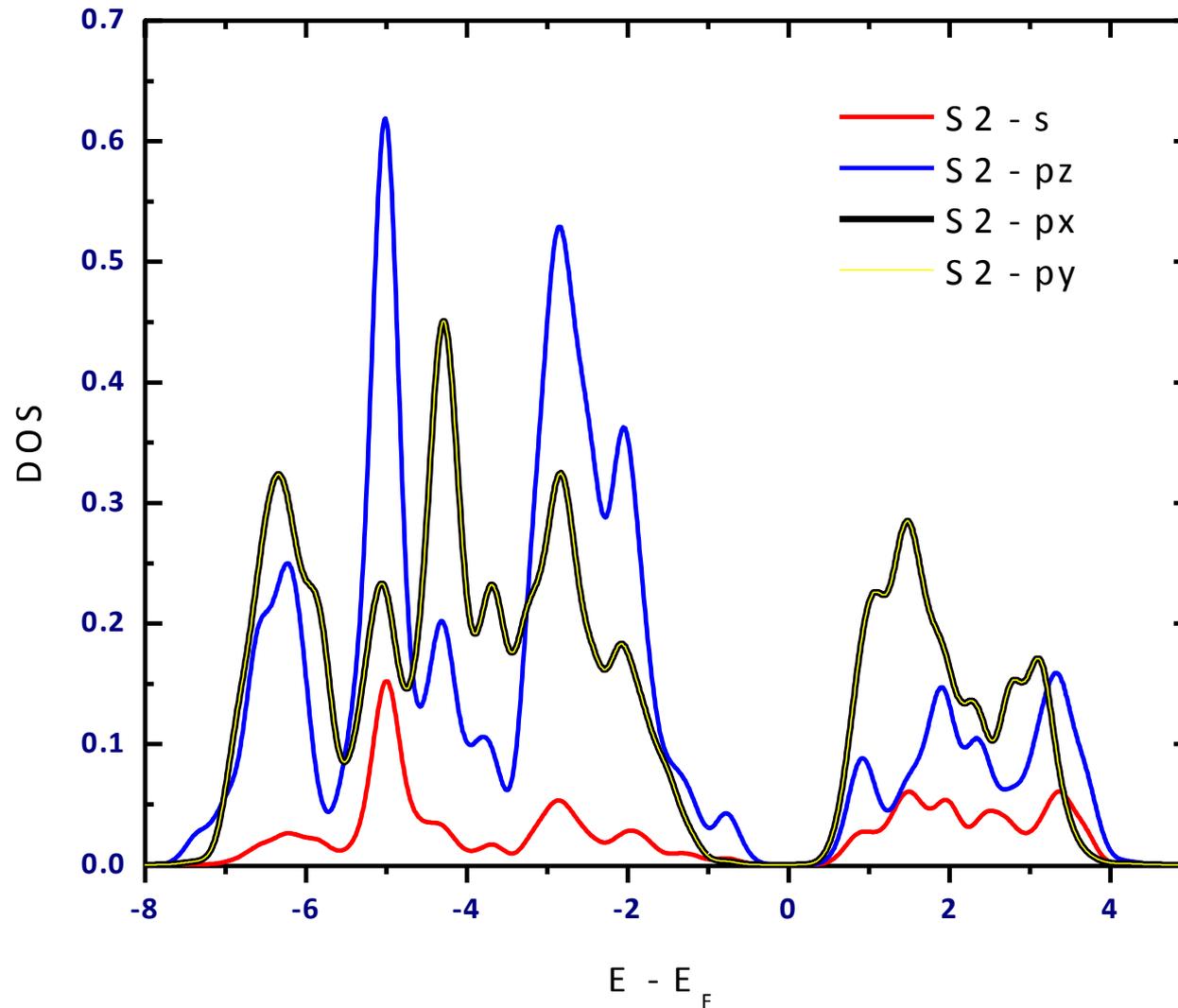


Atom number is a reference for the next slide.



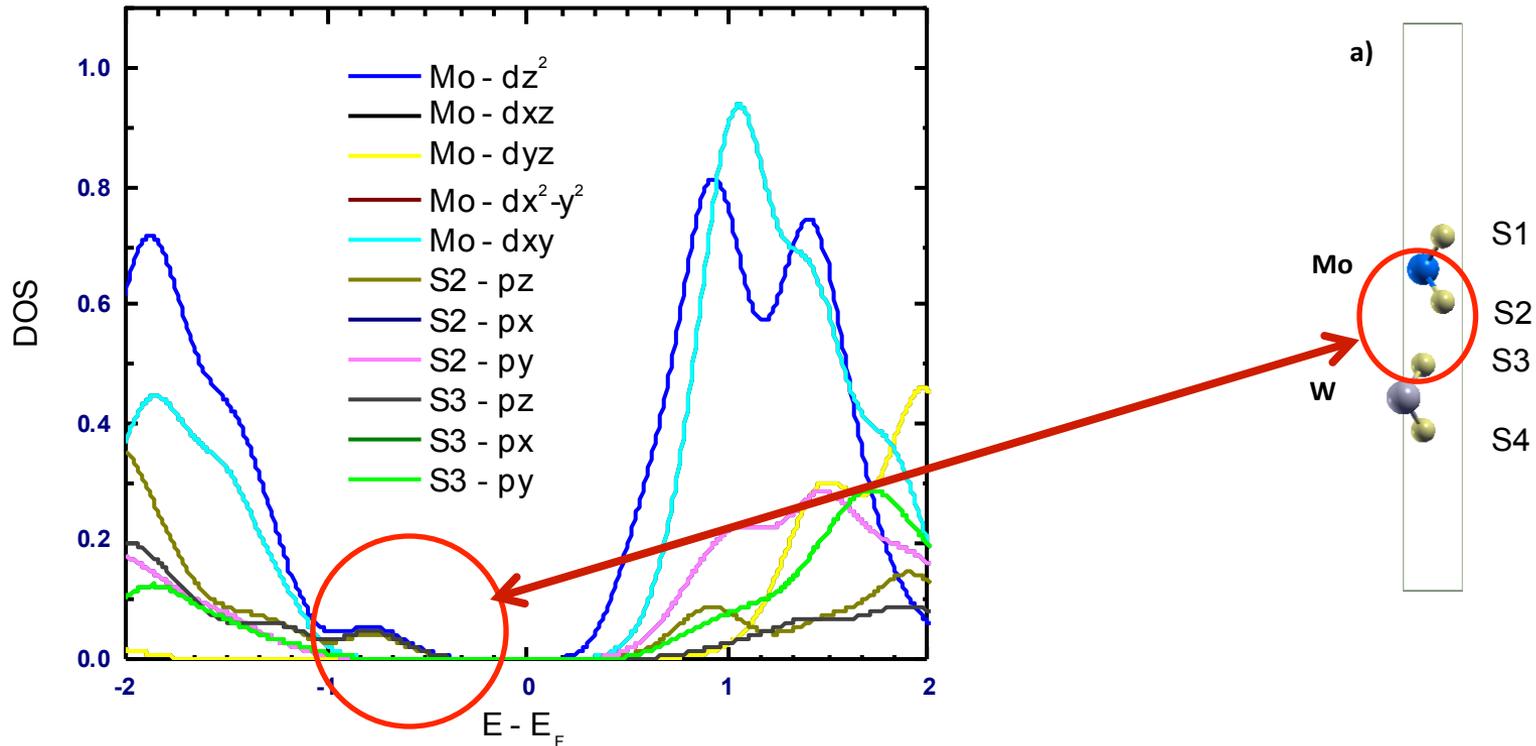
# Bi-layer MoS<sub>2</sub>-WS<sub>2</sub>: electronic spectrum

## S 2 projected DOS for s and p orbitals



# Bi-layer MoS<sub>2</sub>-WS<sub>2</sub>: electronic spectrum

## Mo, S2 and S3 projected DOS



Strong hybridization of the interlayer charges for the hole excitations, favors its migration to W atoms

# Ultrafast electron-hole separation in bi-layer TMDCs

## One-layer Exciton binding energies (meV)

TDDFT, Slater XC kernel

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2L MoS2	204
2L MoSe2	208
MoS2-WS2	180

## Hole transfer and exciton recombination times (ps)

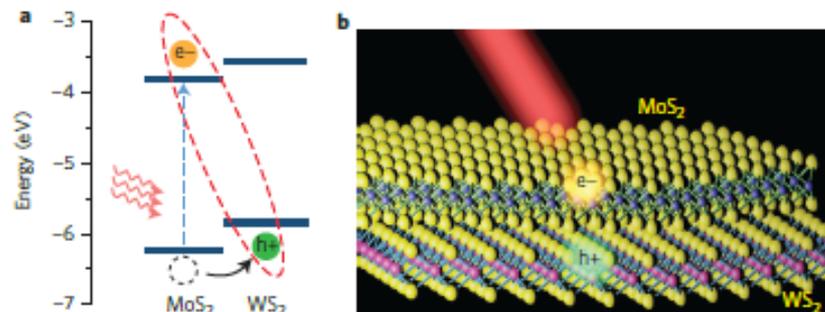
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2L MoS2	0.36	10.0
2L MoSe2	0.42	14.1
MoS2-WS2	0.12	5.4

Lifetimes obtained from the results for the oscillator strength:

$$\tau \sim 1 / \langle \psi^{\uparrow 2} | e \mathbf{r} | \psi^{\uparrow 1} \rangle \langle \psi^{\downarrow 1} | e \mathbf{r} | \psi^{\downarrow 2} \rangle$$

## MoS2-WS2

50fs inter-layer hole transfer



Hong et al., Nature Nano 9, 682 (2014)

## Competition between the inter-layer hole migration and intra-layer e-h recombination times

# Part I

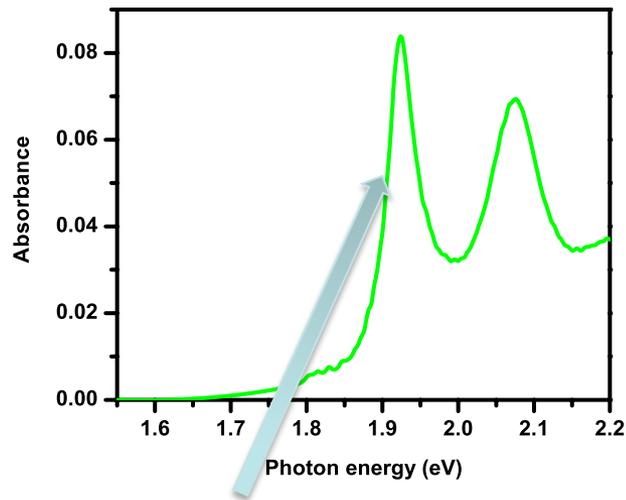
## MoS<sub>2</sub> trion

MoS<sub>2</sub> trion

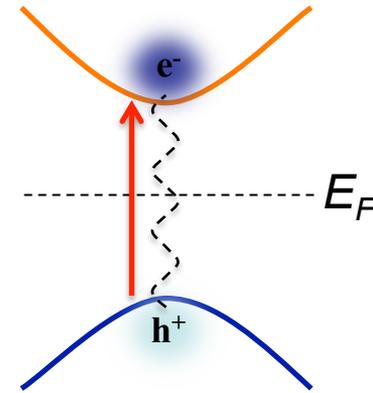
# Experimental observation of excitons and trions in doped monolayer MoS<sub>2</sub>

K.F. Mak, K. He, C. Lee, G.H. Lee, J. Hone, T.F. Heinz, and J. Shan, Nature Mat. (in press).

Exciton – bound electron-hole pair



Excitonic peak in undoped MoS<sub>2</sub>

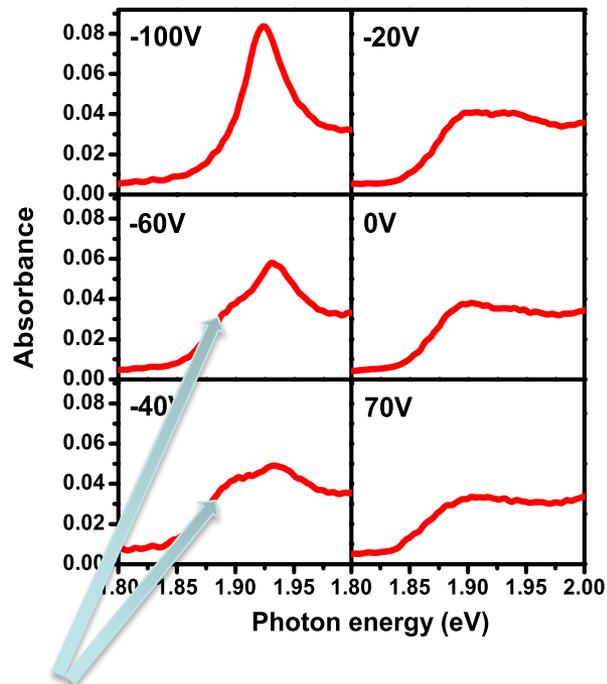


Bound energy  $\sim 1$  eV  
extremely large even for systems  
With reduced dimensionality!

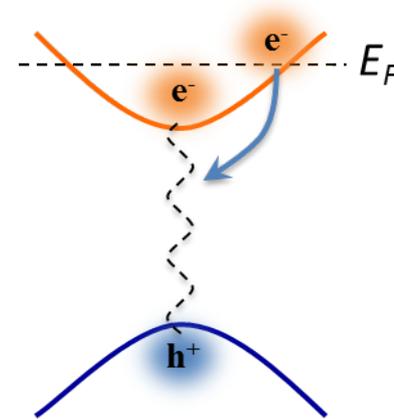
# Experimental observation of excitons and trions in doped monolayer MoS<sub>2</sub>

K.F. Mak, K. He, C. Lee, G.H. Lee, J. Hone, T.F. Heinz, and J. Shan, Nature Mat. 12, 207 (2013).

Trion – bound state of exciton and electron (hole)  
Binding energy – energy necessary to separate them



Trion features below excitonic peak  
in doped MoS<sub>2</sub>



Bound energy  $\sim 20$ meV  
Trion effects must be pronounceable  
at room temperature!

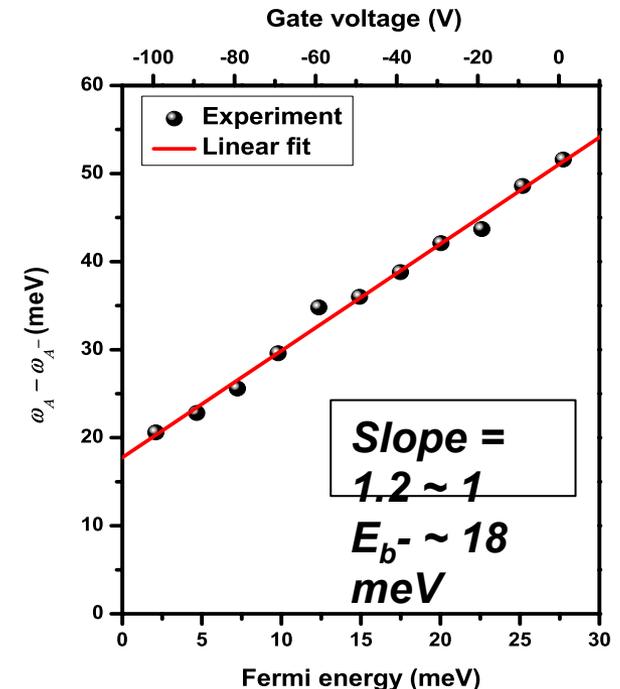
# Solutions: adiabatic LDA approximation

$$v_{xc}[n](r, t) = -q^2 \left( \frac{3}{\pi} \right)^{1/3} n^{1/3}(r, t)$$

60 independent k-points in the Brillion zone

Excitation	Binding energy	exp
Exciton	312meV	~1000meV
Trion	744meV	~20meV

Trion binding energy is strongly overestimated by LDA since it includes only local electron-hole attraction (almost neglecting e-e repulsion (screened by  $\epsilon \sim 2.8$ ) when electron is closer to the hole)



Many body Wannier theory predicts correct estimation of the exciton energy

( T. Cheiwchanchamnangij, W.R.L. Lambrecht, Phys. Rev. B 85, 205302 (2012)

## Solutions: three-dimensional long-range kernel

$$f_{XC}(r, r') = -\frac{1}{|r - r'|}$$

Excitation	Binding energy	exp
Exciton	7meV	~1000meV
Trion	0meV	~20meV

## Solutions: two-dimensional long-range kernel

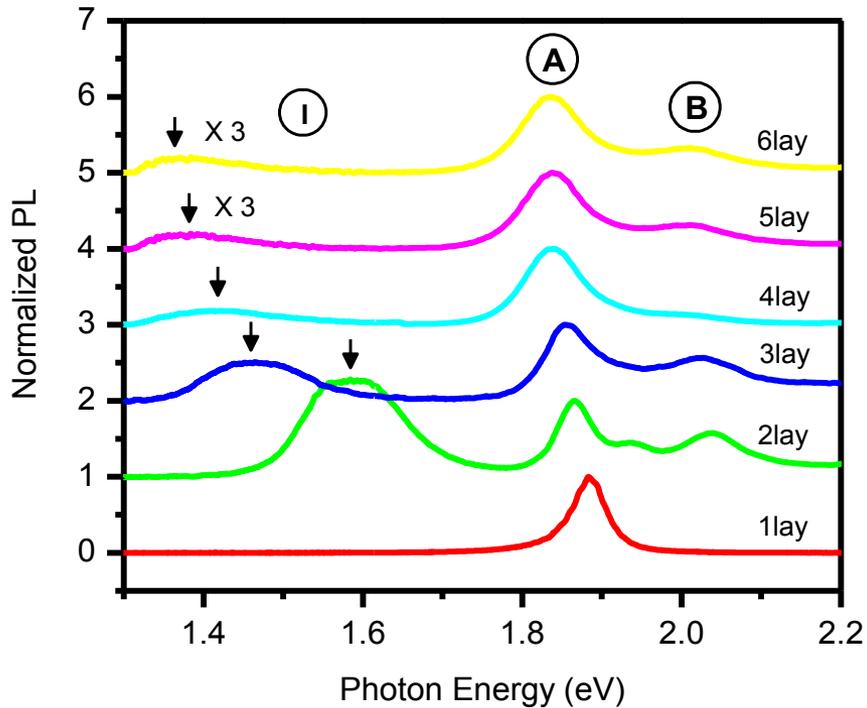
$$f_{XC}(r, r') = 1/\epsilon \ln(|r - r'|/L)$$

(solution of 2D Poisson equation, L-dimensionality scale=14Bohr)

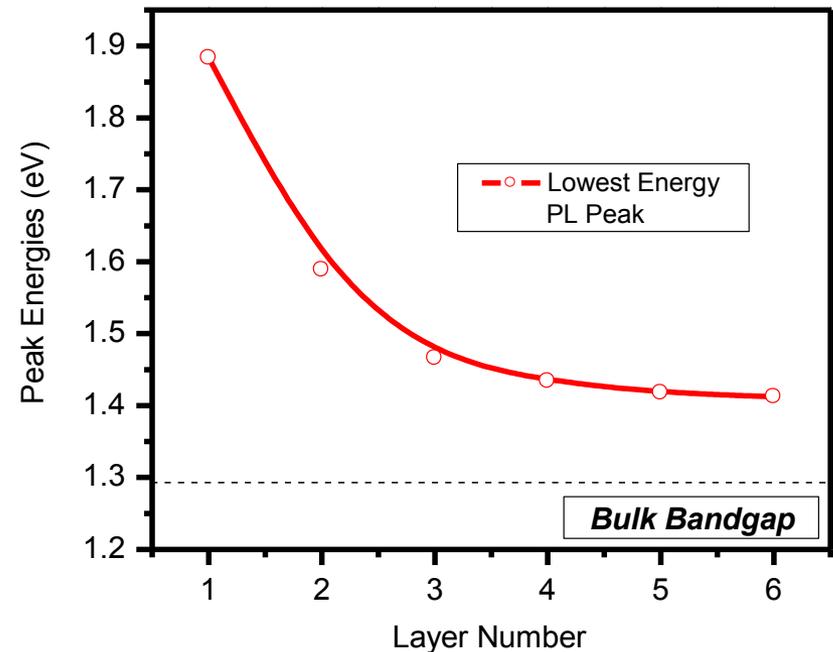
Excitation	Binding energy	exp
Exciton	27meV	~1000meV
Trion	50meV	~20meV

Long-range kernel leads to underestimation of the exciton energy but correct order of magnitude for trions  
This is connected with the correct LR nature of the exciton-electron interaction

# Band Gap Variation in Few-Layer MoS<sub>2</sub>



Band gap decreases as layer number increases



# Summary of MoS<sub>2</sub> band gap

Method	Value (eV)	Reference	Note
Photoluminescence	1.8-1.9	[1,2]	Optical band gap
Scanning Tunneling Spectroscopy (STS)	2.15	[3]	
DFT-LDA	1.81	[4]	
DFT-PBE	1.68	[5]	
DFT-optB88-vdW	1.67	[4]	
GW	2.84	[6]	G <sub>1</sub> W <sub>0</sub> approximation
DFT-HSE06	2.25	[7]	

[1] K. Mak *et al.*, Phys. Rev. Lett. **105**, 136805 (2010).

[2] A. Splendiani *et al.*, Nano Lett. **10**, 1271 (2010).

[3] C. Zhang *et al.*, Nano Lett. **14**, 2443 (2014).

[4] A. Ramirez-Torres, D. Le, and T. S. Rahman, IOP Conf. Ser.: Mater. Sci. Eng. **76**, 012011 (2015).

[5] J. Mann *et al.*, Adv. Mater. **26**, 1399 (2014).

[6] D. Y. Qiu, F. H. da Jornada, and S. G. Louie, Phys. Rev. Lett. **111**, 216805 (2013).

[7] E. Ridolfi *et al.*, to be pulished.